

*N. Rok*

PROGRAM & REPORT

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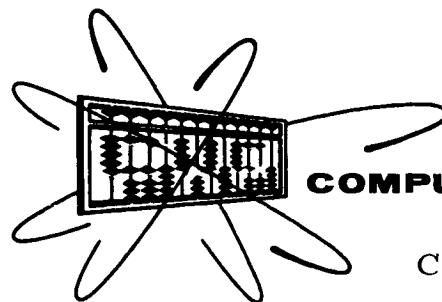
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IN SPHERICAL HARMONICS

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FACILITY FORM 602



**COMPUTER USAGE COMPANY, INC.**

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PART 6

SOLVE PROGRAM

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SECTION I  
INTRODUCTION

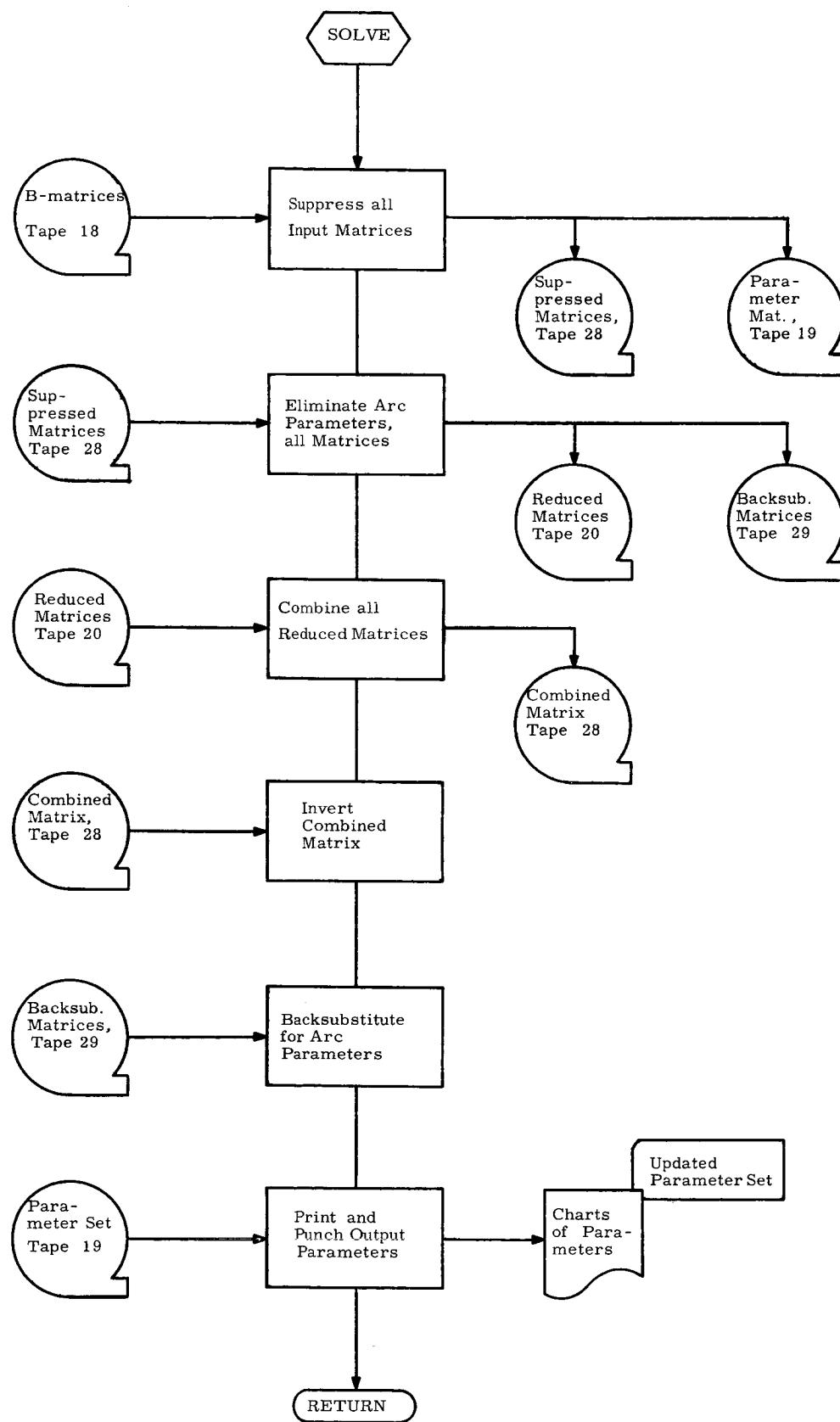
## INTRODUCTION

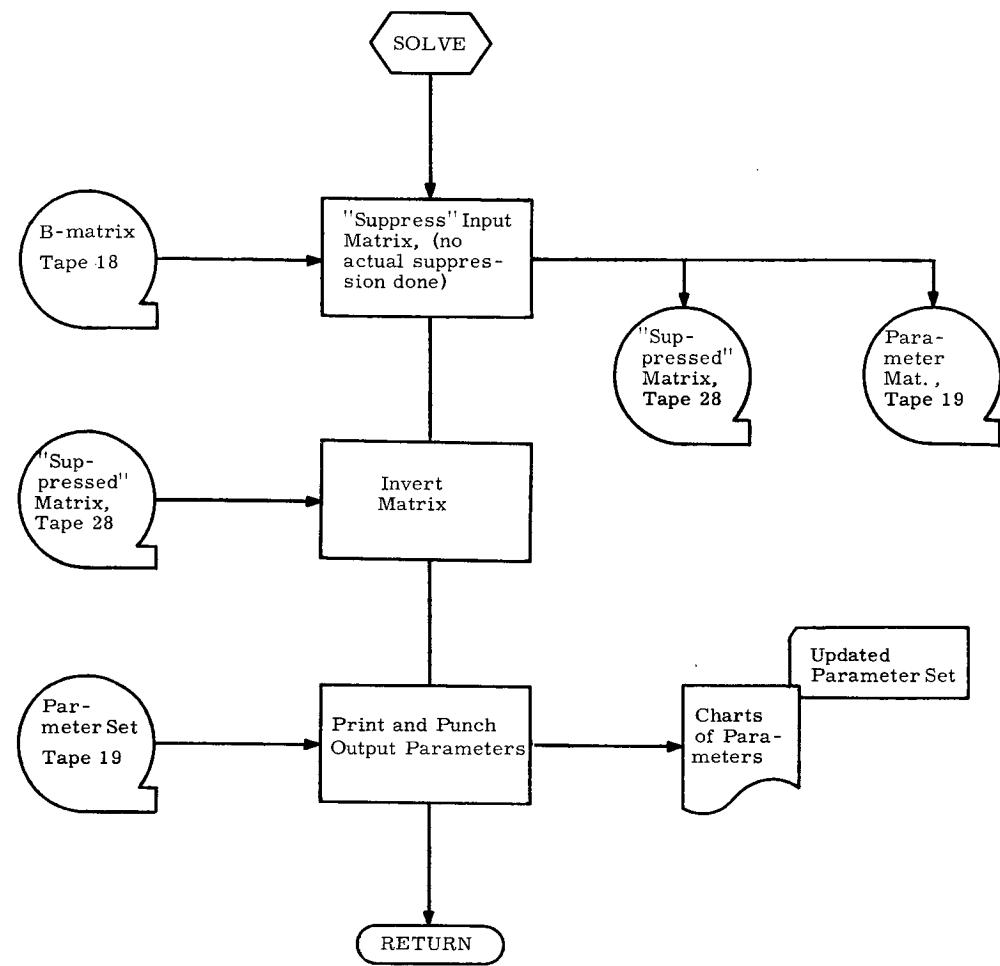
B-matrices from different arcs are combined and inverted to yield parameter corrections. At this point, parameter corrections may be suppressed or eliminated and any desired selection of parameters may be used in the solution. SOLVE offers complete flexibility in the **selection of arcs used in the solution and in the parameters whose corrections are obtained from the solution.**

The solution is now used as a correction set to update the parameters. If necessary, the new parameter set can be used as a starting-point for a second run through the entire program. This will be necessary when the parameter corrections are large enough to violate the assumed linearity of the model.

**SECTION II**  
**SYSTEM FLOW CHART**

FLOW OF NORMAL SOLVE RUN





SECTION III  
USER INFORMATION

## INPUT CARDS

### 1) Card Type One, Header Card

cc 1-72      Alpha-numeric data to be printed at the top of each page of output. This card must be present.

### 2) Card Type Two, Options Card

cc 5      Integer 0, 1 or 2, as follows:

0 - Input Format Check on Tape and  
Card Input

1 - Input Format Check on Card Input  
Only

2 - No Input Format Check

cc 10      Integer 0 or 1, as follows:

0 - Indicates a normal SOLVE run

1 - Indicates an invert only SOLVE run

cc 15      Integer 0 or 1, as follows:

0 - The edit tape will be printed in a  
later job.

1 - The edit tape will be printed in this job.  
This card must be present.

### 3) Card Type Three, Edit Card

cc 5      Edit code for the input B<sub>1</sub> matrices

cc 10      Edit code for the input parameter set matrices

cc 15      Edit code for the suppressed matrices

cc 20      Edit code for the reduced matrices

cc 25      Edit code for the back-substitution matrices

cc 30      Edit code for the combined matrix

cc 35      Edit code for the inverse matrix

The "Edit Codes" are integers, as follows:

- 1 - Unnormalized
- 2 - Normalized, diagonal elements one
- 3 - Inverse
- 4 - Identification Records Only
- 5 - Normalized Inverse with Standard Deviations

(Note: For more detail on edit formats, see the subroutine write-up for EDIT)

This card must be present.

4) Card Type Four, Combined Matrix Data

- cc 1 - 5 Positive integer less than or equal to 99999 or zero; the matrix identification number for the combined matrix.
  - cc 9 - 20 Alpha-numeric data--the name of the combined matrix.
  - cc 24 - 25 The number of parameters to be suppressed in the combined matrix. Zero or a positive integer less than 51.
- This card must be present in a normal SOLVE run.

5) Card Type Five, Combined Matrix Suppression List

- cc 1 - 70 The labels or code labels of parameters to be suppressed in the combined matrix, if there are any. These are integers, right adjusted in five-column fields. The list may extend over one or more cards, but there should be no blank fields embedded in the list. The parameter labels need not be in sort. The various code labels are described in the section on Parameter Labels, page 3.7. This card must be present in a normal SOLVE run where the number of parameters to be suppressed in the combined matrix is greater than zero.

6) Card Type Six, B Matrix Data

- cc 1 - 5 B matrix identification number, as follows:  
0 through 99998 indicates the matrices to be used in this SOLVE run.

99999 indicates that all B matrix cards have been read and is the last card of the data deck. The other fields in the 99999 card are blank.

- cc 9 - 20      New alpha-numeric name to be attached to the B matrix. If this is blank, the name of the B matrix will not be changed.
- cc 24-25      The number of parameters to be suppressed in the B matrix. Zero or a positive integer less than 51. This card must be present in a normal SOLVE run.

#### 7) Card Type Seven, B Matrix Suppression List

This card is exactly the same as Card Type Five, except it refers to the input B matrix, not the combined matrix.

## OPERATING INSTRUCTIONS

- 1) The system control cards required in the overall deck setup are:

```
$JOB  
$SETUP    04  
$SETUP    16      (omit if EDIT LATER option off)  
$EXECUTE  IBJOB  
$IBJOB
```

SOLVE decks, binary or source

```
$DATA  
      SOLVE data deck
```

- 2) The tape setup is:

<u>DCS Unit</u>	<u>Tape Function</u>
04	Input tape, produced by MERGE
05	Scratch tape, or disk file
06	Scratch tape, or disk file
14	Scratch tape, or disk file
15	Scratch tape, or disk file
16	Edit tape to be saved if the EDIT LATER option is on, otherwise it can be a disk file

- 3) Output consists of punched cards, printing and the EDIT LATER tape, if that option is on.

### EDIT LATER

EDIT LATER is simply a separate program which will print the edit tape from a SOLVE run. It consists of the routine EDIT, compiled as a main routine, and the subroutines EDIT calls. These subroutines are CHECK, ERROR and MINV. There is no card input to EDIT LATER.

OPERATING INSTRUCTIONS, EDIT LATER

- 1) The system control cards required in the overall deck setup are:

\$JOB	
\$SETUP	16
\$EXECUTE	IBJOB
\$IBJOB	

EDIT LATER DECKS, Binary or Source

- 2) The tape setup is:

<u>DCS Unit</u>	<u>Tape Function</u>
16	Edit Tape

- 3) Output consists of printing.

## PARAMETER LABELS

Parameter labels are used to identify the rows and columns of a matrix.

They are as follows:

- 1) Gravity parameter labels, five digit integers.

C mn	1	m xx	n xx	Where: n ≥ m m ≤ 5 m + n ≤ 10
S mn	2	xx	xx	

The gravity parameter labels are in strict numeric sequence.

- 2) Station parameter labels, four digit integers.

r p	1	Stat. No., p xxx	Where: xxx ≤ 998
φ p	2	xxx	
γ p	3	xxx	

The station parameter labels are in sequence according to station number as the major key, and first digit as the minor key.

- 3) Arc parameter labels, three digit integers.

Radiation Pressure	3	xx	xx = 01 to 03
Thrust	2	xy	xx = 1 or 2; and y = 1 to 3
Initial Conditions	1	xx	xx = 01 to 06
Orbital Elements	1	xx	xx = 07 to 12

The arc parameter labels are in sequence according to the first digit as major key, in descending order; and the last two digits as minor key, in ascending order.

- 4) Special parameters, treated as station parameters by SOLVE.

Earth-Moon Separation Multiplier	5	999	
Speed of light	6	999	

5) Code labels

Use the preceding parameters labels to indicate the parameters to be suppressed. To facilitate the suppression of groups of parameters, use the following code labels:

Gravity Parameters

3	m xx	n xx	$C_{lk}$ and $S_{lk}$ are suppressed for all $l, k \geq m, n$ respectively.
4	xx	xx	Both $C_{mn}$ and $S_{mn}$ are suppressed.

Station Parameters

4	Stat. No., p xxx	$\tau_p, \phi_p, \gamma_p$ are all suppressed.
---	---------------------	--

## PROGRAM RESTRICTIONS

The following are various restrictions on the size of the matrices and arrays processed by S $\backslash$ LVE:

1. The input matrix may not exceed order 100.
2. The matrix to be inverted may not exceed order 82.
3. The number of parameters to be eliminated from a given matrix may not exceed 60.
4. The number of parameters to be suppressed from the combined matrix, or from an input matrix, may not exceed 50.
5. There is no restriction on the number of input matrices which can be processed except that they must all appear on one tape.

## ERROR LIST

<u>Number</u>	<u>Routine</u>	<u>Meaning</u>
1	ELIM	A negative or zero pivot element found during elimination. The matrix is either ill-conditioned for elimination or not positive definite.
2	ELIM	Program error, dump core.
3	COMB	No match found between the combined matrix label record, formed by UPCOMB, and the label record of the new matrix to be combined.
5	BACKSB	No match found between the label record of the inverted matrix and the label record of the back-substitution matrix.
6	BEDIT	Edit requested of scratch tape.
7	MAIN	Matrix requested by input cards not found on tape 18 (input).
8	OPARC	Matrix called for in argument to OPARC not found on parameter tape, (tape 19).

The following errors refer to an input matrix or card.

10	INCK	Record type code word, IRTI, for the ID record is not of the form xxxx1.
11	INCK	Matrix identification number is 99999
12	INCK	The number of columns is greater than 101.
13	INCK	The number of rows plus one is not equal to the number of columns of a B matrix.
14	INCK	The number of observations is less than one for a B matrix.

15	INCK	The input square matrix is neither a B matrix nor a combined matrix.
16	INCK	The number of rows is not one in a parameter set matrix.
17	INCK	The type code word is not "8" for a parameter set matrix.
18	INCK	Record type code word, IRT2, for the label record is not of the form xxxx2.
19	INCK	Illegal parameter label, less than 100 or greater than 99999.
20	INCK	Illegal gravity parameter label, or gravity parameter labels out of sort.
22	INCK	Illegal station parameter label, or station parameter labels out of sort or some missing.
23	INCK	Illegal station parameter label with station number 999.
24	INCK	Illegal arc parameter label, or arc labels out of sort or a parameter missing.
28	INCK	Input tape does not consist of at least one B matrix and its parameter set matrix.
29	INCK	Illegal value on option card, run continues with option set to zero.
30	INCK	Illegal value on edit card, run continues with option set to one.

31	INCK	Illegal value for combined matrix identification number, i. e., negative or greater than 99999.
32	INCK	The number of parameters to be suppressed in the combined matrix is negative or greater than fifty.
33	INCK	One of the suppression lists contains an illegal parameter label, less than 100.
34	INCK	Illegal gravity parameter label in a suppression list.
35	INCK	Illegal station parameter label in a suppression list.
36	INCK	Illegal arc parameter label in a suppression list.
37	INCK	Illegal value for input B matrix identification number, negative or greater than 99999.
38	INCK	The number of parameters to be suppressed in an input matrix is negative or greater than fifty.

## PROGRAM DECK ARRANGEMENT

The SOLVE decks do not have to be in any special order. They are currently set up in the following order:

```
. UN18.  
. UN19.  
. UN20.  
. UN28.  
. UN29.  
. UN30.  
MAIN  
BACKSB  
BEDIT  
CALTYP  
CHECK  
COMB  
EDIT  
ELIM  
ERROR  
INCK  
INVERT  
LBLSUP  
MATSUP  
MINV  
OPARC  
OPGRAV  
OPSTAT  
SUPRSS  
UPCOMB
```

## FILE BLOCK PROGRAM OPTIONS

1) Tape 18:

    Filename is "UNIT18"  
    Mode is "BIN"  
    Unit assignment is "A(1)"

2) Tape 19:

    Filename is "UNIT19"  
    Mode is "BIN"  
    Unit assignment is "A(2)"

3) Tape 20:

    Filename is "UNIT20"  
    Mode is "BIN"  
    Unit assignment is "A(3)"

4) Tape 28:

    Filename is "UNIT28"  
    Mode is "BIN"  
    Unit assignment is "B(1)"

5) Tape 29:

    Filename is "UNIT29"  
    Mode is "BIN"  
    Unit assignment is "B(2)"

6) Tape 30:

    Filename is "UNIT30"  
    Mode is "BIN"  
    Unit assignment is "B(3)"

## TAPE FORMATS

The main portion of SOLVE uses five tapes, identified in the code as 18, 19, 20, 28, and 29, all binary. There are three types of data which may appear on these tapes. They are (1) a square matrix, (2) a rectangular backsubstitution matrix, and (3) a parameter set matrix. The square matrix may be an original B, a suppressed, a reduced, a combined, or an inverse combined matrix. All of these matrices are in a standard format. The last record on each tape is a dummy matrix ID record (the first record of any matrix), with a negative record type.

The function of each tape is as follows:

Tape 18: Input tape to SOLVE, containing all B matrices and their associated parameter set matrices, written on tape in pairs.

Tape 19: Scratch tape, holds the parameter set matrices.

Tape 20: Scratch tape, holds the reduced matrices.

Tape 28: Scratch tape, holds the suppressed matrices, then the combined matrix.

Tape 29: Scratch tape, holds the backsubstitution matrices.

The other tape used by SOLVE is tape 30, the edit tape, also binary. The first record of this tape is a twelve word alpha-numeric page header for all printed output. The rest of the tape contains some mixture of complete matrices in standard formats and the identification records (the first two records) of various matrices. The only modification to the matrix records occurs in the ID record, word ITYPE, which is modified to indicate the type of edit desired, as well as the type of matrix. The last record of the tape is a dummy ID record, with a negative record type.

## STANDARD FORMAT, SQUARE MATRICES

### Matrix Identification (ID) Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT1	1	Integer	"10001"
IDMAT	1	Integer	Matrix Identification Number, 1 to 99998
NRROW	1	Integer	Number of matrix data rows
NCOL	1	Integer	Number of matrix data elements per row, including Right Hand Side element
V1	1 x 2	Double	Total Variance
V2	1 x 2	Double	Dummy Variance word
V3	1 x 2	Double	Arc Variance
NOB	1	Integer	Number of Observations
ITYPE	1	Integer	Code for matrix type, as follows: "1" B-matrix "3" Combined matrix "5" Reduced matrix "6" Inverse combined matrix "7" Suppressed matrix
BNAME	2	Alpha	Alpha-numeric name for matrix, for editing purposes only. It can be blanks.

### Matrix Label Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT2	1	Integer	"10002"
IDUM	1	Integer	Dummy parameter label
LABS	NCOL-1	Integer	Parameter labels

### Matrix Data Element Records, NROW Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT3	1	Integer	"10003"
RHS	1 x 2	Double	Right Hand Side element
DATA	(NCOL-1)x 2	Double	Matrix data elements, one matrix row

### End of Logical Tape Record, One Per Tape

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT	1	Integer	" - 19991"
IDUM	13	Integer	Dummy words to fill out record

## STANDARD FORMAT, PARAMETER SET MATRIX

Parameter Set Identification (ID) Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT1	1	Integer	"10011"
IDMAT	1	Integer	Matrix Identification Number (same as in matrix ID record for corresponding matrix)
NRDW	1	Integer	"1"
NCOL	1	Integer	Number of elements in parameter set
IDUM	7	Integer	Dummy words to fill record
ITYPE	1	Integer	"8"
BNAME	2	Alpha	Alpha-numeric name for parameter set, for editing only. It may be blanks.

Parameter Set Label Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT2	1	Integer	"10012"
LABS	NCOL	Integer	Parameter Labels

Parameter Set Data Element Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT3	1	Integer	"10013"
DATA	NCOL x 2	Double	Parameter Values

## BACKSUBSTITUTION MATRIX FORMAT

### Matrix Identification (ID) Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT1	1	Integer	"20001"
IDMAT	1	Integer	Matrix Identification Number, 1 to 99998
NRDW	1	Integer	Number of matrix data rows
NCOL	1	Integer	Number of matrix data elements per row, including Right Hand Side element and the Eliminated Parameter label
V1	1 x 2	Double	Total Variance
V2	1 x 2	Double	Dummy Variance
V3	1 x 2	Double	Arc Variance
NOB	1	Integer	Number of Observations
ITYPE	1	Integer	"2"
BNAME	2	Alpha	Alpha-numeric name for matrix, for editing purposes only. It may be blanks.

### Matrix Label Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT2	1	Integer	"20002"
IDUM	2	Integer	Dummy parameter label
LABS	NCOL-2	Integer	Parameter labels for matrix columns

### Matrix Data Element Records, NROW Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT3	1	Integer	"20003"
LAB	1	Integer	Parameter label for matrix row
IDUM	1	Integer	Dummy word for padding
RHS	1 x 2	Double	Right Hand Side element
DATA	(NCOL-2) x 2	Double	Matrix data elements, one matrix row

### End of Logical Tape Record, One Per Tape

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT	1	Integer	" - 29991"
IDUM	13	Integer	Dummy words for padding

## PERM COMMON DEFINITIONS

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
B	82 x 2	Double	Right hand side or solution vector for inversion
BNEW	60 x 2	Double	Solution vector from backsubstitution
SIGT $\emptyset$ N	1 x 2	Double	Signal to noise ratio
V1	1 x 2	Double	Total variance
V2	1 x 2	Double	Dummy variance words
V3	1 x 2	Double	Arc variance
V1C	1 x 2	Double	Combined matrix total variance
V2C	1 x 2	Double	Combined matrix dummy variance
V3C	1 x 2	Double	Combined matrix arc variance
IRT1	1	Integer	Record type one (ID)
IDMAT	1	Integer	Matrix identification number
NR $\emptyset$ W	1	Integer	Number of rows in matrix
NC $\emptyset$ L	1	Integer	Number of columns in matrix
N $\emptyset$ B	1	Integer	Number of observations
ITYPE	1	Integer	Matrix type
BNAME	2	Alpha	Matrix alpha-numeric name
IRT2	1	Integer	Record type two (label)
LABS	101	Integer	Parameter labels record
LABSI	82	Integer	Labels of inverted matrix
NR $\emptyset$ WI	1	Integer	Number of rows in inverted matrix
LABSN	60	Integer	Labels of parameters solved for by backsubstitution
NR $\emptyset$ WN	1	Integer	Number of elements in LABSN
NGRAV	1	Integer	Number of gravity parameters
NSTAT	1	Integer	Number of station parameters
NARC	1	Integer	Number of arc parameters
JPAGE	1	Integer	Printed output page number

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
LINE	1	Integer	Printed output line number
NØREC	1	Integer	Number of backspaces necessary to position tape at 10001 record
NØREC2	1	Integer	Number of backspaces necessary to position tape at 10001 record
ØBVS	1	Real	Total number of observations
ALPHA	12	Alpha	Page header for printed output
IDCØMB	1	Integer	Matrix identification number for combined matrix
NRØWC	1	Integer	Number of rows in combined matrix
NCØLC	1	Integer	Number of columns in combined matrix
NØBC	1	Integer	Number of observations in combined matrix
ITYPEC	1	Integer	"3"
BNAMEC	2	Alpha	Combined matrix alpha name
LABSC	101	Integer	Parameter label record of combined matrix

## INPUT COMMON DEFINITIONS

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IOPT1	1	Integer	Input check option switch
IOPT2	1	Integer	Program path option switch
IOPT3	1	Integer	Edit Now or Later option switch
MEORG	1	Integer	Edit original code
MEPAR	1	Integer	Edit parameter set code
MESUP	1	Integer	Edit suppressed code
MERED	1	Integer	Edit reduced code
MEDIC	1	Integer	Edit backsubstitution code
MECOM	1	Integer	Edit combined code
MEINV	1	Integer	Edit inverse code
NCMSUP	1	Integer	Number of parameters to be suppressed in combined matrix
JCMSUP	50	Integer	Parameters to be suppressed in combined matrix
IDIN	1	Integer	Matrix identification number of input matrix
BNAME	2	Alpha	Alpha name of input matrix
NBSUP	1	Integer	Number of parameters to be suppressed in input matrix
JBSUP	50	Integer	Parameters to be suppressed in input matrix
NARG	1	Integer	Argument for calling SUPRSS
BLKS	1	Alpha	Alpha blanks
LARC	21	Integer	Legal arc parameter labels, in proper sort
LGRAV	58	Integer	Legal gravity parameter labels, in proper sort
TDAT	6	Alpha	Data for printing arc parameter chart

SECTION IV  
SUBROUTINE WRITE-UPS

NAME	MAIN	
PURPOSE	Main control program for SØLVE	
CALLS	BACKSB	Solves the backsubstitution equations
	BEDIT	Writes a matrix to be edited onto tape 30
	CALTYP	Calculates the number of gravity, station and arc parameter labels in an array
	CHECK	Controls page feeding and header on printed output
	CØMB	Performs the matrix combination
	EDIT	Edits all matrices on tape 30 to ØU1
	ELIM	Eliminates parameters from the input matrix
	ERRØR	Handles error exits from SØLVE
	INCK	Checks card and tape input for errors
	INVERT	Control program for matrix inversion
	ØPARC	Print and punch arc parameter output
	ØPGRAV	Print and punch gravity parameter output
	ØPSTAT	Print and punch station parameter output
	SUPRSS	Control program for matrix suppression
OPTIONS	SØLVE	Options are described under Input Cards, page 3.1.
INPUT	Tape 18, the B matrix and parameter set matrix tape. The input cards described on page 3.1.	
OUTPUT	<ol style="list-style-type: none"> <li>1) Four signal to noise ratios</li> <li>2) Charts of the original parameter values, the changes and the updated parameter values for the gravity, station and arc parameters</li> </ol>	

- 3) Punched cards containing the updated gravity, station and orbital elements parameter set
- 4) Any desired editing, either on a tape to be printed later or printed

TAPES      Six tapes are used, and all are rewound at the beginning and end of the run

18 Input tape

19, 20, 28, 29 Scratch tapes

30 Edit tape

ERROR CHECKS      Error number seven is produced if a matrix indicated on an input card cannot be found on tape 18

NOTE      No cards are punched for the two special parameters, speed of light and earth-moon separation multiplier.

NAME	BACKSB	
PURPOSE	Solves the backsubstitution equations	
METHOD	The backsubstitution equations are rectangular matrices ( $D^{-1}C$ ) generated during the elimination process, along with their right hand side vector ( $D^{-1}\underline{b}_2$ ). The solution vector ( $\Delta p_2$ ) is formed as follows, where $\Delta p_1$ is the vector consisting of the solution set for the portion of the matrix not eliminated:	
	$\Delta p_2 = D^{-1}\underline{b}_2 - D^{-1}C\Delta p_1$	
CALLED BY	MAIN	Main control program for SØLVE
CALLS	ERRØR	Handles error exits from SØLVE
INPUT	B	The known delta-p set; i. e., $\Delta p_1$
	LABSI	The parameter labels for B
	NRØWI	The number of entries in B
	PERM	Common area PERM contains the ID and label records of the $D^{-1}C$ matrix
OUTPUT	BNEW	The new delta-p set; i. e., $\Delta p_2$
	LABSN	The parameter labels for BNEW
	NRØWN	The number of entries in BNEW
TAPES	USED	29 Input, backsubstitution matrix
	START	29 At the first 10003 record
	END	29 After the last 10003 record
ERROR CHECKS	Error number 5 indicates a program or system failure	
NOTES	Before the backsubstitution is performed, the parameter labels in LABSI and those in LABS (backsubstitution matrix label record) are compared. If a parameter appears in the backsubstitution matrix and not in the delta-p set, it is suppressed in the matrix. If a parameter appears in the delta-p set and not in the backsubstitution matrix, it is suppressed in the delta-p vector.	

NAME	BEDIT (NØREC, NØTAP, ITYP)		
PURPOSE	Writes a matrix to be edited onto tape 30		
CALLED BY	MAIN	Overall control program for SØLVE	
CALLS	ERRØR	Handles error exits from SØLVE	
INPUT	NØREC	The number of times a tape must be back-spaced to position it at the X0001 (ID) record	
	NØTAP	The logical tape number of the input matrix	
	ITYP	An integer indicating the desired format for the edited matrix. This is read from input card type three, the edit card.	
OUTPUT	The matrix, with ITYPE modified, written in standard format on tape 30		
TAPES	USED	30	Output, edit tape
		NØTAP	Input, holds the matrix to be edited
	START	30	Before the old -49991 record
		NØTAP	NØREC records past the ID, (X0001) record of the input matrix
	END	30	Before the new -49991 record
		NØTAP	After the last 10003 record
ERROR CHECKS	Error number 6 indicates that NØTAP is not 18, 20, 28 or 29		
NOTES	The code word ITYPE, used by the EDIT program to determine the type of matrix and the edit format, is computed as follows:  $\text{ITYPE} = 100 * \text{ITYP} + \text{ITYPE},$ where the old ITYPE is as it appears in the standard matrix.		

NAME	CALTYP (LABA, NP)	
PURPOSE	Calculates the number of gravity, station and arc parameter labels in array LABA	
CALLED BY	SUPRSS MAIN UPCQMB INCK OPARC OPSTAT	Control program for matrix suppression Overall control program for SOLVE Updates the combined matrix identification and label records Checks formats and values of input Prints and punches arc output Prints and punches station output
INPUT	LABA NP	Array of parameter labels Number of entries in LABA
OUTPUT	NGRAV NSTAT NARC	Number of gravity labels in LABA Number of station labels in LABA Number of arc labels in LABA
NOTES	NGRAV, NSTAT and NARC all appear in common PERM.	

NAME	CHECK (NØLIN)	
PURPOSE	Controls the page feeding and writes the page header for printed output	
CALLED BY	MAIN MINV INCK ØPARC ØPGRAV ØPSTAT	Overall control program for SØLVE Matrix inversion routine Checks input format and values Prints and punches arc parameter output Prints and punches gravity parameter output Prints and punches station parameter output
INPUT	NØLIN LINE ALPHA JPAGE	The number of lines to be printed The number of lines which appear on the current page A twelve-word array consisting of the page header The current page number
OUTPUT	LINE is incremented. If the new LINE is greater than forty-five, a new page is started and JPAGE is incremented.	

NAME	C $\emptyset$ MB	
PURPOSE	Performs the matrix combination	
METHOD	<p>"Combination" is basically a matrix addition, with right hand side elements also added. However, the matrices to be added are not necessarily the same size, nor do they necessarily represent the same parameter set.</p> <p>Therefore, the addition is performed on corresponding matrix elements; that is, elements with the same row and column parameter labels. Thus the combined matrix will represent a parameter set consisting of all parameters appearing in the input matrices.</p>	
CALLED BY	MAIN	Overall control program for S $\emptyset$ LVE
CALLS	ERR $\emptyset$ R	Processes error exits from S $\emptyset$ LVE
INPUT	The combined matrix ID and label records in common area PERM	
OUTPUT	The combined matrix	
TAPES	USED	20 Input, matrices to be combined 28 Output, the combined matrix
	START	20 and 28 are rewound
	END	20 After the new -19991 record 28 Before the new -19991 record
ERROR CHECKS	Error number 3 occurs if a label match cannot be found between an input matrix and the combined matrix label	
NOTES	The parameters represented in the matrices to be combined must be from the same original parameter set, or the delta-p's are meaningless. Therefore, in a normal S $\emptyset$ LVE run, the arc parameters are eliminated before combination and only matrices representing the same gravity and station sets should be combined.	

NAME	EDIT	
PURPOSE	This routine "prints" (i. e., writes on the systems output tape) all matrices on tape 30, in a specified format.	
CALLED BY	MAIN	Overall control program for SOLVE. Edit can also be an independent program.
CALLS	MINV	Matrix inversion routine.
OPTIONS	ITYPE	<p>1XX Print matrix as is; i. e., unnormalized. The rectangular matrices (parameter set matrices and back-substitution matrices) may only be edited in the unnormalized format.</p> <p>2XX Print normalized matrix; i. e., the diagonal elements are set to one; the standard deviation vector is also printed.</p> <p>3XX Print the inverse of the input matrix, with the solution vector as the right hand side.</p> <p>4XX Print the Identification and Label records only; i. e., records X0001 and X0002.</p> <p>5XX Print the normalized inverse matrix. Also print the standard deviation vector; i. e., the square roots of the diagonal elements of the inverse matrix.</p>
INPUT	ITYPE	<p>A three-digit code word in the ID record of the record of the matrix, YXX, where:</p> <p>Y Specifies the edit format, as indicated on input card type three (see OPTIONS).</p> <p>XX Specifies the type of matrix.</p>

- XX = 1    B matrix  
           2    Backsubstitution matrix  
           3    Combined matrix  
           5    Reduced matrix  
           6    Inverse combined matrix  
           7    Suppressed matrix  
           8    Parameter set matrix

**OUTPUT**    The matrices in the described format on the systems output tape.

**TAPES**    USED        30    Input, edit tape  
                 START     30    Before the -49991 record  
                 END       30    Rewound

**NOTES:**    The normalization performed is such that if N is the normalized matrix and A the original matrix, the following is true:

$$N_{ij} = \frac{1}{\sqrt{a_{ii}}} \quad a_{ij} \frac{1}{\sqrt{a_{jj}}}$$

The right hand side vector is not changed and the vector  $\sqrt{a_{ii}}$  is printed after the matrix.

The edit types normalized, inverse and inverse normalized may only be used with matrices of order 82 or less.

NAME            ELIM (NUMB, CMBLBL)

PURPOSE        This routine eliminates parameters from the input matrix.

METHOD         A Gauss-Jordan elimination is performed on those parameters to be eliminated, which must be the last parameters in the matrix. A reduced matrix representing the remaining parameters is produced, along with a backsubstitution matrix for the eliminated parameters.

CALLED BY      MAIN        Overall control program for S<sub>O</sub>LVE

CALLS          UPC<sub>O</sub>MB    Develops combined matrix label record  
                   ERR<sub>O</sub>R    Handles error exits from S<sub>O</sub>LVE

OPTIONS        CMBLBL     If it is greater than zero, subroutine UPC<sub>O</sub>MB is called. If it is less than one, UPC<sub>O</sub>MB is not called.

INPUT          NUMB        The number of parameters to be eliminated from the matrix. The last (far right) NUMB parameters are eliminated.  
                   PERM       Common area PERM contains the matrix ID and Label records, as usual.

OUTPUT         A reduced matrix and a backsubstitution matrix, both on tape.

TAPES          USED        20      Output, reduced matrix  
                   28      Input, matrix to be eliminated  
                   29      Output, backsubstitution matrix  
                   START     20      Rewound, or before -19991 record  
                   28      At first 10003 record  
                   29      Rewound, or before -29991 record

END        20     Before new - 19991 record  
            28     After last 10003 record  
            29     Before new - 29991 record

**ERROR  
CHECKS**

Error number 1 indicates that a zero or negative pivot element was found during elimination. This means the matrix is either ill conditioned for elimination or is not positive definite.

Error number 2 indicates a program or system error during ELIM.

NAME           **ERROR (NERR)**

PURPOSE       Handles error exits from S<sub>O</sub>LVE

CALLED BY      MAIN        Main control routine for S<sub>O</sub>LVE  
                 BACKSB     Backsubstitution routine  
                 BEDIT      Writes matrices to the Edit tape  
                 C<sub>O</sub>MB      Matrix combination routine  
                 ELIM        Matrix elimination routine  
                 OPARC     Prints and punches arc parameter output  
                 INCK        Checks input format and values

INPUT           NERR       Error number  
                 PERM       The matrix ID and label records are in PERM  
                         common, as usual

OUTPUT          The following messages are printed:  
  
JOB TERMINATED DUE TO ERROR NUMBER XXXX.  
IDENT    NR<sub>O</sub>WS    NC<sub>O</sub>LS    BNAME    TYPE  
XXXXXX   XXXXXX    XXXXXX    Alpha    X

The "XXXXXX" are the appropriate numbers.

NAME INCK (M)

PURPOSE Checks the card and tape input to SØLVE for various errors

CALLED BY MAIN Main control program for SØLVE

CALLS CALTYP Calculates the number of gravity, station and arcs  
CHECK Controls the page feeding on printed output  
ERRØR Handles error exits from SØLVE

OPTIONS M Indicates the particular input to be checked:  
M = 0, check input tape  
M = 2, check Options Card, card type two  
M = 3, check Edit Card, card type three  
M = 4, check Combined Matrix Card, card type four  
M = 5, check Combined Matrix Suppression List, card type five  
M = 6, check B Matrix Card, card type six  
M = 7, check B Matrix Suppression List, card type seven

INPUT INPUT Common contains all quantities read from the input cards.  
Tape 18 is the input tape.

OUTPUT If an error is found which would cause SØLVE to function incorrectly, ERRØR is called and the job terminated. If a correctable error is found, a message is written, the item corrected, and the run continues.  
If no errors are found, no action is taken.

TAPES                  USED                  18                  Input if M = 0

START 18 Rewound

END 18 Rewound

**ERROR CHECKS** For a list of the error checks made by INCK and the action taken for non-fatal errors, please see Error Checks, page 3.10.

NAME            INVERT (IEDIT)

PURPOSE        Control routine for matrix inversion

CALLED BY      MAIN        Main control program for S $\emptyset$ LVE

CALLS           MINV        The subroutine which actually inverts a matrix

OPTIONS         IEDIT       If it is greater than zero, the inverse matrix is  
                                to be edited and is written on tape 30. If it is zero  
                                or negative, the matrix is not edited.

INPUT           SIGT $\emptyset$ N      Signal to noise ratio

                 PERM        Common contains the ID and Label records of the  
                                matrix to be inverted.

OUTPUT          Updated SIGT $\emptyset$ N  
  
                 Delta-p set, that is, the solution vector in array B in common  
                                area PERM, and the parameter labels for it in array LABSI.

TAPES           USED        28      Input, matrix to be inverted  
                              30      Output, edit tape

                 START       28      Before the first 10003 record  
                             30      Before the -49991 record

                 END         28      After the last 10003 record  
                             30      Before the new -49991 record.

NAME	LBLSUP (JSUALL, NSUALL)	
PURPOSE	Sets to zero the labels in array LABS corresponding to parameters to be suppressed	
CALLED BY	SUPRSS	Control program for suppression
INPUT	JSUALL	An array of up to 50 entries, consisting of parameter labels or code labels to be suppressed
	NSUALL	The number of entries in JSUALL
	LABS	Matrix label record
	NCOL	Number of entries plus one in LABS
	NGRAV	Number of gravity parameter labels
	NSTAT	Number of station parameter labels
OUTPUT	LABS	Matrix label record, with zeros inserted
NOTES	<ol style="list-style-type: none"><li>1. For an explanation of parameter code labels, see Parameter Labels, page 3.7.</li><li>2. If a parameter label to be suppressed does not appear in array LABS, no action is taken and the routine continues normally.</li></ol>	

NAME	MA TSUP	
PURPOSE	Deletes matrix rows and columns and writes the suppressed matrix data records on tape 28	
METHOD	The rows and columns corresponding to the various parameters to be suppressed are deleted. The remaining rows and columns, condensed to a square matrix, form the suppressed matrix.	
CALLED BY	SUPRSS	Control program for matrix suppression
INPUT	LABS	Parameter label record, with zeros substituted for the original label of the various parameters to be suppressed
	NCOL	The number of elements in an original matrix data row, including the right hand side
OUTPUT	The suppressed matrix data rows, written on tape 28	
TAPES	USED	18 Input, original B-matrix data rows 28 Output, suppressed matrix data rows
	START	18 Before first 10003 record 28 After the 10002 record
	END	18 After the last 10003 record 28 After the last 10003 record

NAME	MINV (N)	
PURPOSE	Inverts and solves a matrix	
METHOD	A Gauss-Jordan elimination, with a pivot search on the diagonal elements	
CALLED BY	INVR	Control program for matrix inversion
	EDIT	Edits matrices for printing
CALLS	CHECK	Controls page spacing of printed output
INPUT	N	Order of matrix, not to exceed 82
	A	Two-dimensional array containing the matrix to be inverted
	B	The Right Hand Side vector
OUTPUT	A	Inverted matrix
	B	The Solution vector
ERROR CHECKS	If a pivot element is found which is negative or zero, a message is printed indicating that the matrix is not positive definite and in which row the bad pivot occurred. However, the run continues.	

NAME	OPARC (VEC, LAB, NP, ID)	
PURPOSE	Print and punch arc parameter output	
CALLED BY	MAIN	Overall control program for SOLVE
CALLS	CALTYP	Calculates number of gravity, station or arc parameters
	CHECK	Controls page feeding on printed output
	ERROR	Error exit from SOLVE
INPUT	VEC	Delta-p set of arc parameters for this matrix
	LAB	Label set corresponding to VEC
	NP	The number of elements in VEC
	ID	Matrix identification number for the matrix whose arc parameters are being processed
	Tape 19 contains the parameter set matrix for matrix ID.	
OUTPUT	A chart of original parameter values, computed change, and the updated parameter values.	
	Punched cards containing the updated parameter set, to be used as input to the integration system.	
TAPES	USED	19 Input, parameter set matrices
	START	19 Positioned at any type 10011 record or at the -19991 record
	END	19 After the 10013 record
ERROR CHECKS	Error number eight indicates that the parameter set for matrix ID was not found on tape 19	
NOTES	If all arc parameters in a matrix are suppressed, no printed or punched output will be generated for that matrix.	

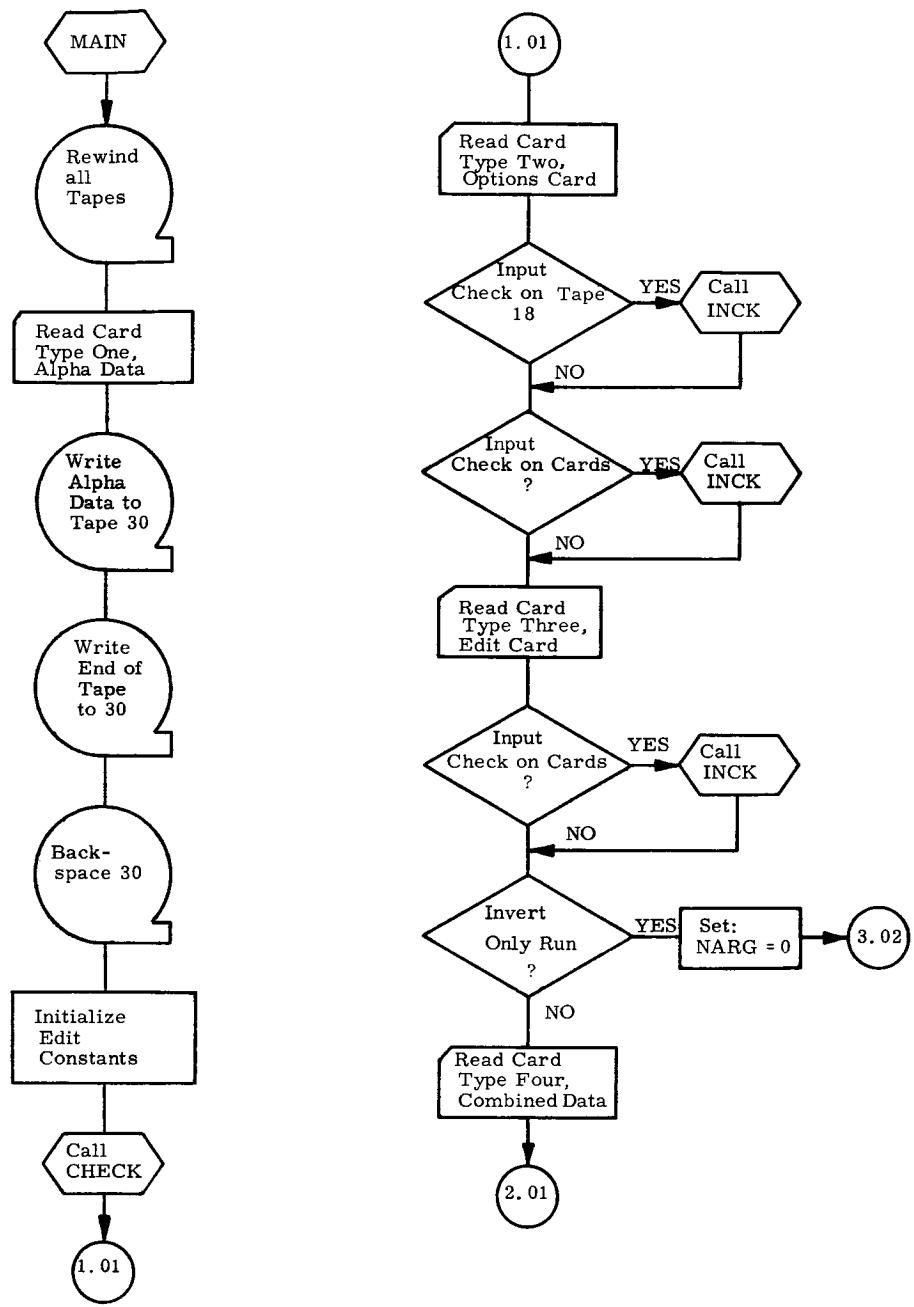
NAME	OPGRAV (VEC, LAB, NP)	
PURPOSE	Print and punch gravity parameter output	
CALLED BY	MAIN	Overall control program for S $\otimes$ LVE
CALLS	CHECK	Controls page feeding and header on printed output
INPUT	VEC	Delta-p set of gravity parameters for this run
	LAB	Label set corresponding to VEC
	NP	Number of entries in VEC
	Tape 19 contains the parameter set matrices	
OUTPUT	A chart of original parameter values, computed changes, and the updated parameter value	
	Punched cards containing the updated parameter set, to be used as input to the integration system.	
TAPES	USED	19 Input, parameter set matrices
	START	19 Not positioned
	END	19 After the 10013 record of the last parameter set matrix
NOTES	If all gravity parameters in this run have been suppressed, no printed or punched output will be generated for this run.	

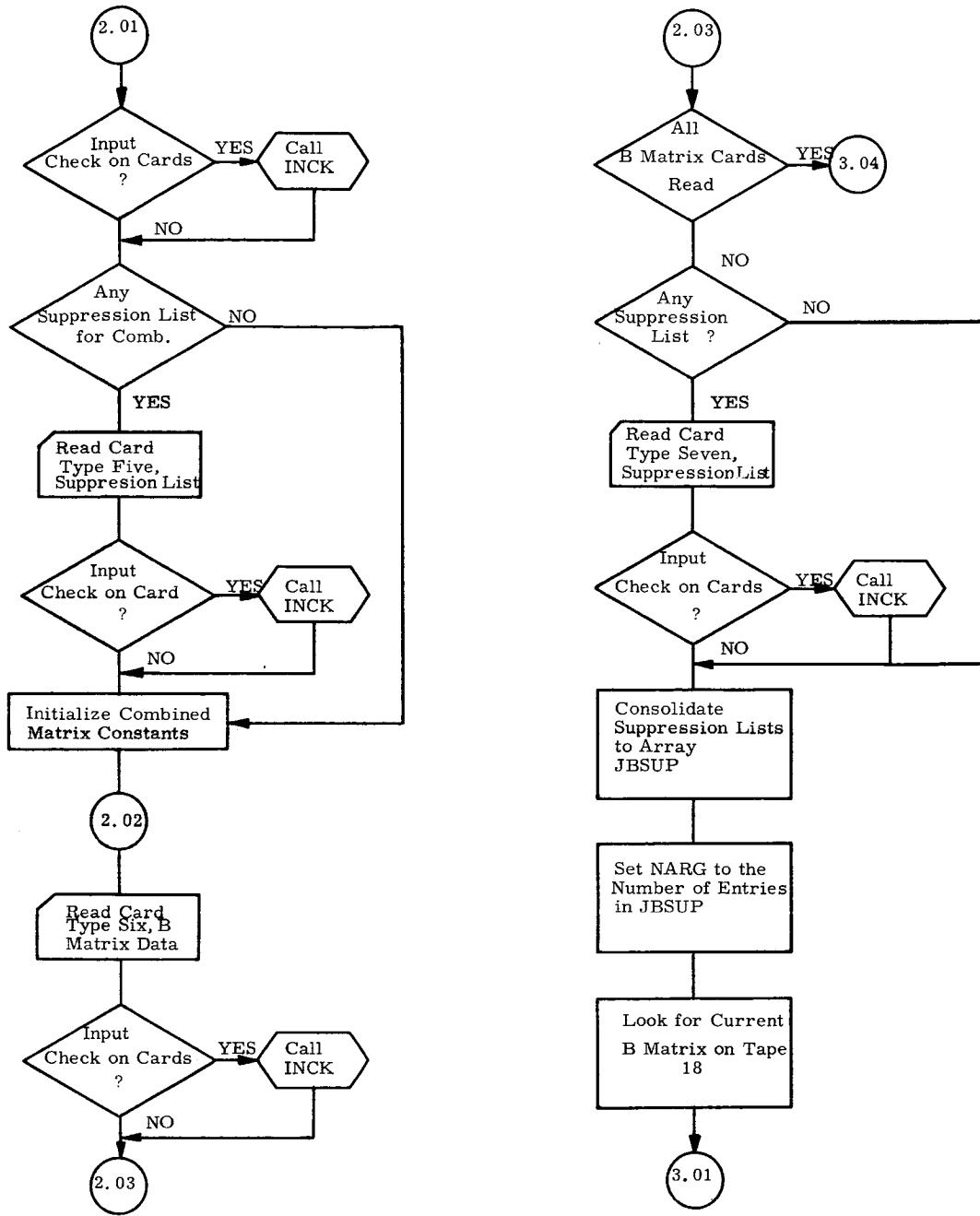
NAME	OPSTAT(VEC, LAB, NP)	
PURPOSE	Print and punch station parameter output	
CALLED BY	MAIN	Overall control program for S $\varnothing$ LVE
CALLS	CALTYP	Calculates the number of gravity, station and arc parameters
	CHECK	Controls page feed and header printing
INPUT	VEC	Delta-p set of station parameters for this run
	LAB	Label set corresponding to VEC
	NP	Number of entries in VEC
	Tape 19 contains the parameter set matrices	
OUTPUT	A chart of original parameter values, computed change, and the updated parameter values in spherical co-ordinates. Punched cards containing the updated parameter set, to be used as input to the Normal Equations system.	
TAPES	USED	19 Input, parameter set matrices
	START	19 Not positioned
	END	19 Before the -19991 record
NOTES	If all station parameters in the run have been suppressed, no printed or punched output will be generated for that run.	

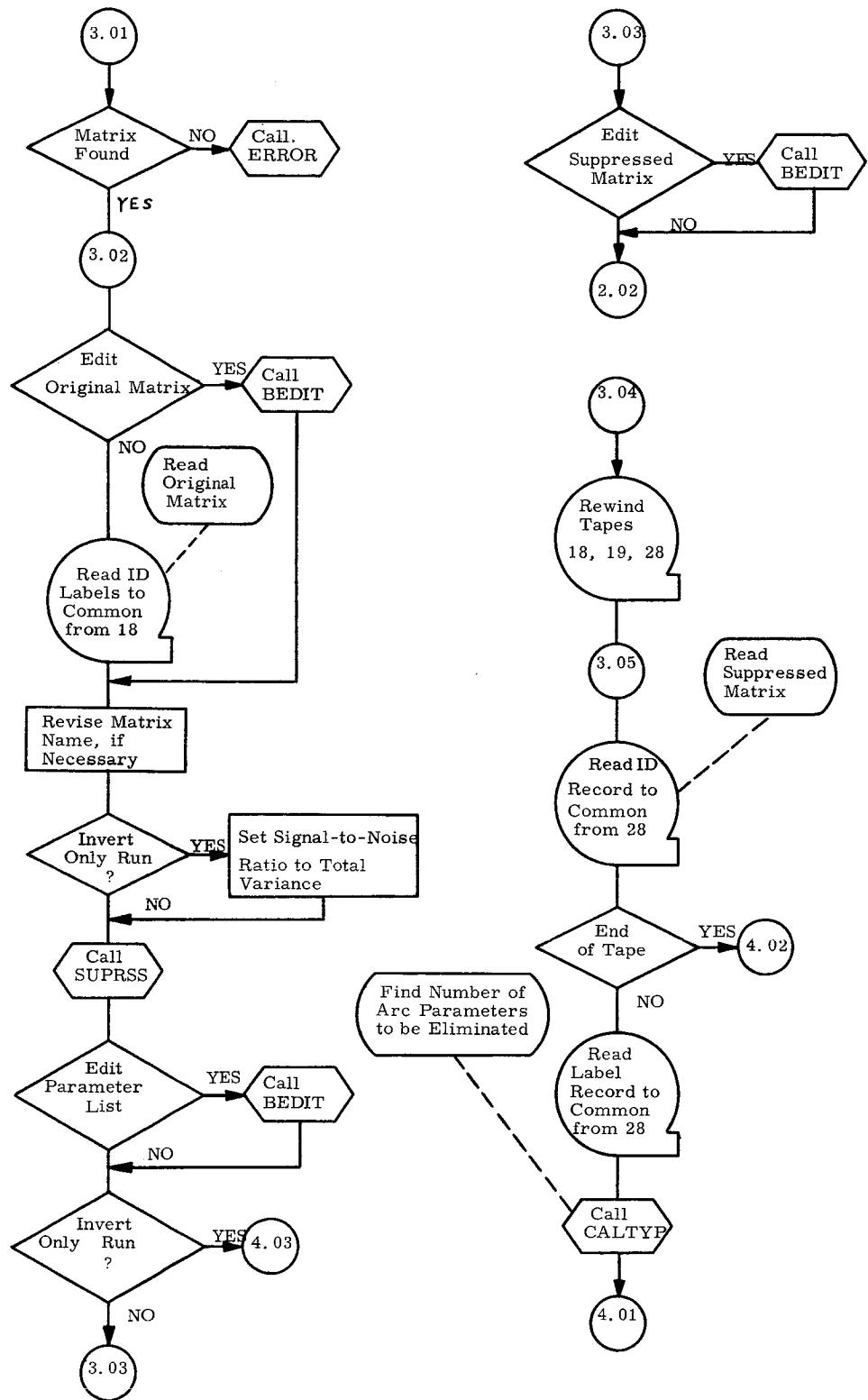
NAME	SUPRSS (JSUALL, NSUALL)		
PURPOSE	Control program for matrix suppression		
CALLED BY	MAIN	Overall control program for S\$OLVE	
CALLS	CALTYP	Calculates number of gravity, station and arc parameters in original matrix	
	LBLSUP	Sets to zero the labels in array LABS corresponding to parameters to be suppressed	
	MATSUP	Deletes matrix row and column of the parameters to be suppressed	
OPTIONS	NSUALL=0	No parameters to be suppressed for this matrix; the matrix is transferred from tape 18 to tape 28, with revised ITYPE	
INPUT	JSUALL	An array of up to 50 entries, consisting of parameter labels or code labels to be suppressed	
	NSUALL	The number of entries in JSUALL	
	PERM	Common area PERM contains the matrix identification and label record	
OUTPUT	<ol style="list-style-type: none"> <li>1. Suppressed matrix</li> <li>2. Parameter set matrix</li> </ol>		
TAPES	USED	18	Input, original B-matrix
		19	Temporary parameter set tape
		28	Output, suppressed matrix
	START	18	Before first 10003 record, input matrix
		19	Rewound, or before -39991 record
		28	Rewound, or before -19991 record
END	18	After last 10003 record, input matrix	
	19	Before new -39991 record	
	23	Before new -19991 record	

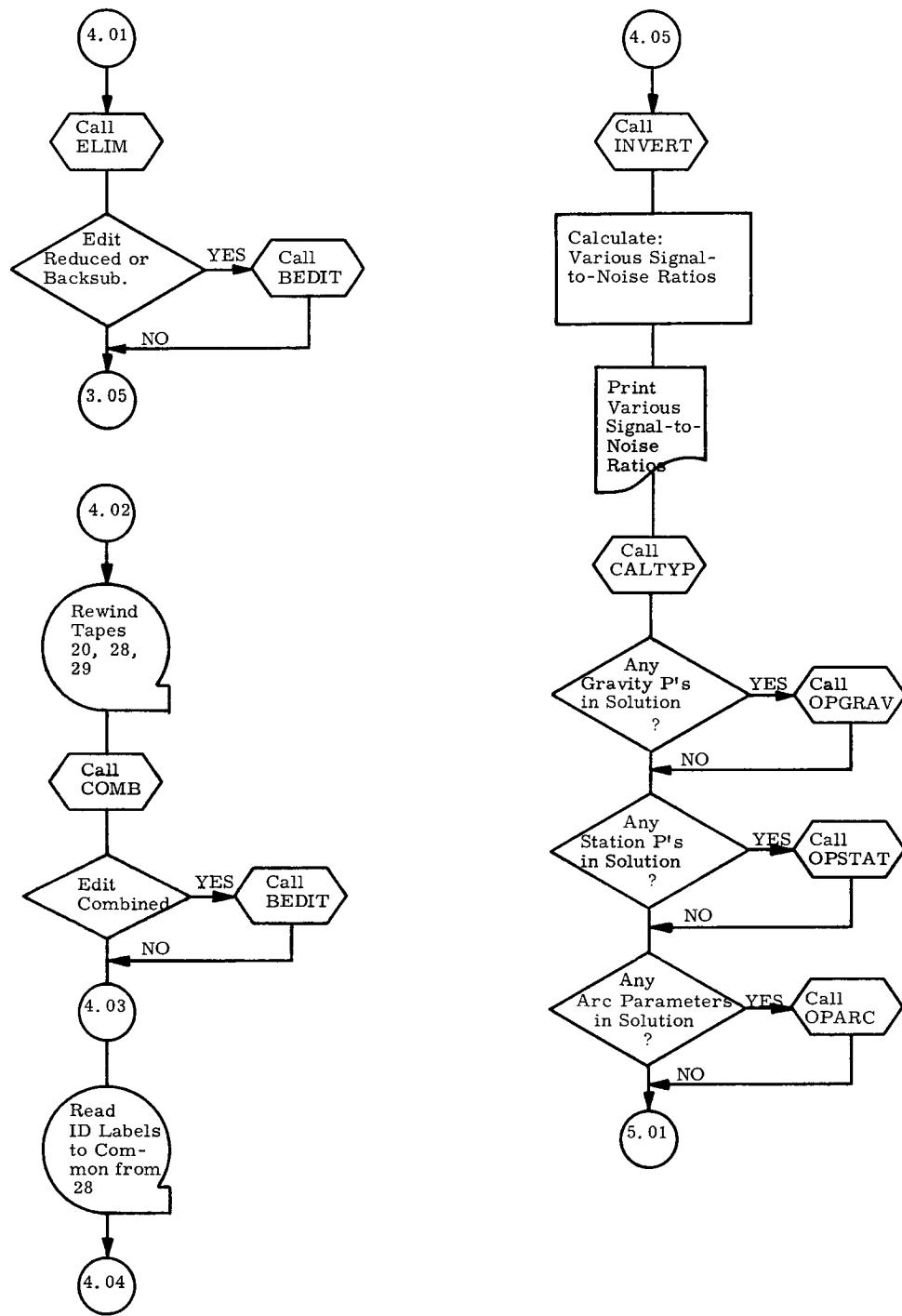
NAME	UPCØMB	
PURPOSE	Develops the combined matrix ID and label records, in common area PERM	
CALLED BY	ELIM	Elimination routine
CALLS	CALTYP	Calculates the number of gravity, station and arc parameters in a matrix
INPUT	SIGTØN	Current signal-to-noise ratio
	ID and label records to be used to update the combined ID and label records	
OUTPUT	Updated SIGTØN	
	Updated ID and label records for the combined matrix	
NOTES	UPCØMB should be called by the subroutine which generates the matrices to be combined. In a normal SØLVE run, this subroutine is ELIM.	

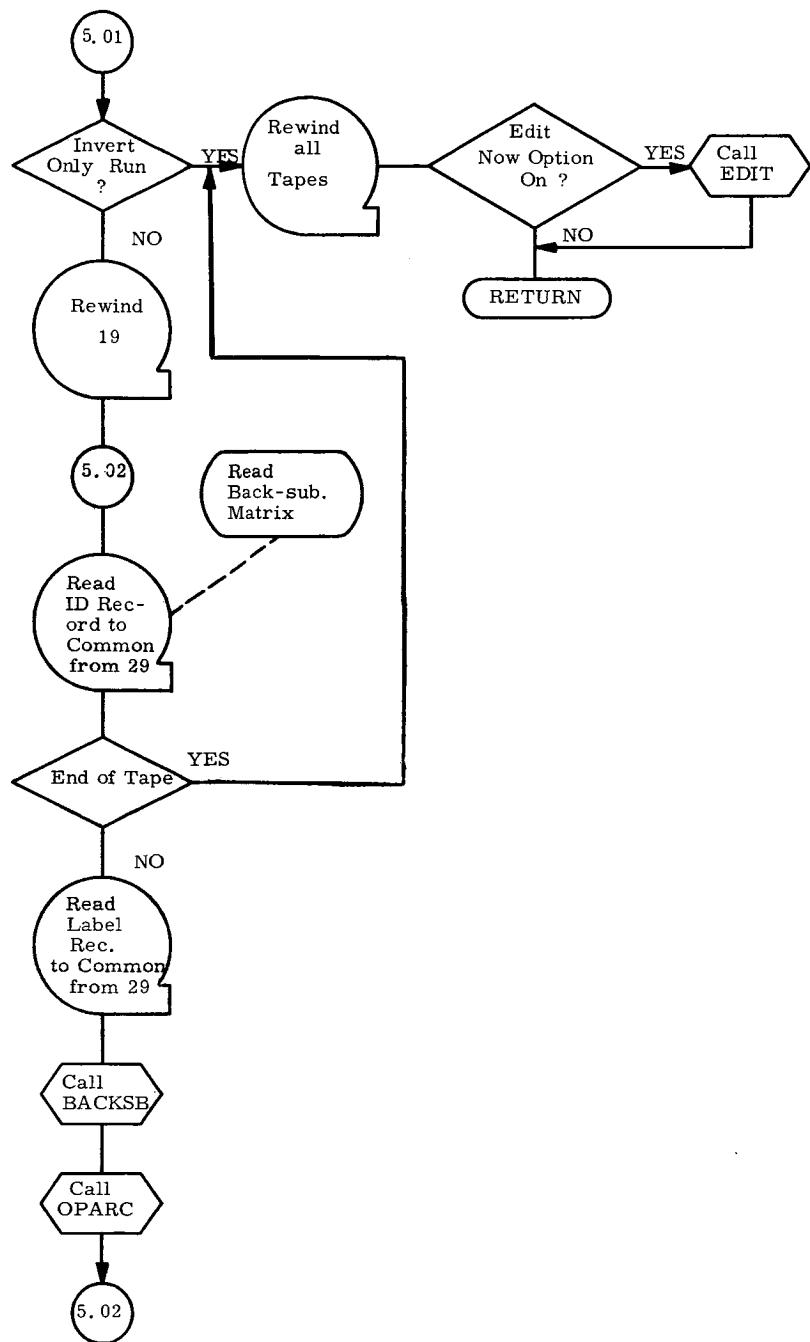
**SECTION V**  
**FLOW CHARTS**

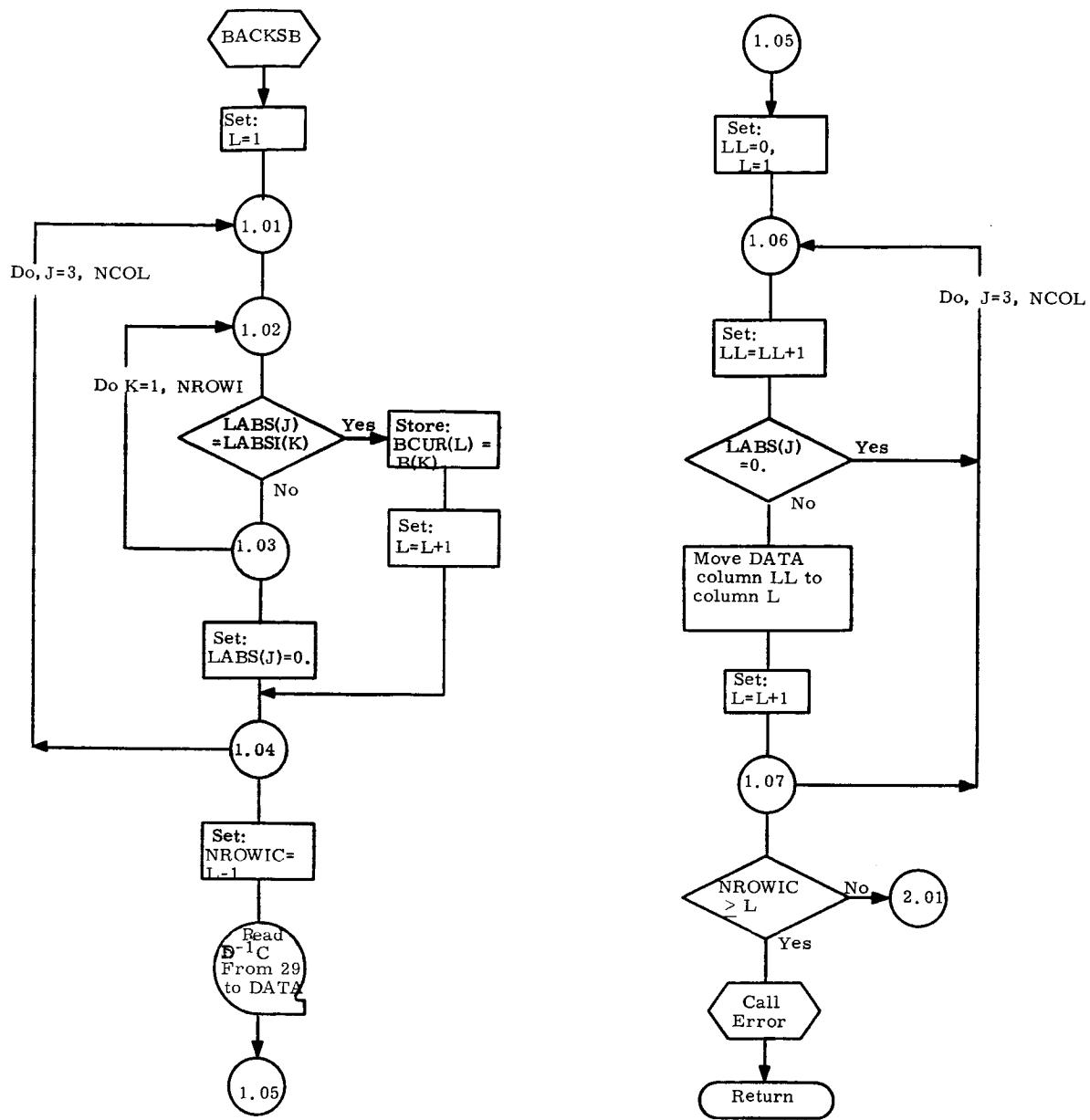


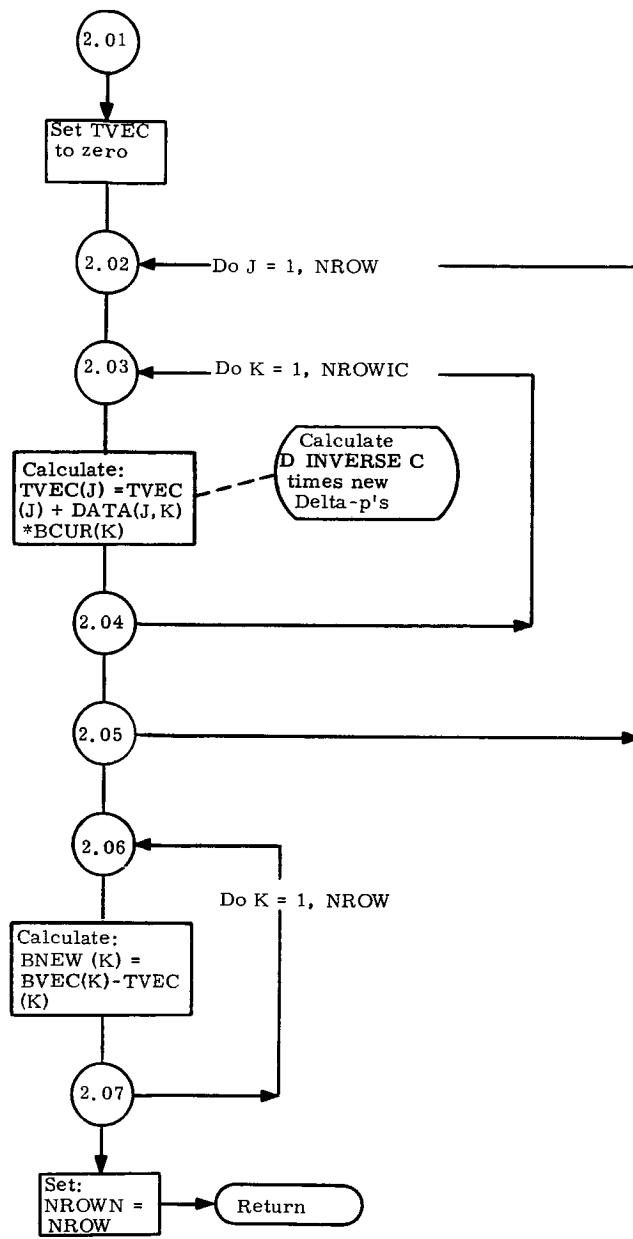


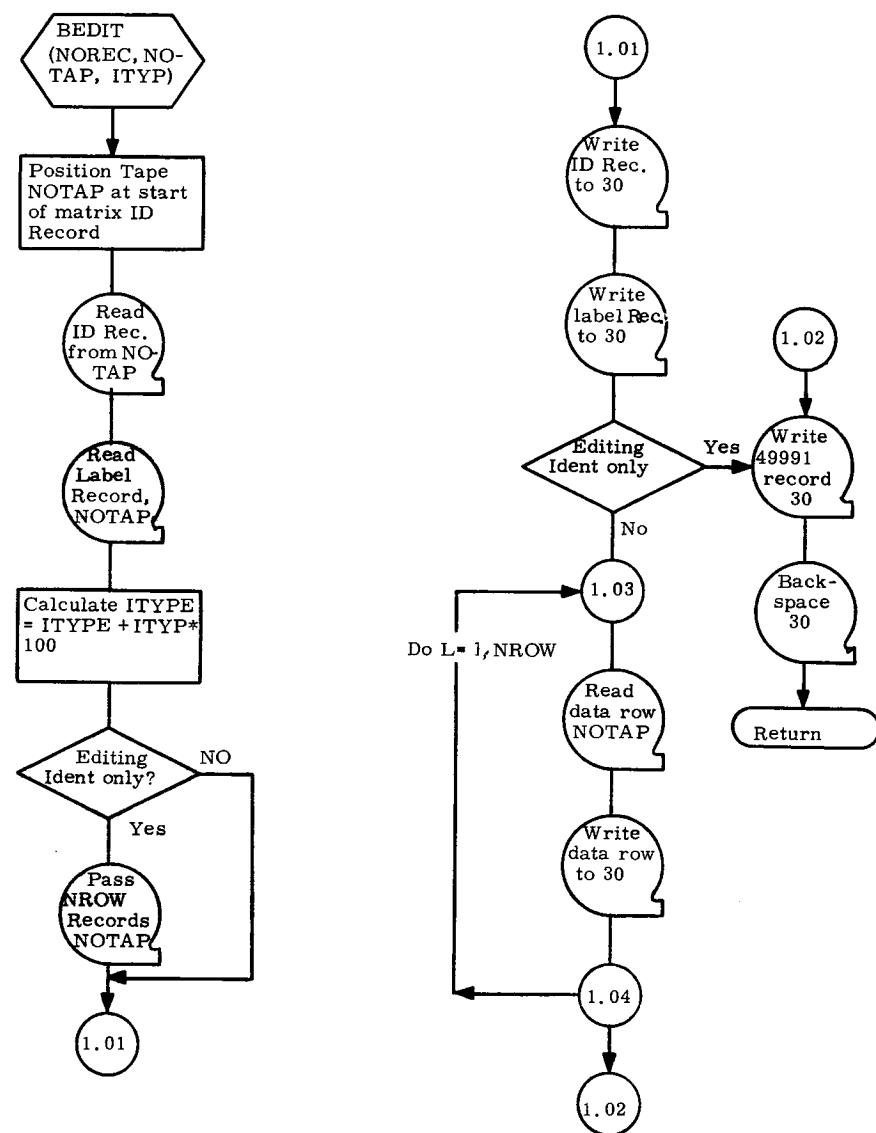


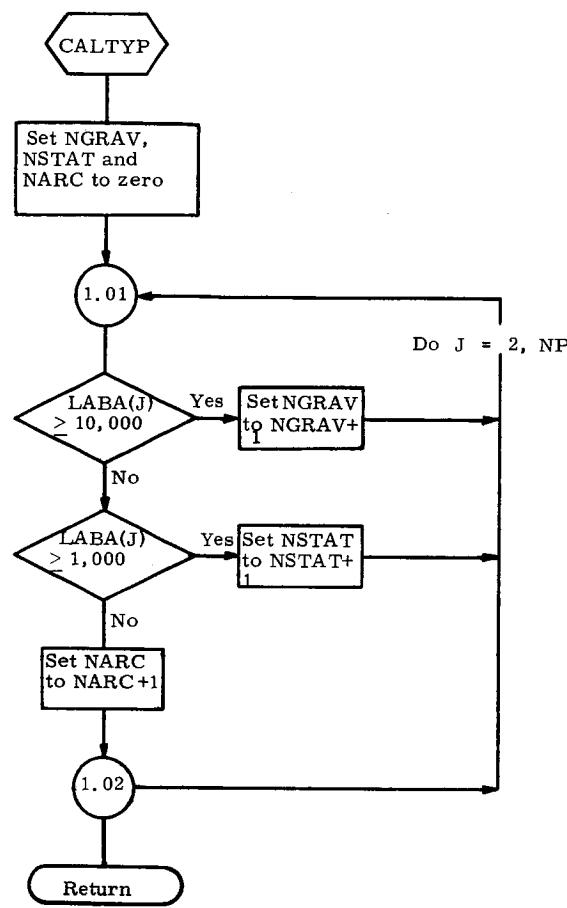


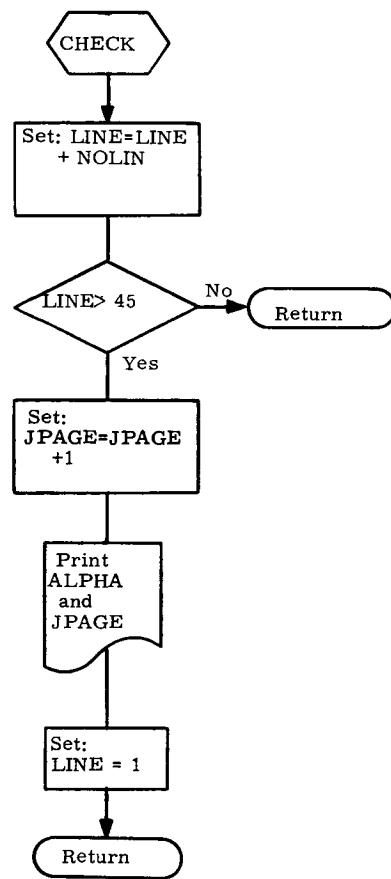


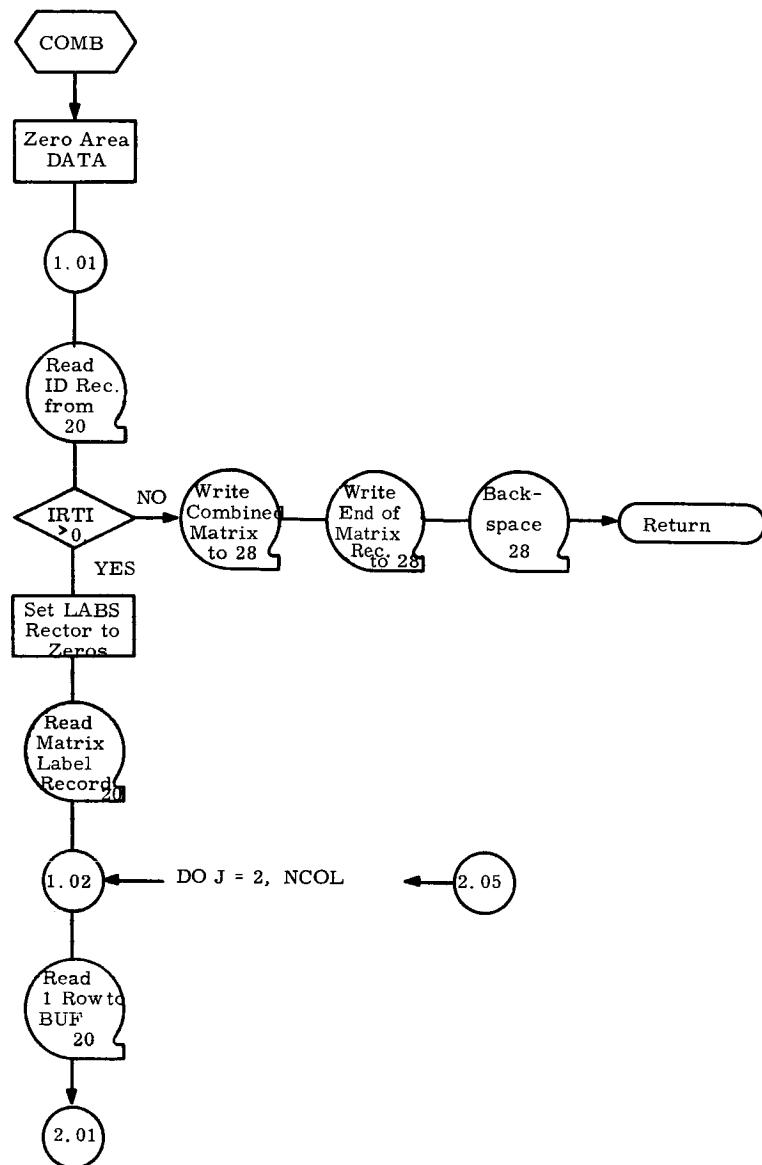


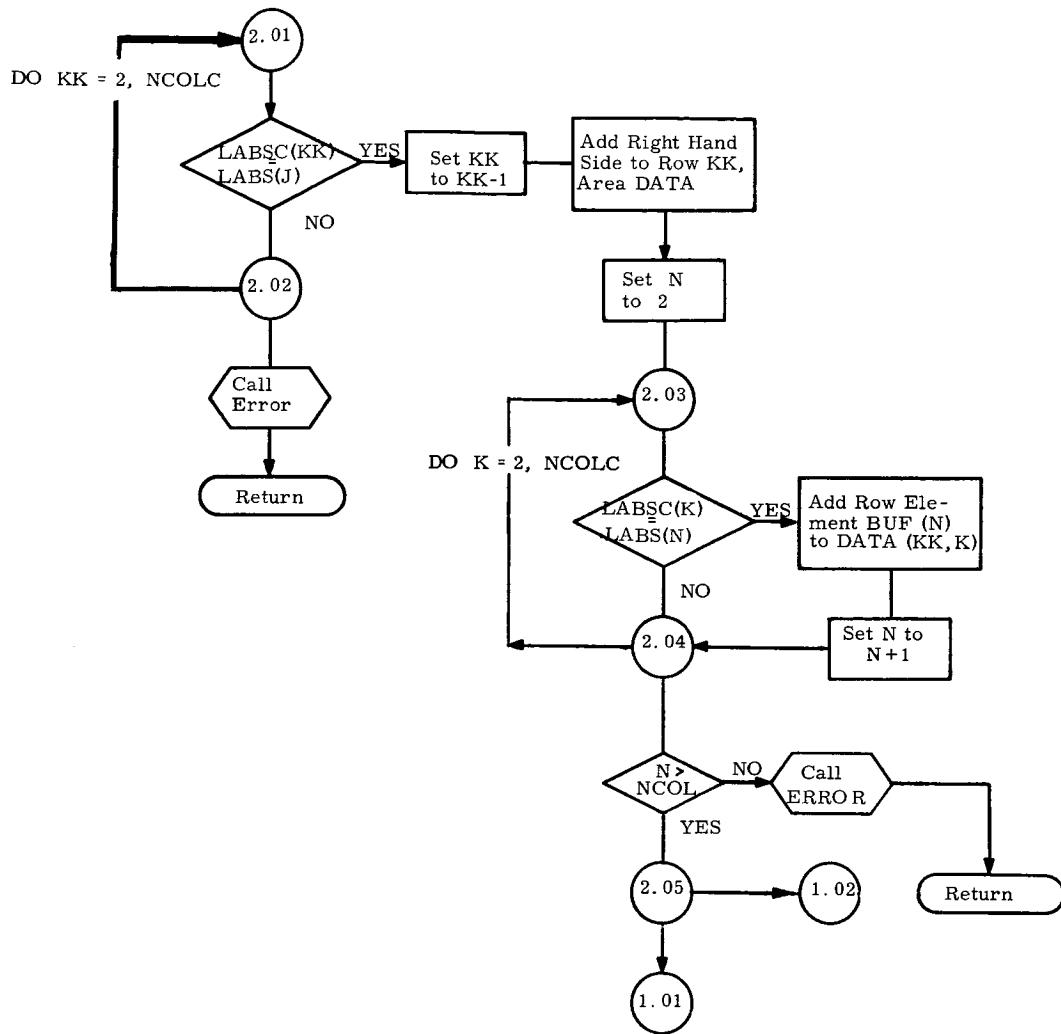


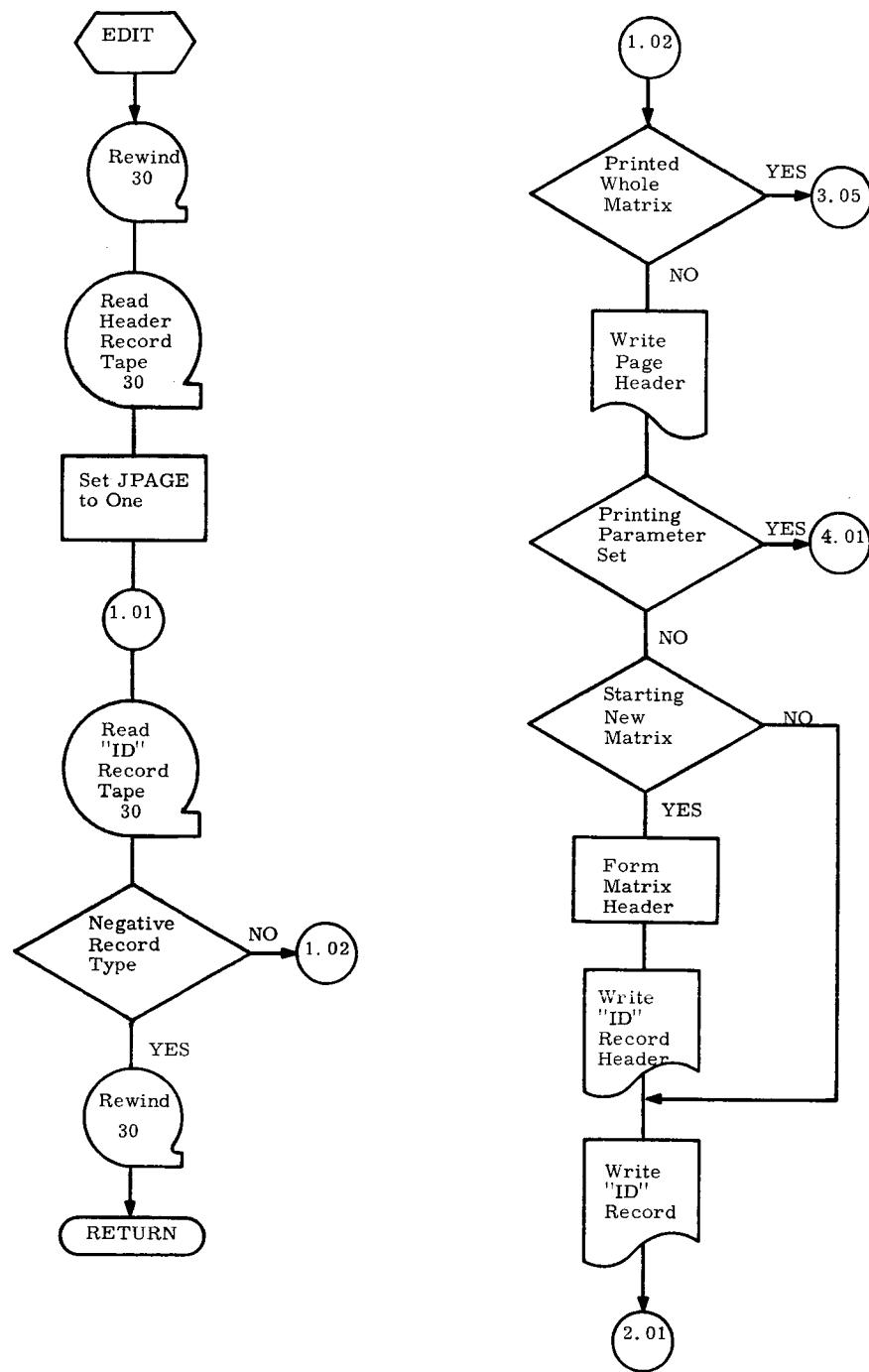


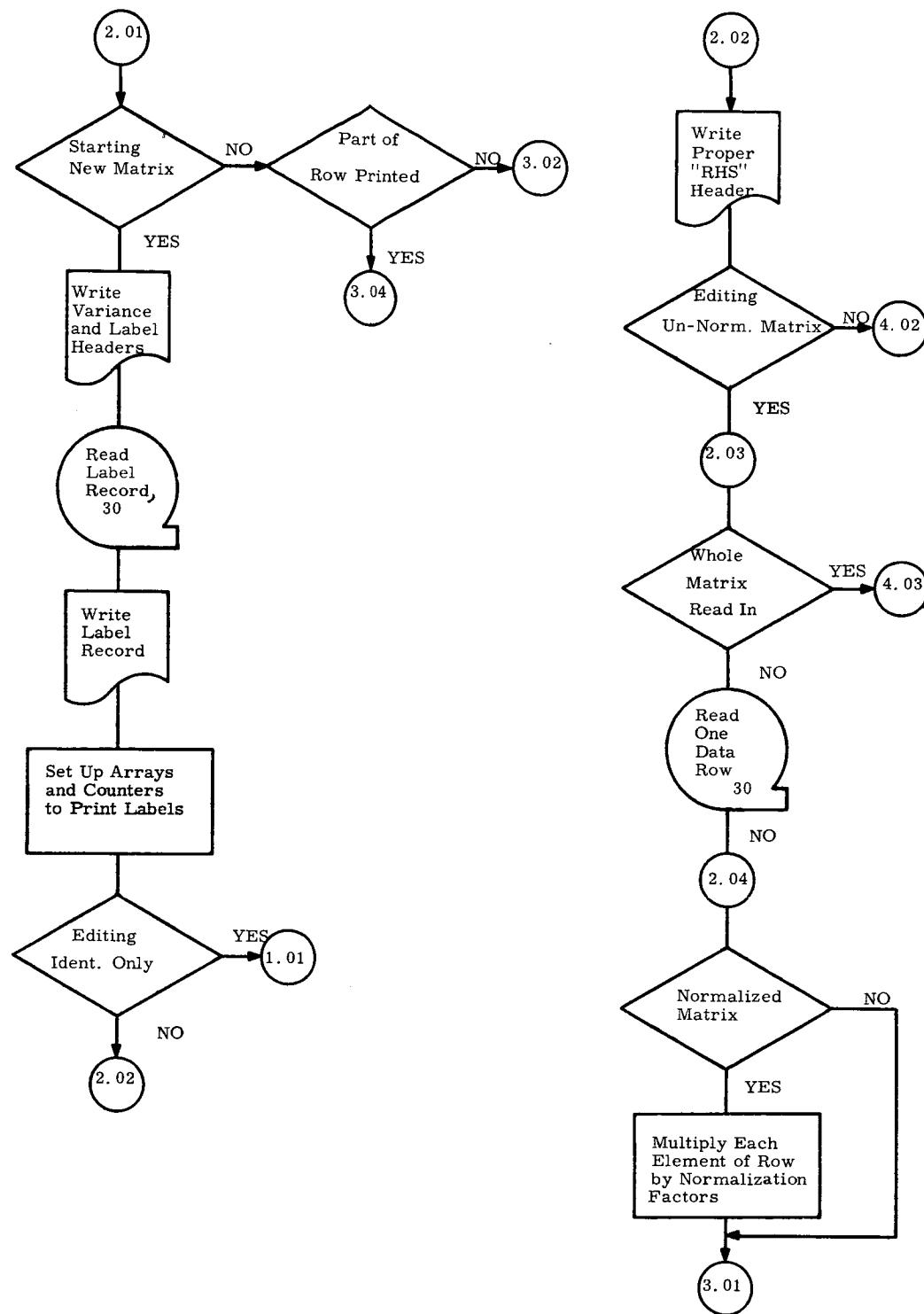


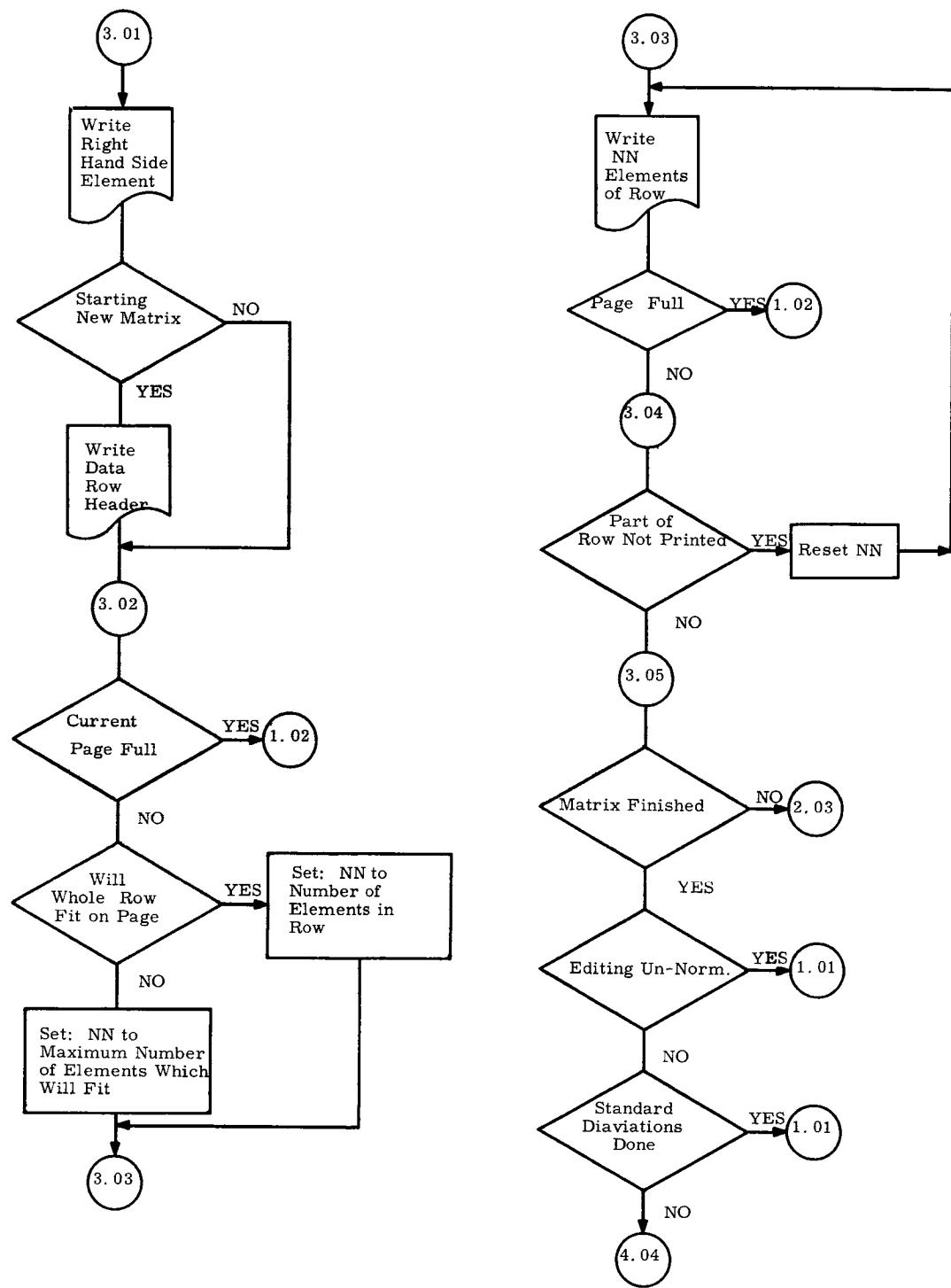


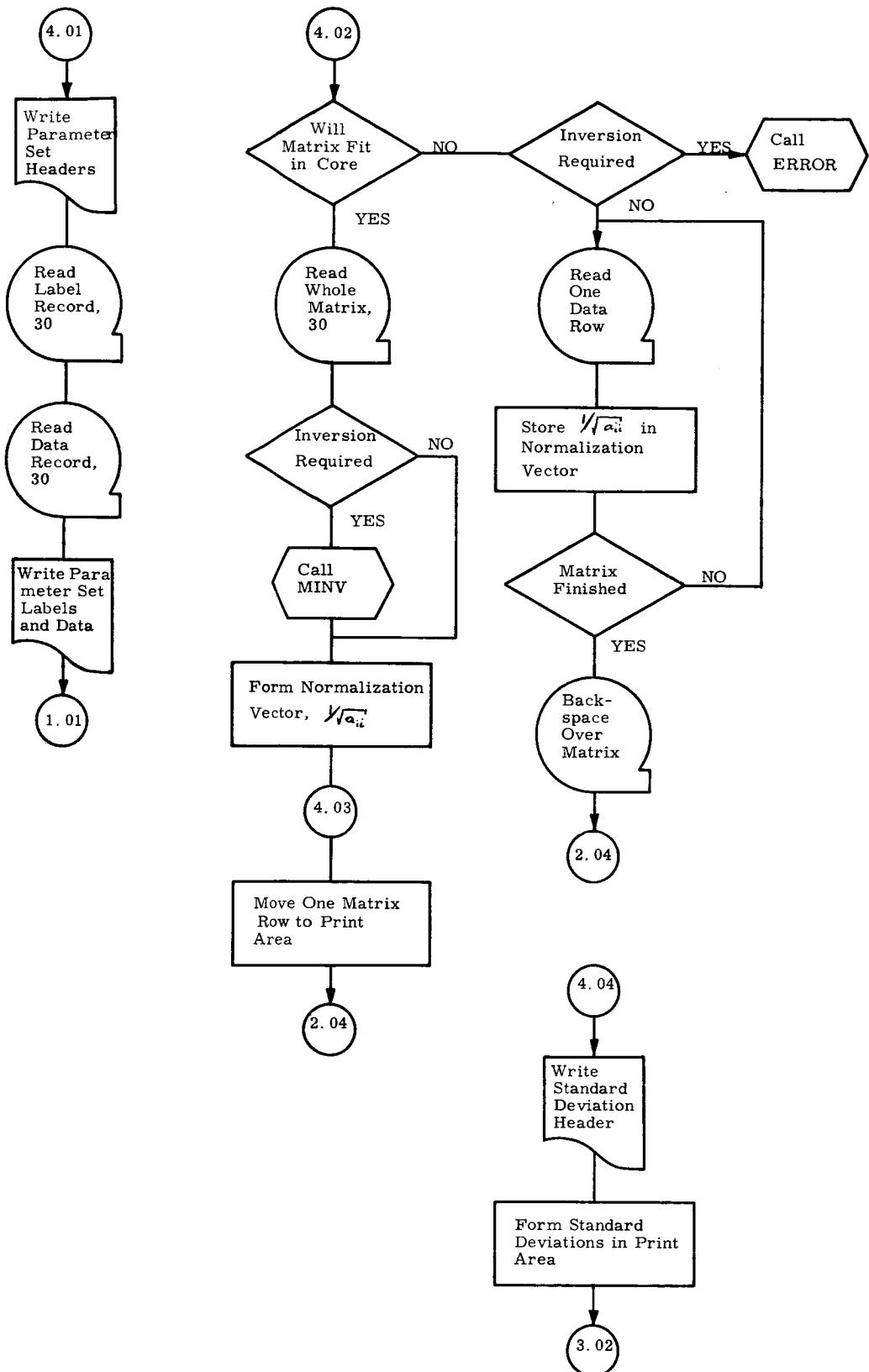


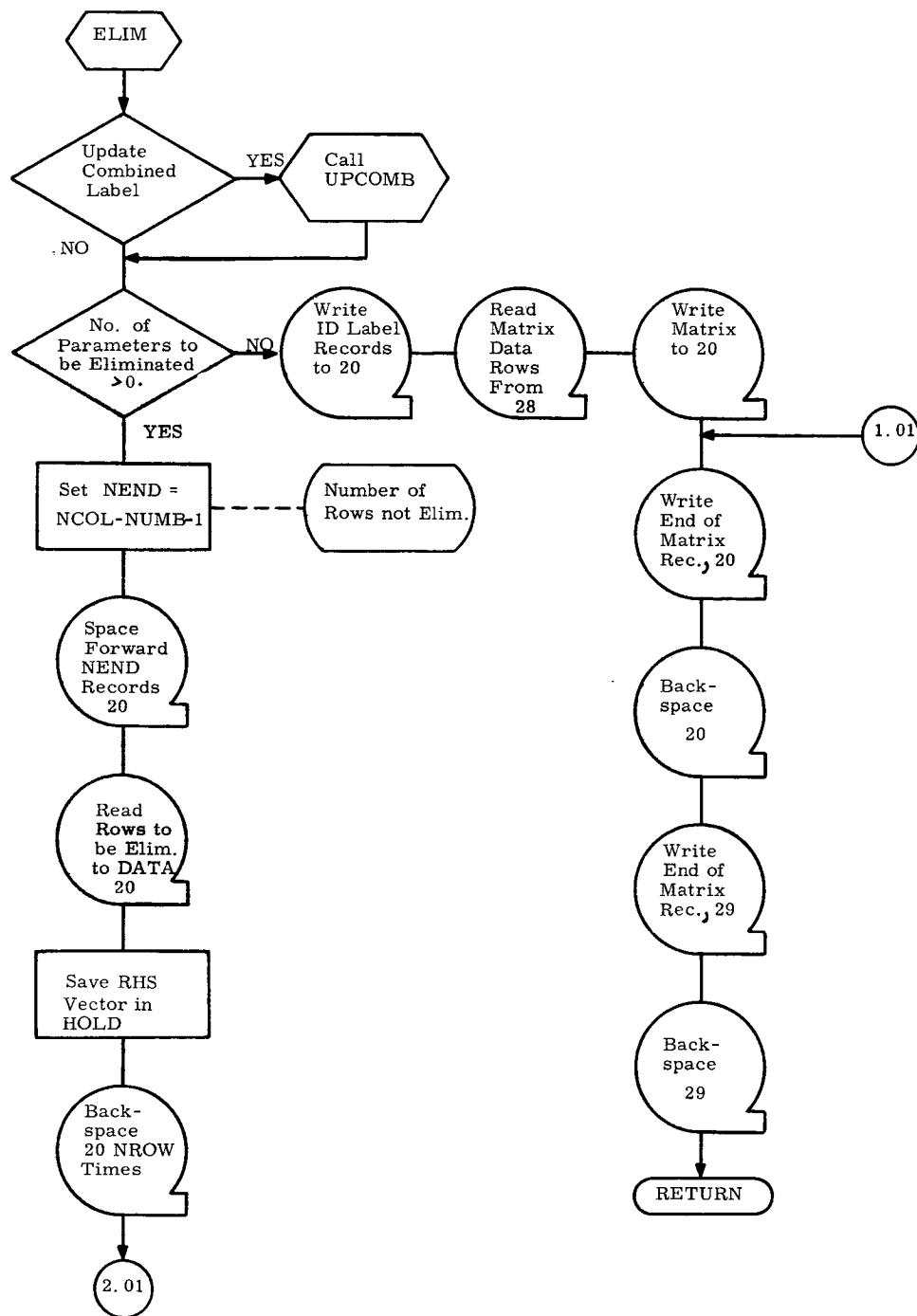


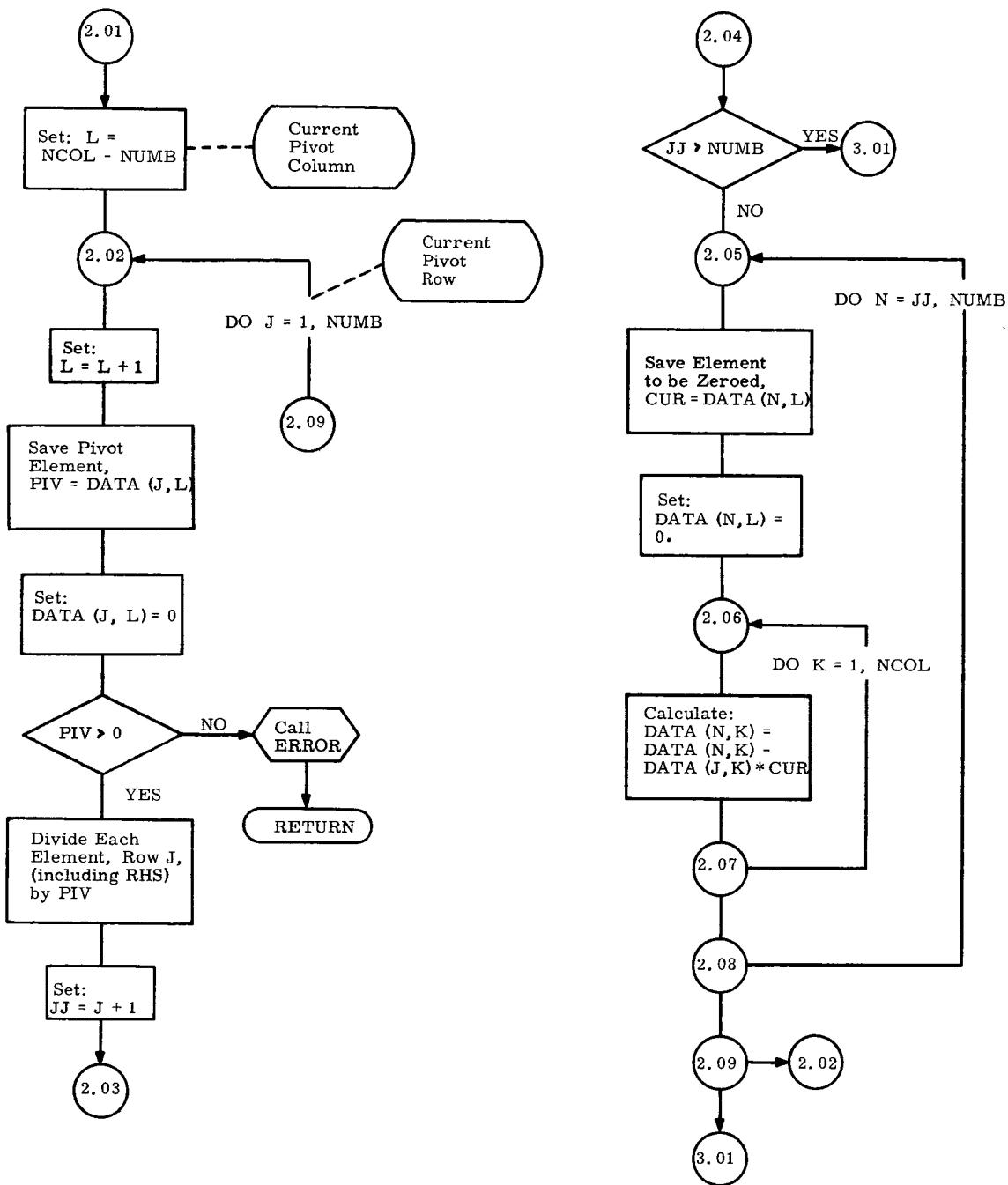


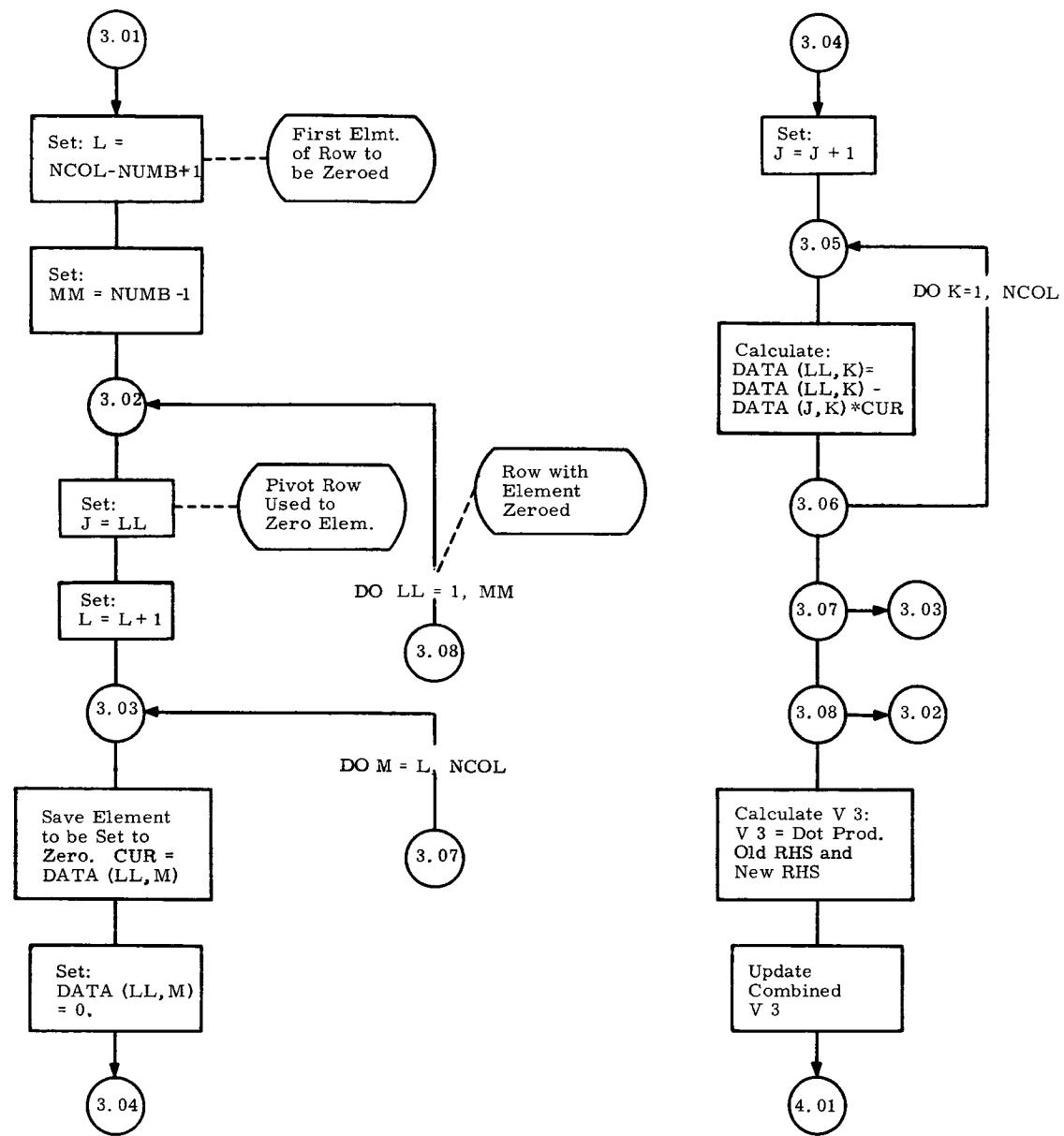


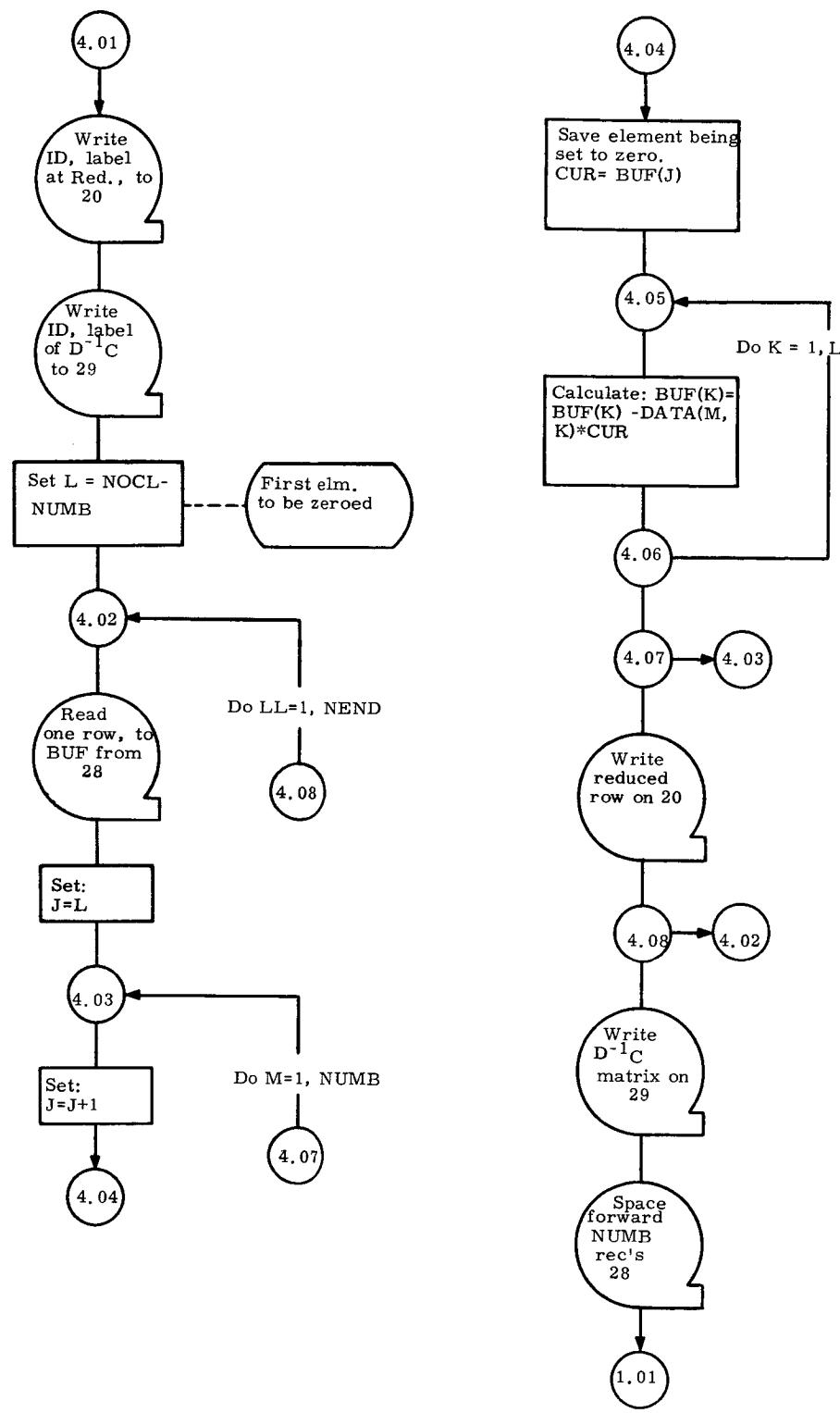


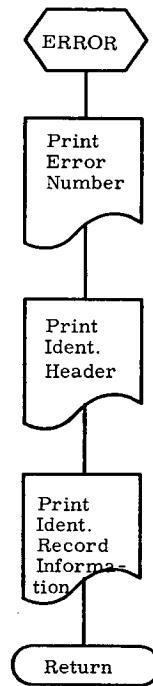


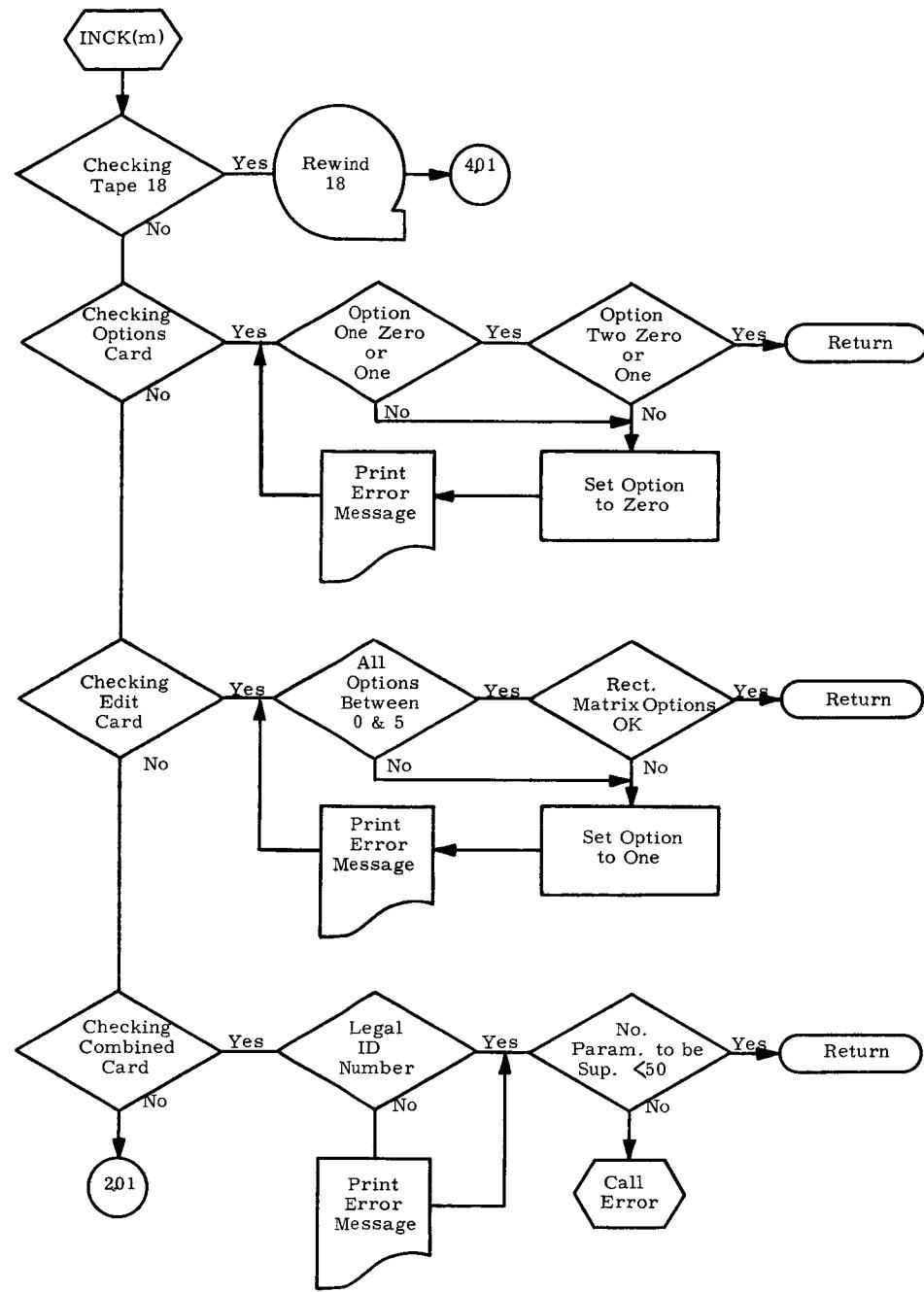


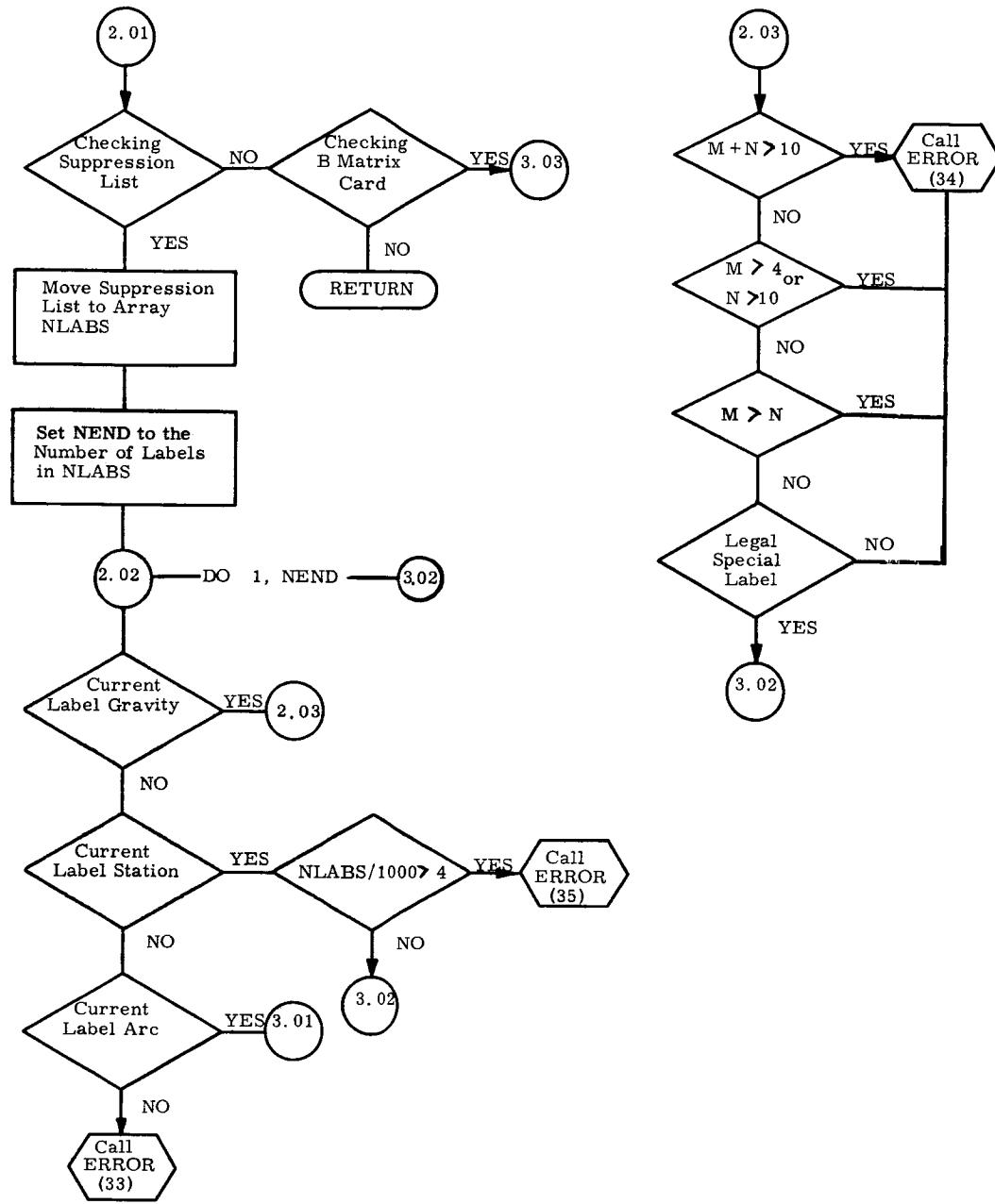


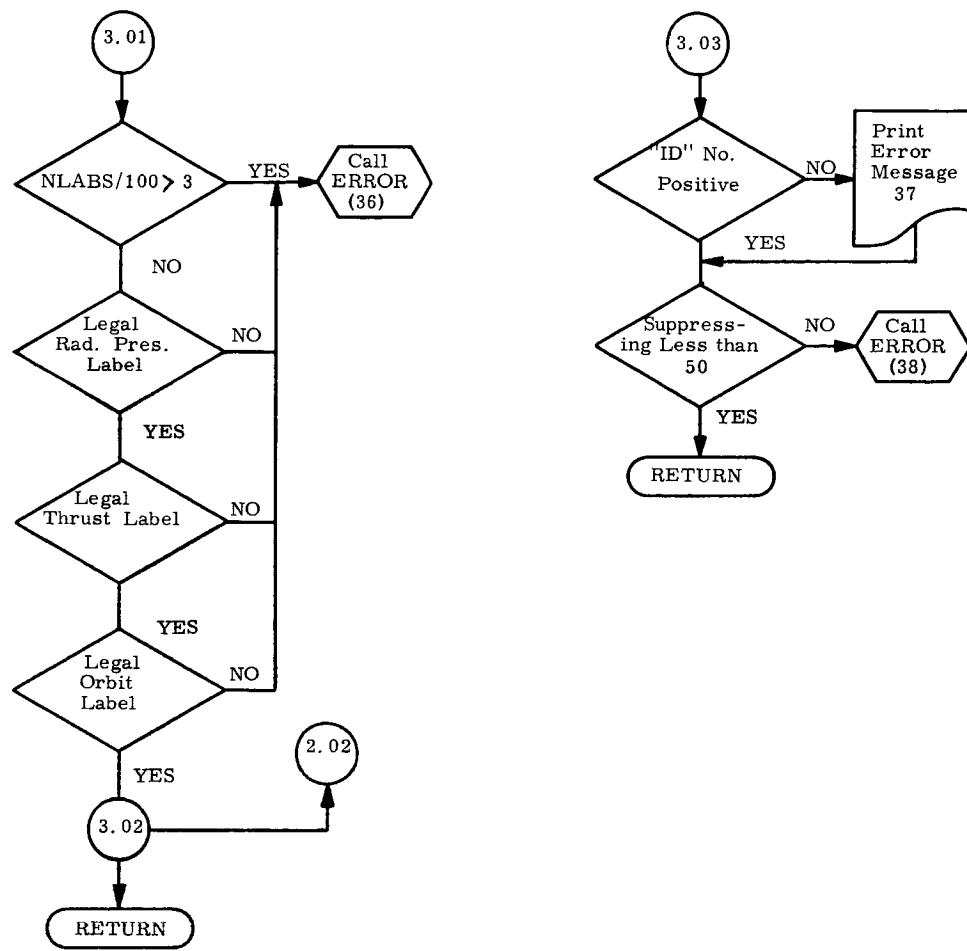


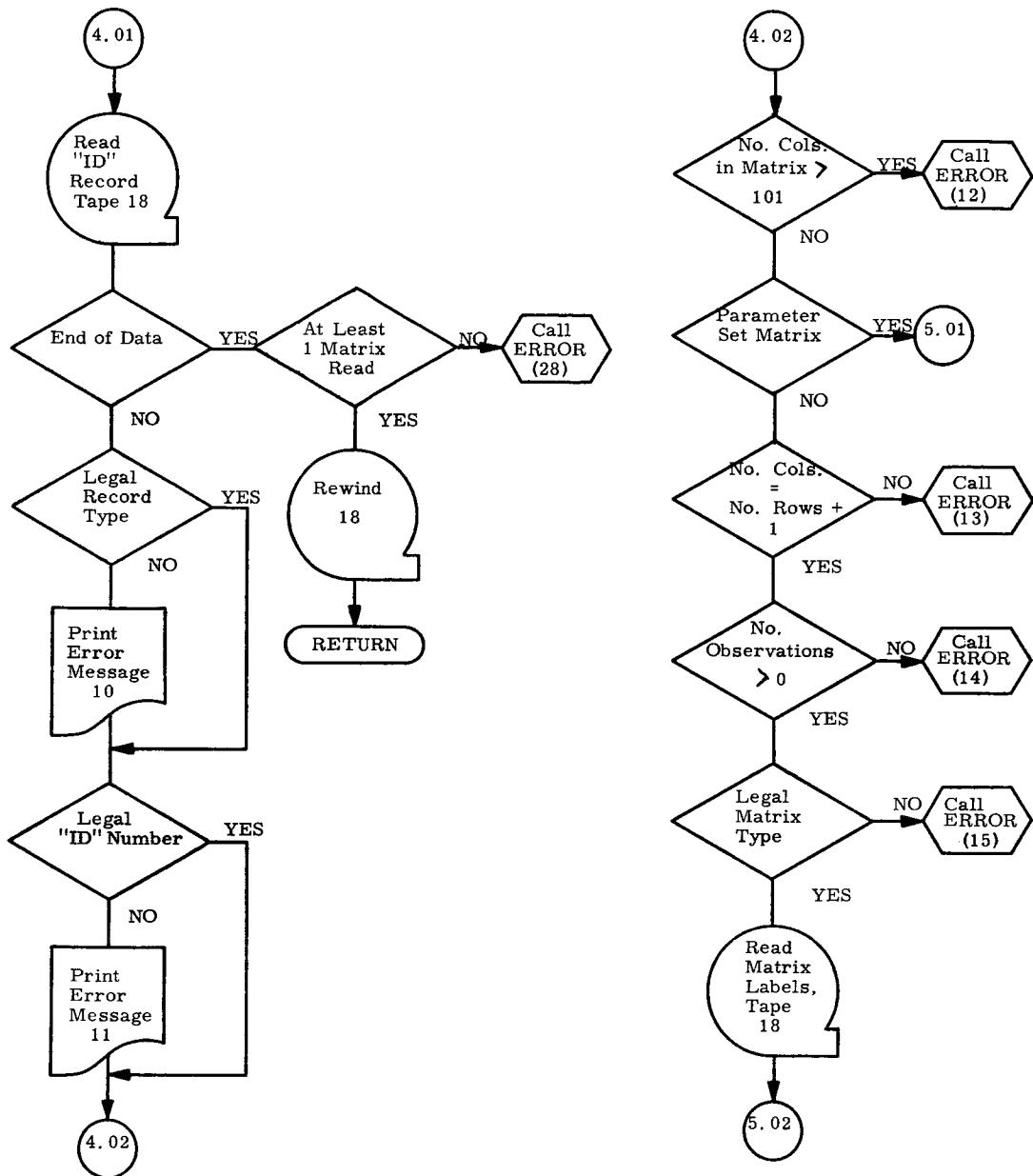


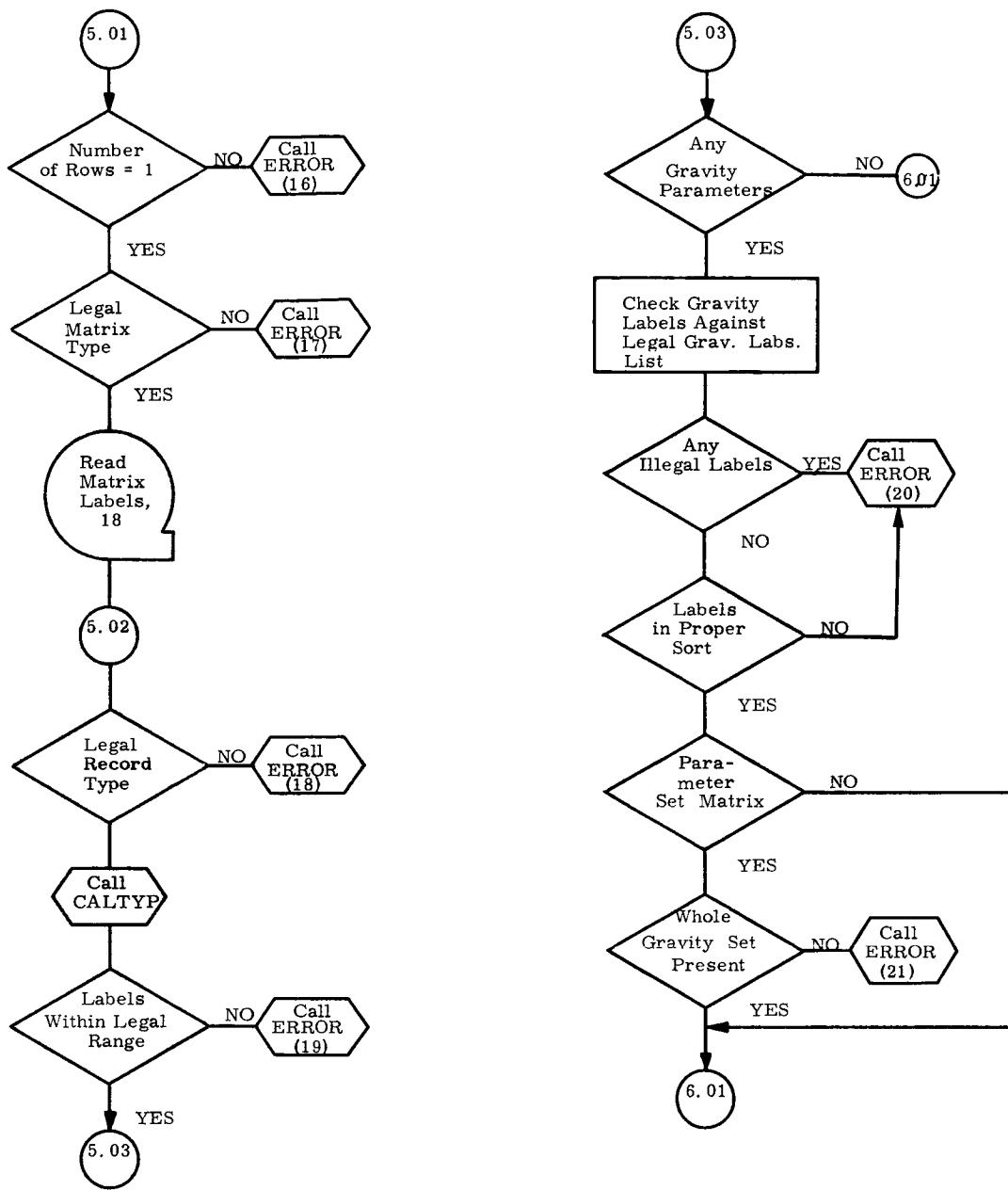


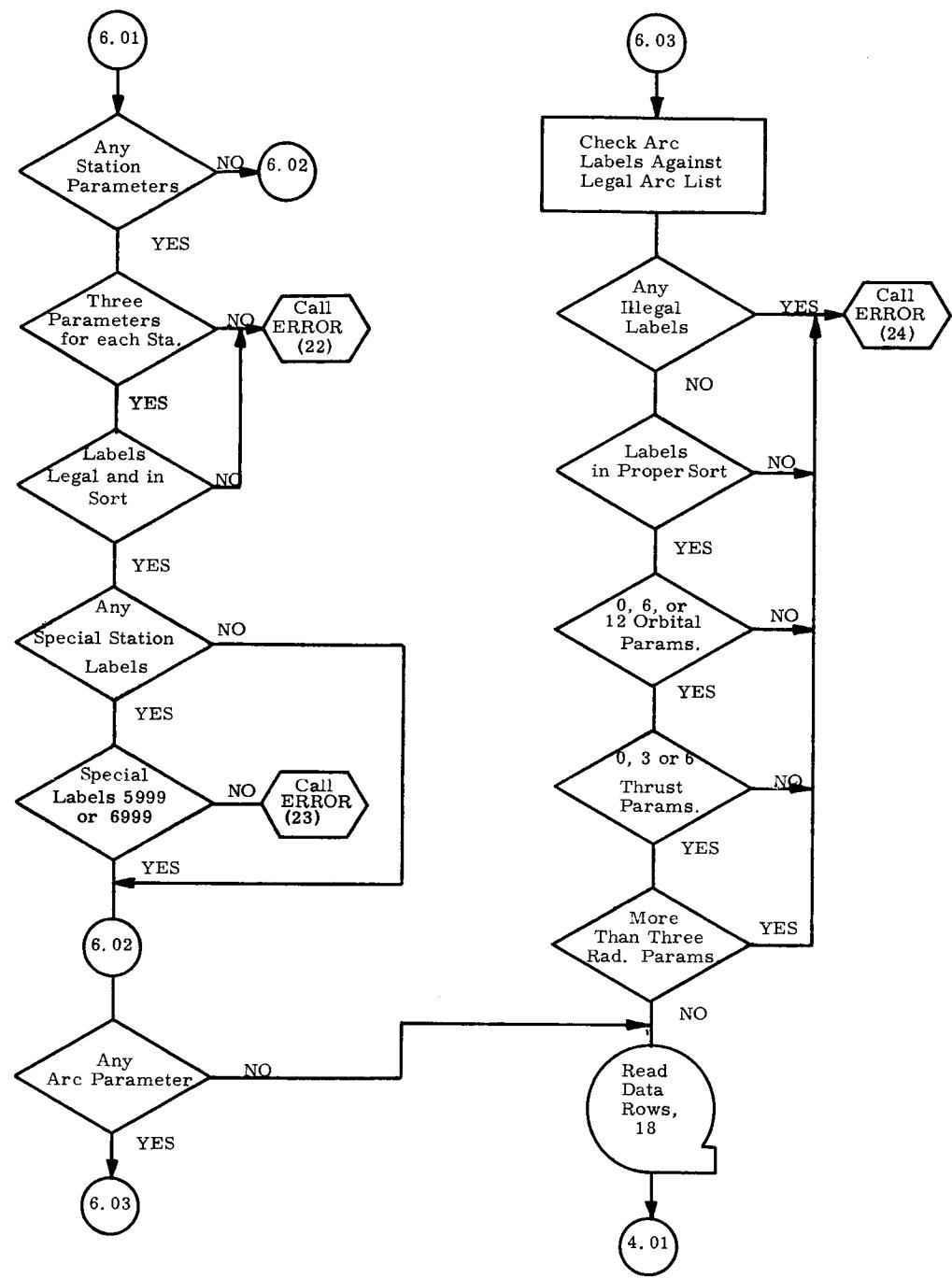


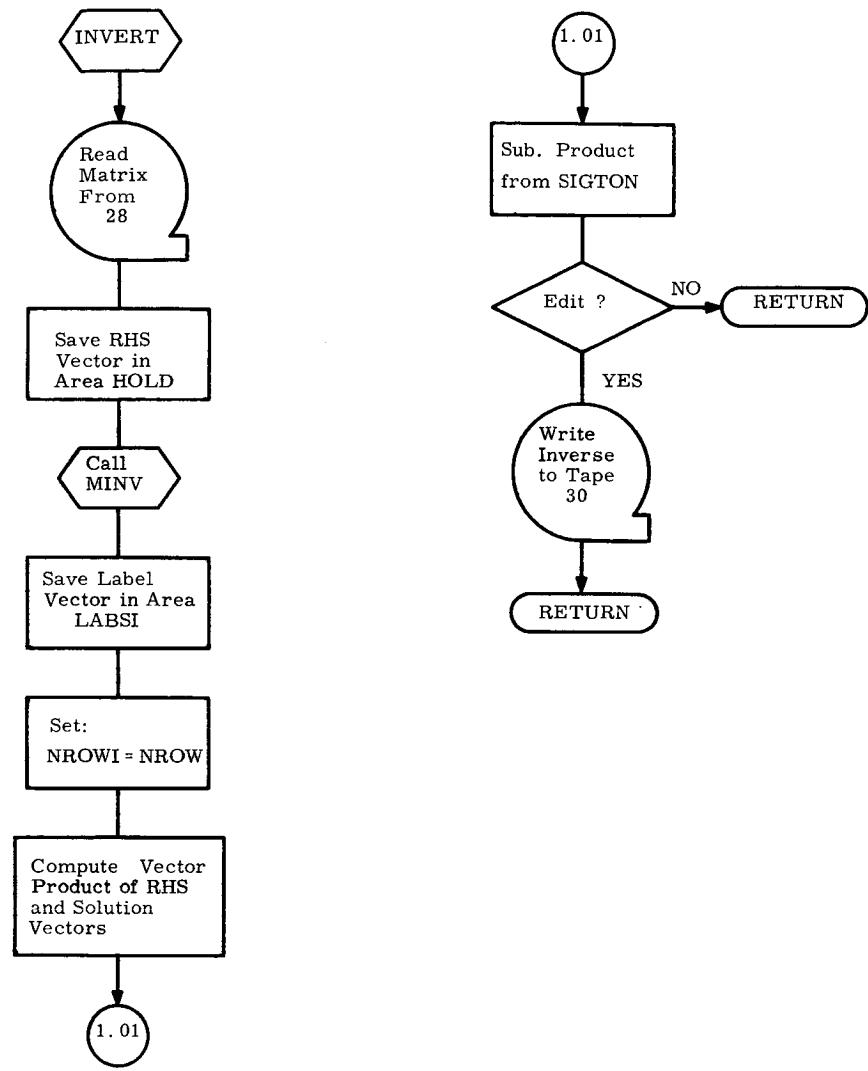


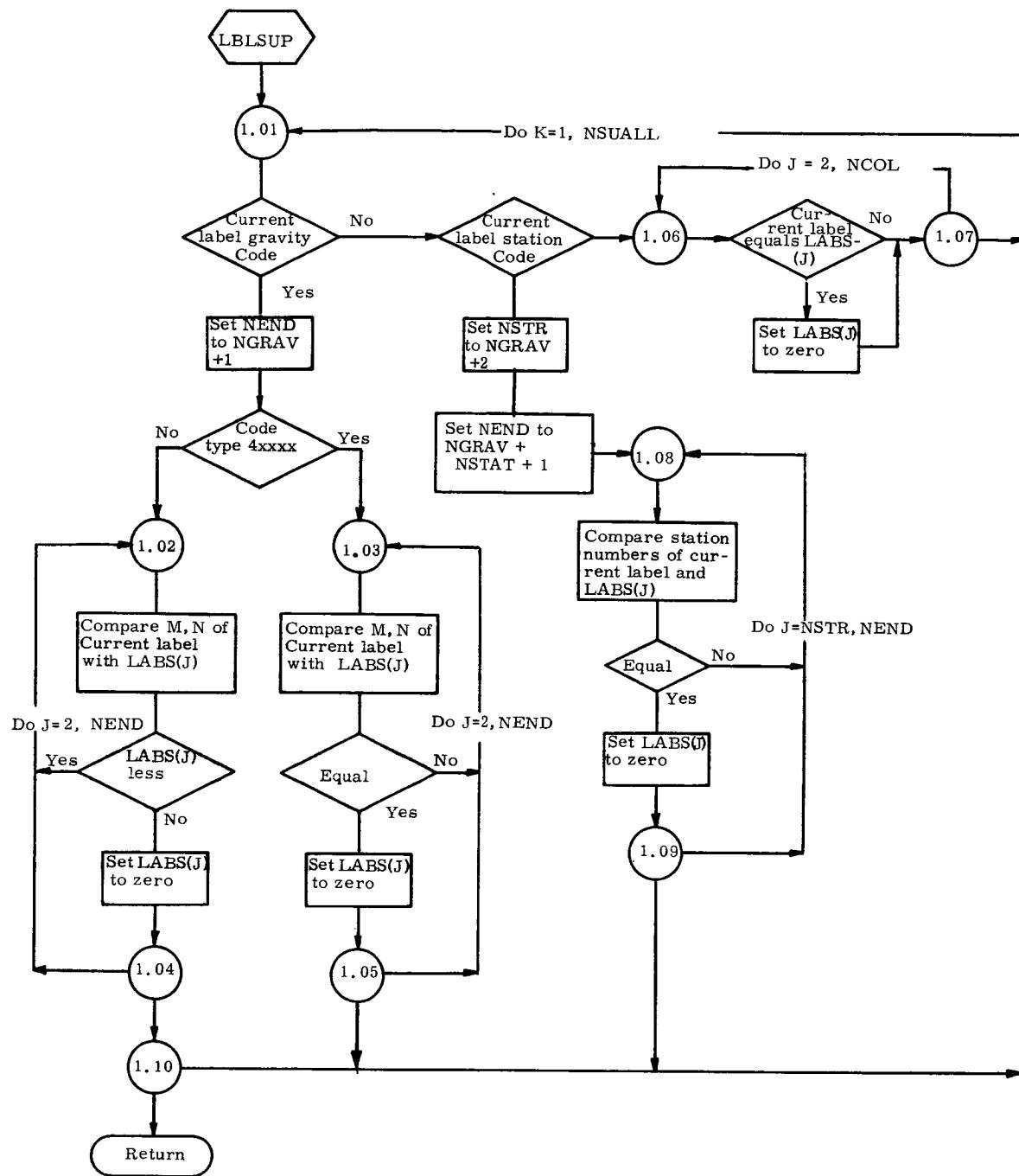


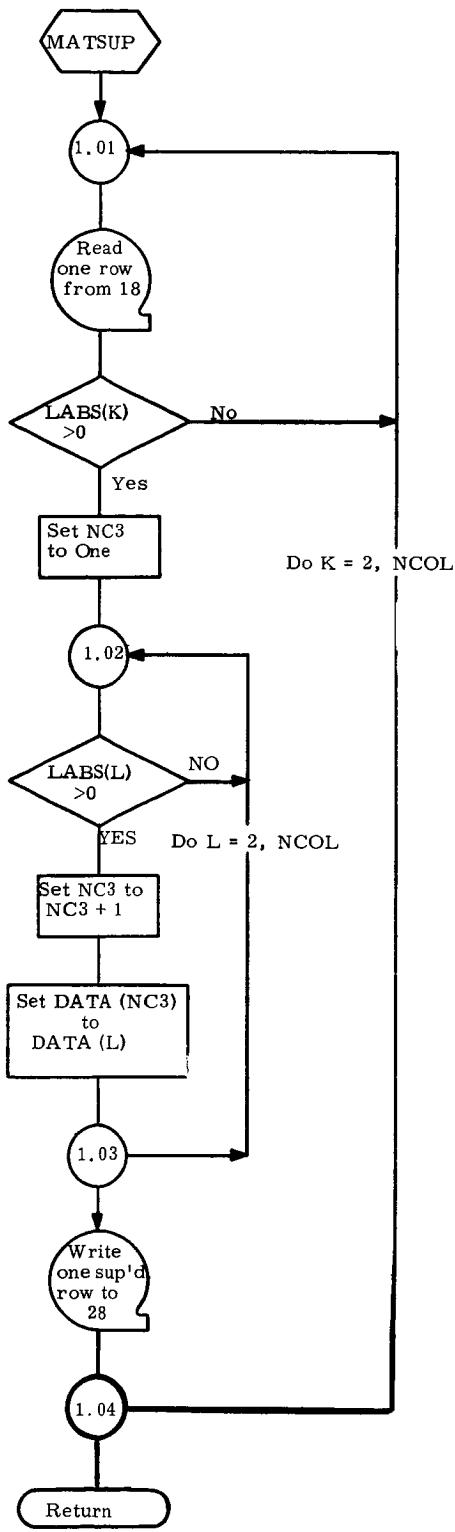


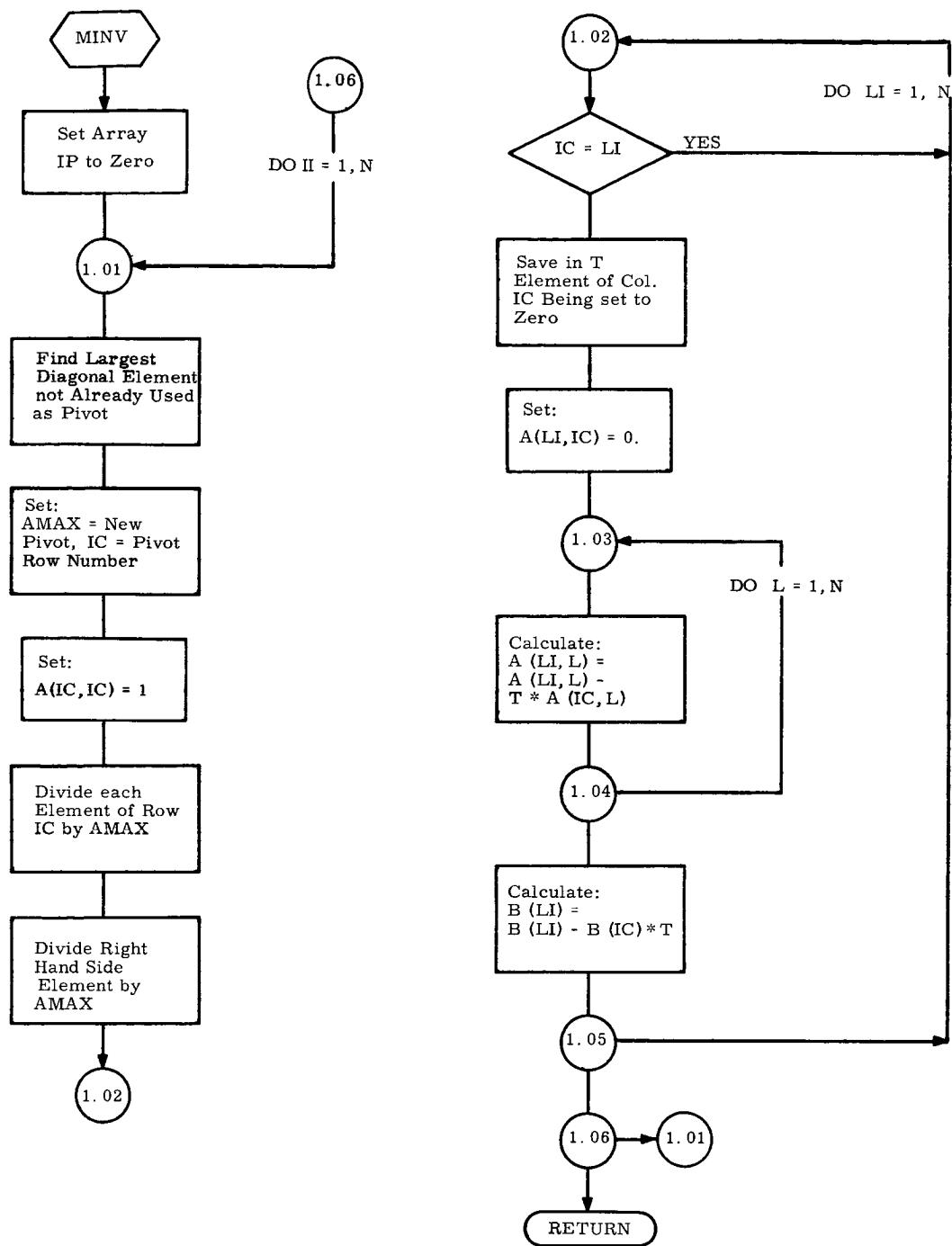


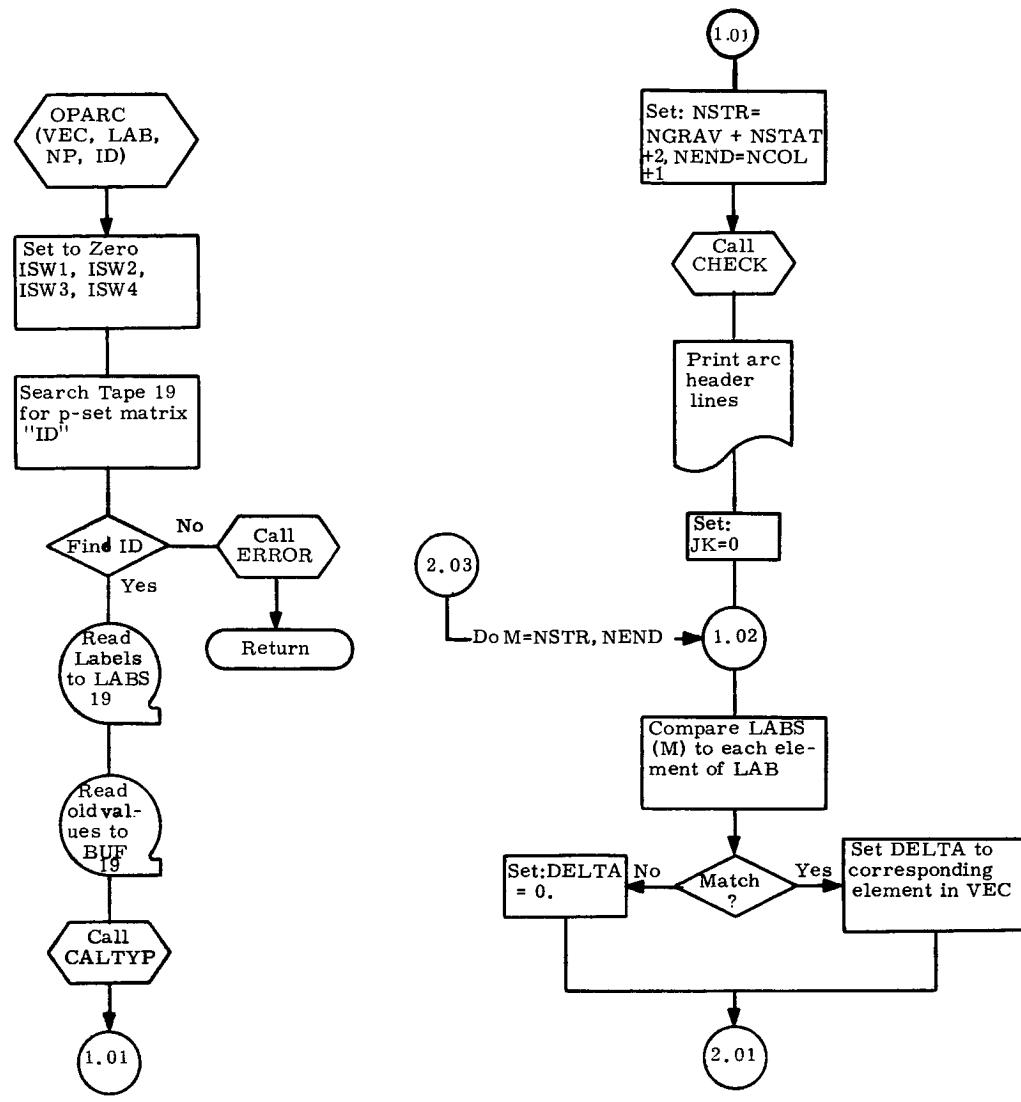


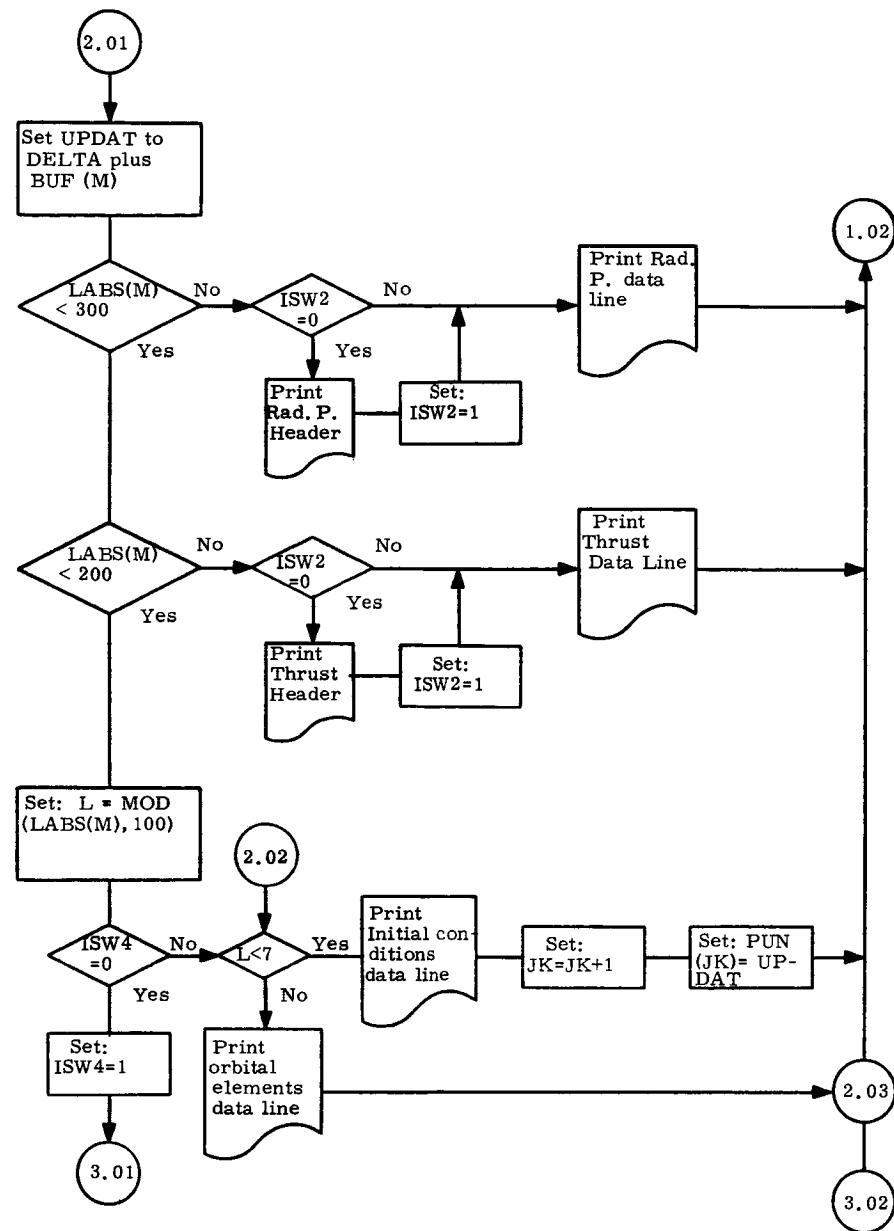


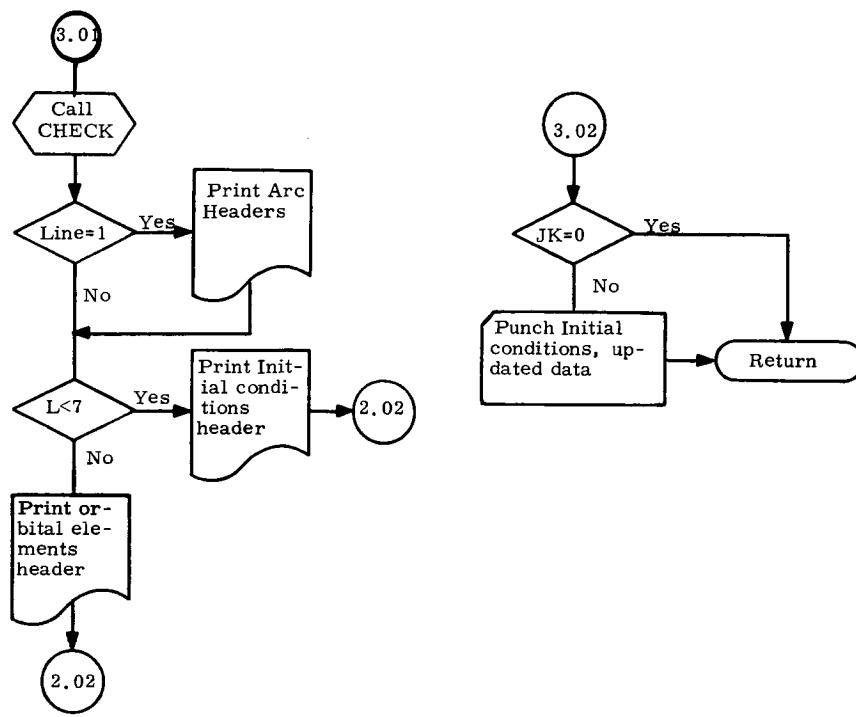


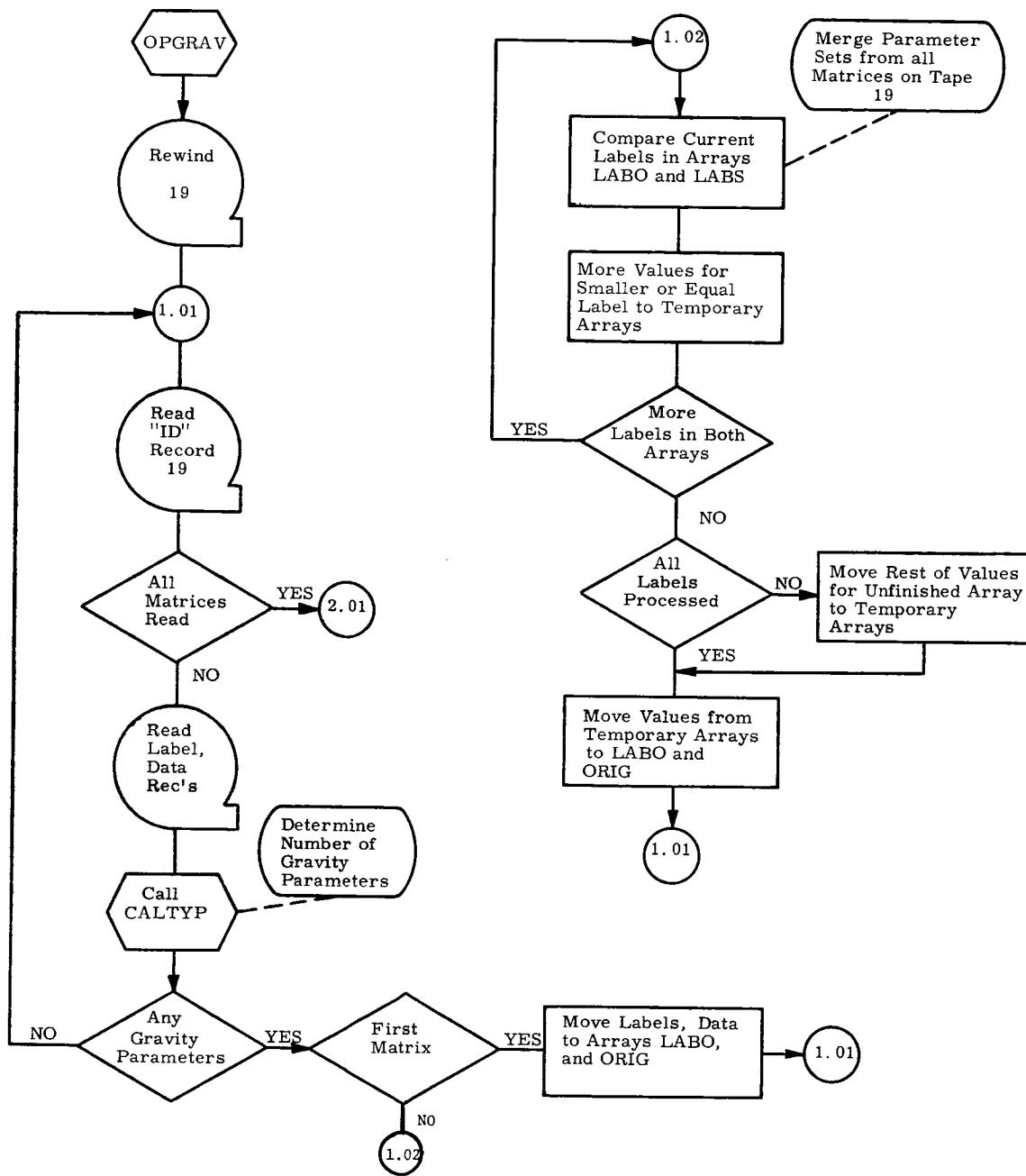


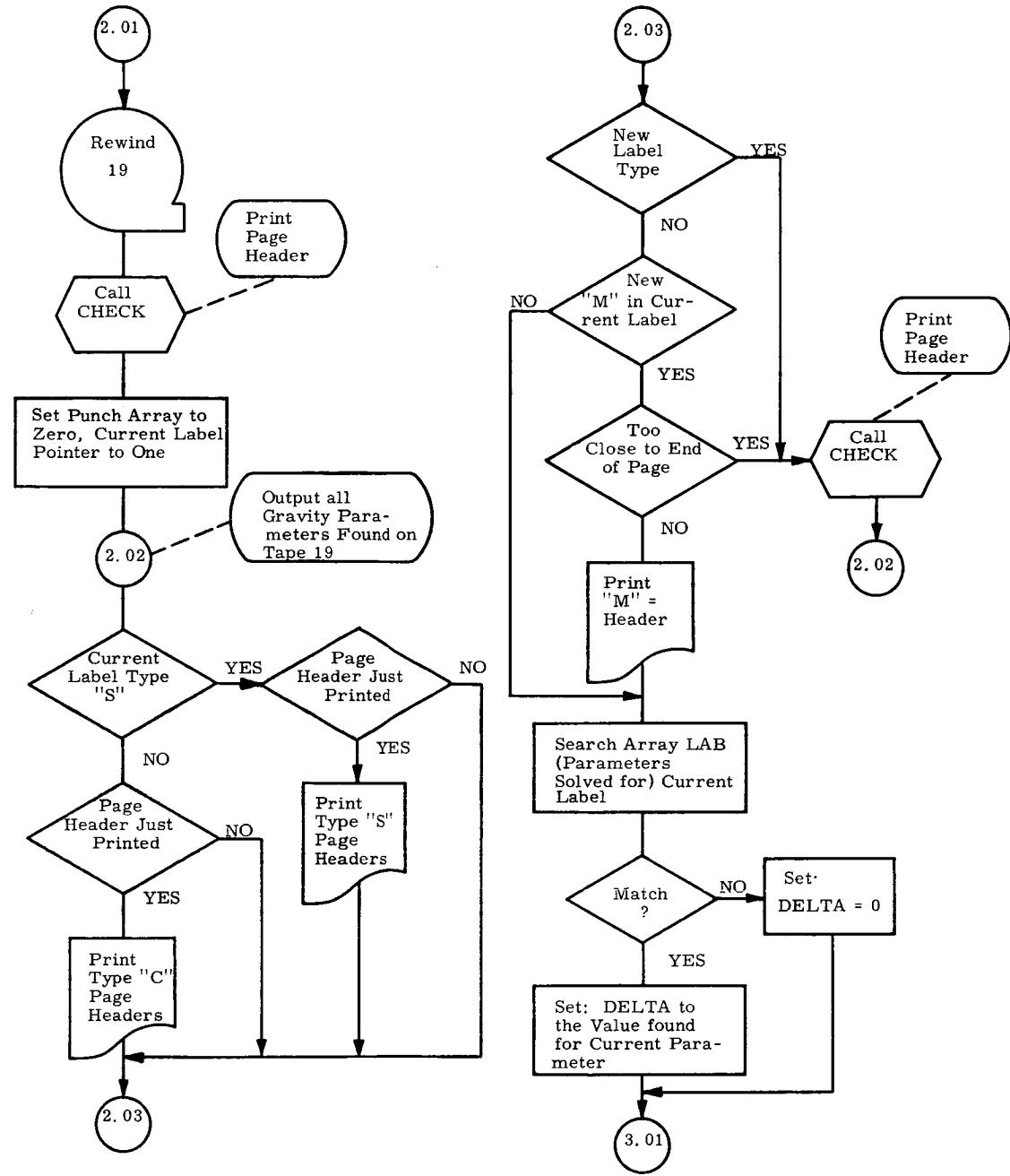


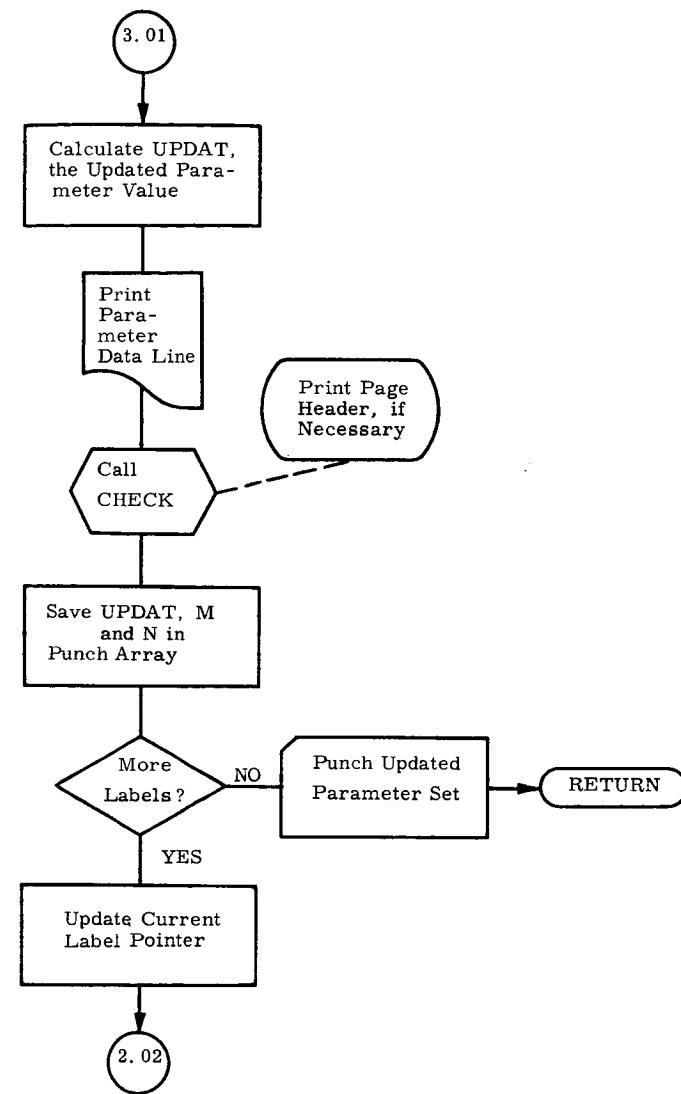


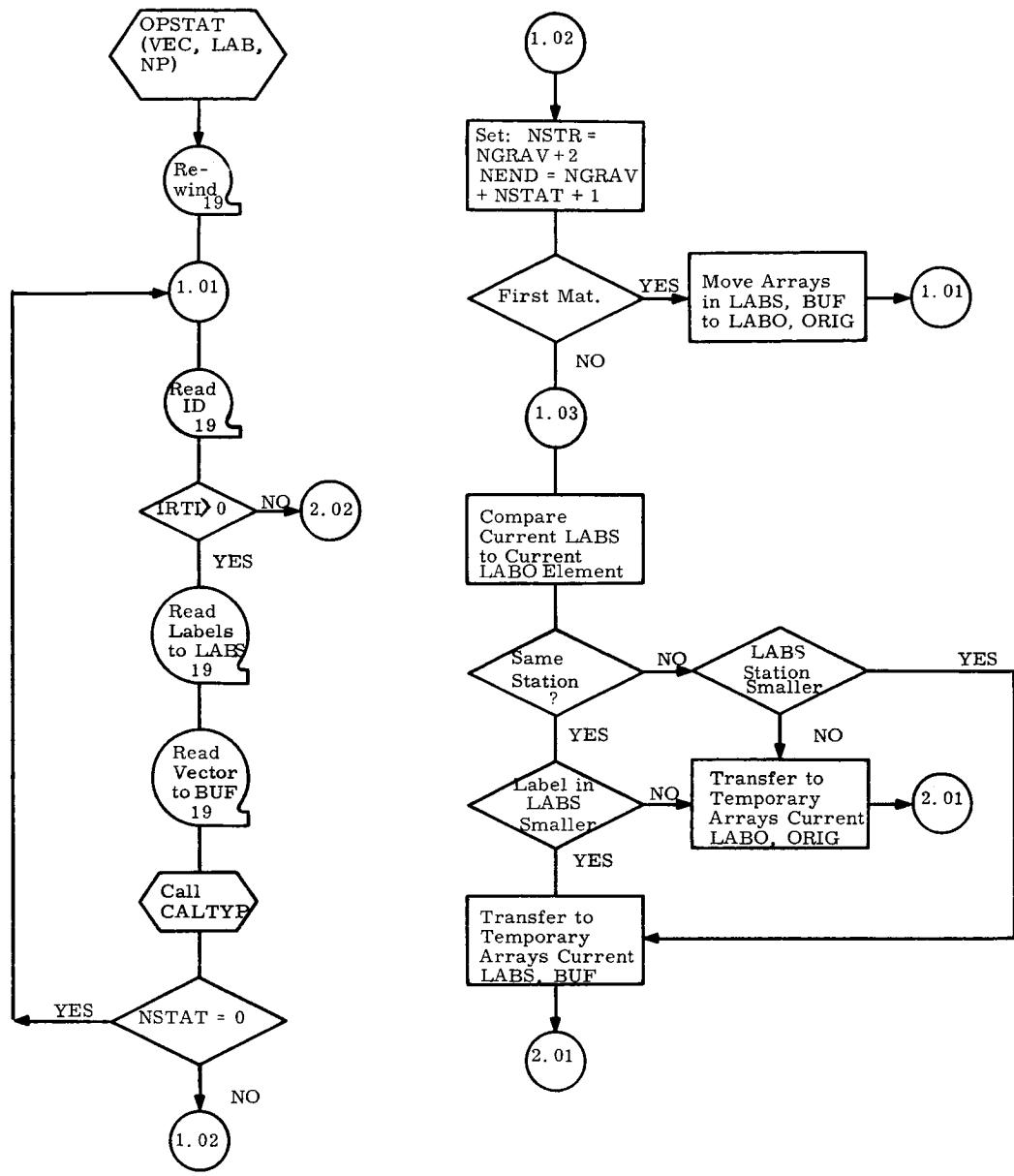


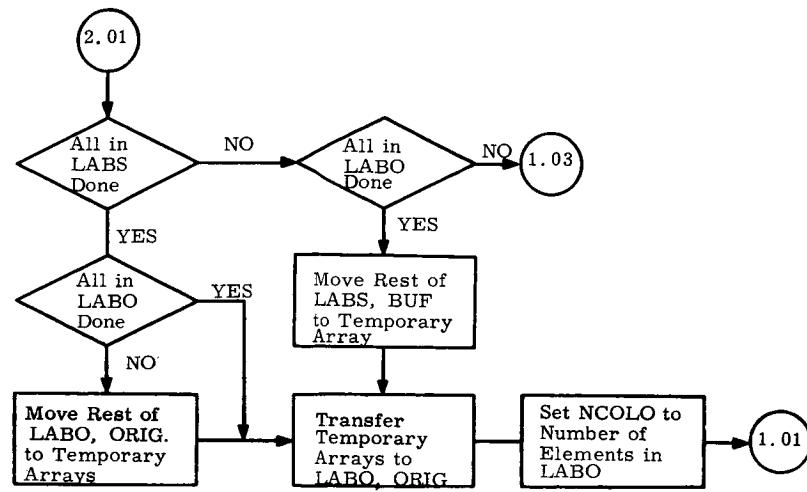


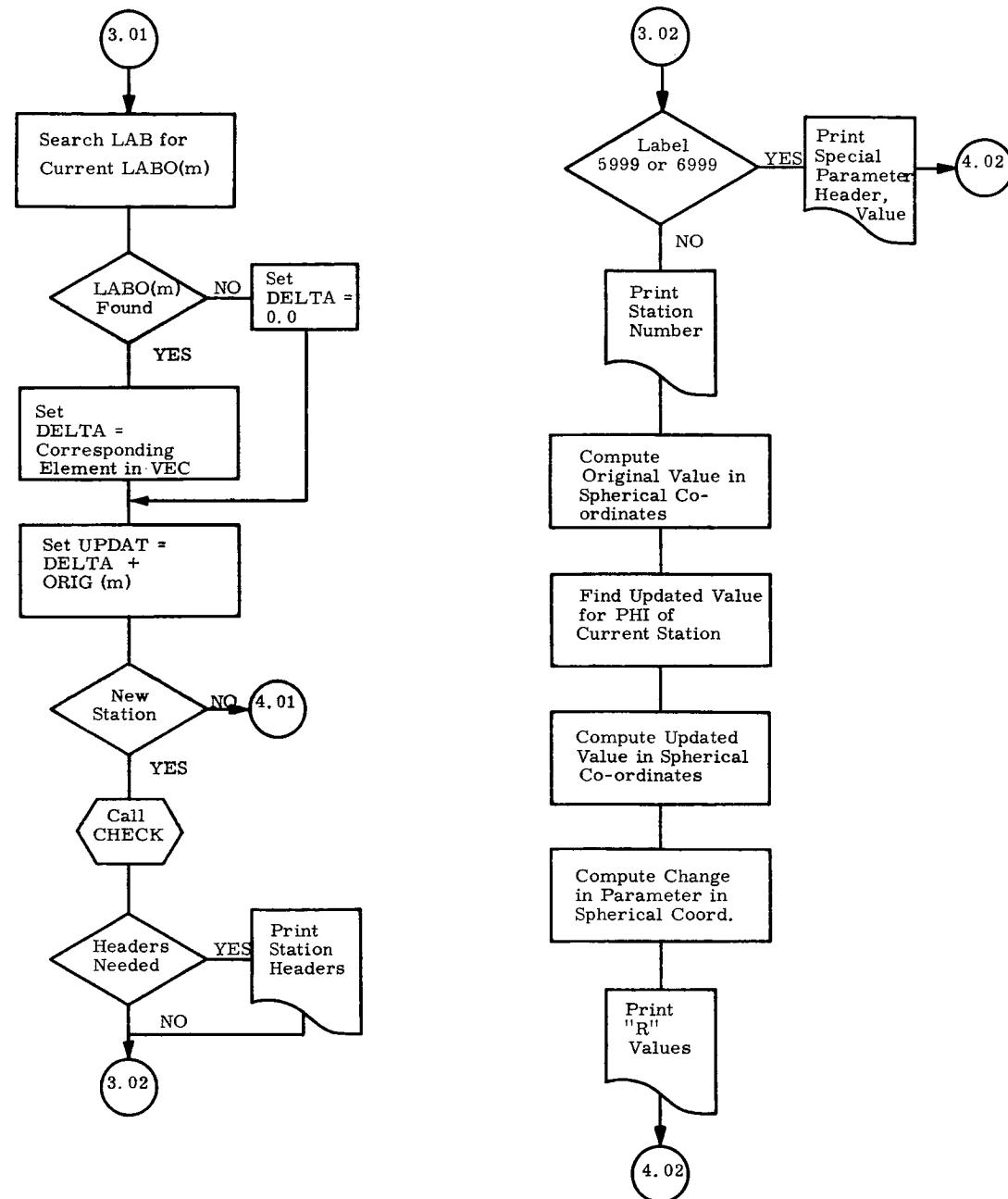


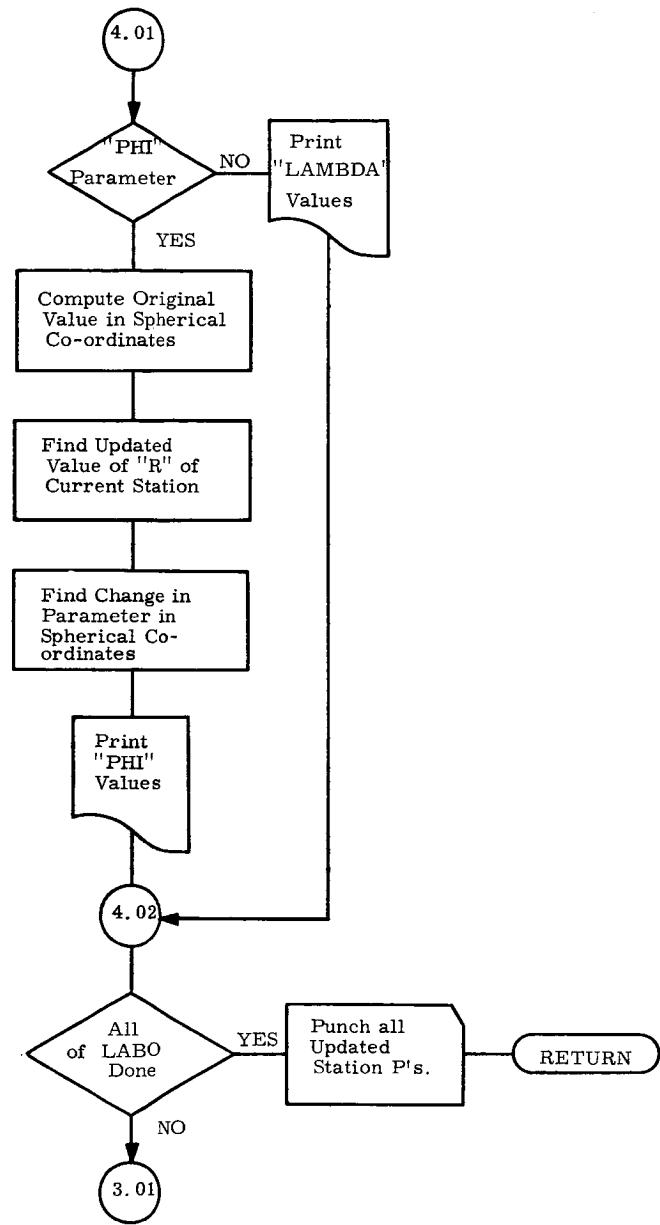


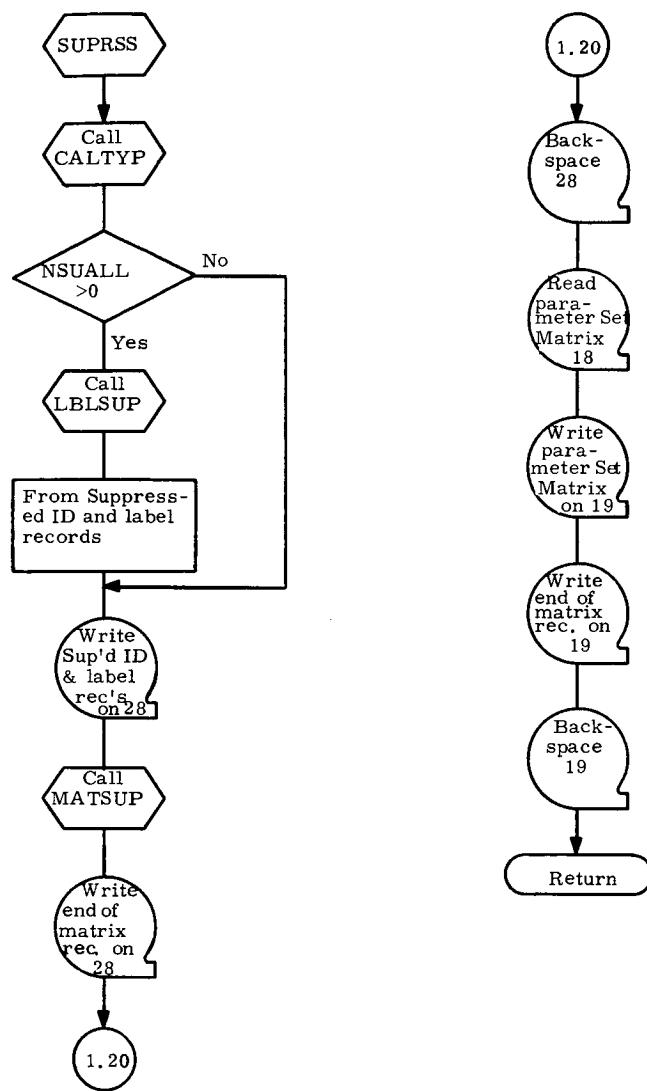


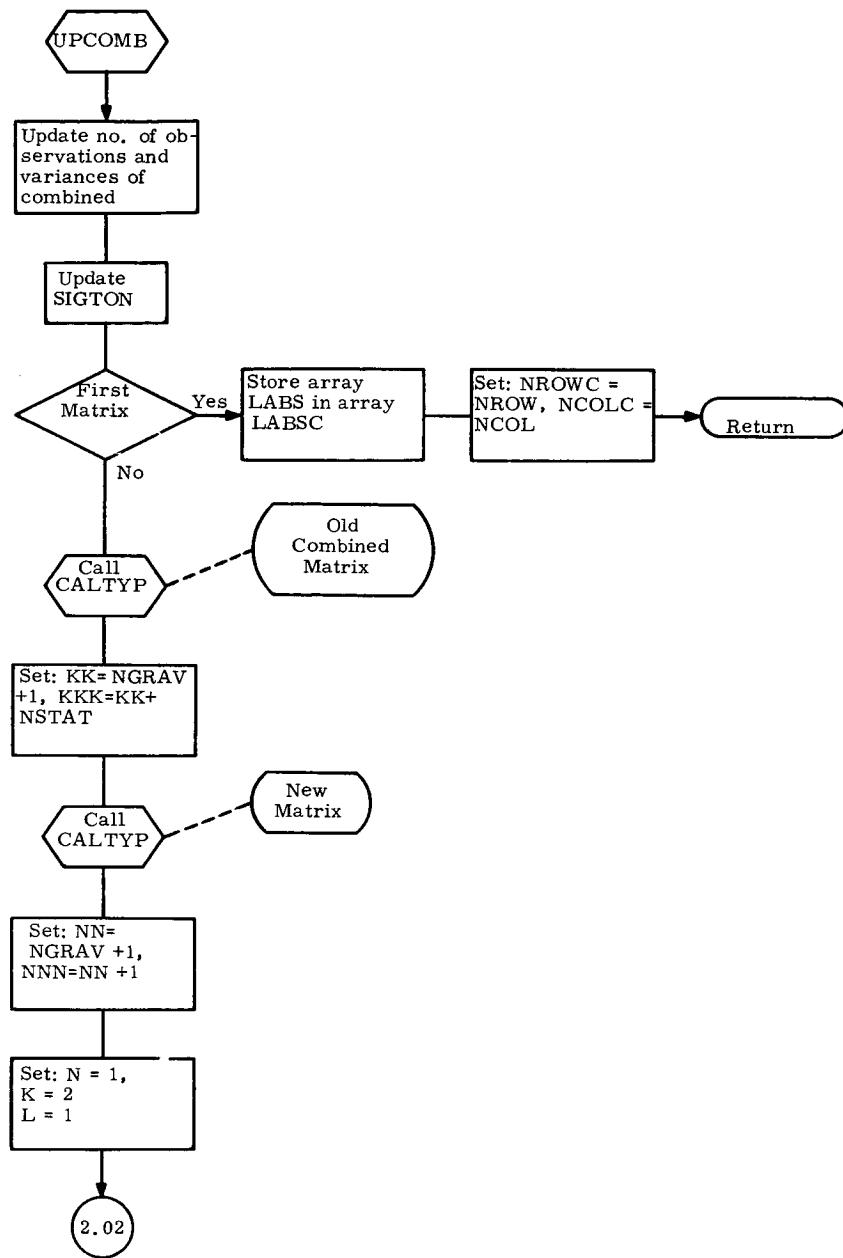


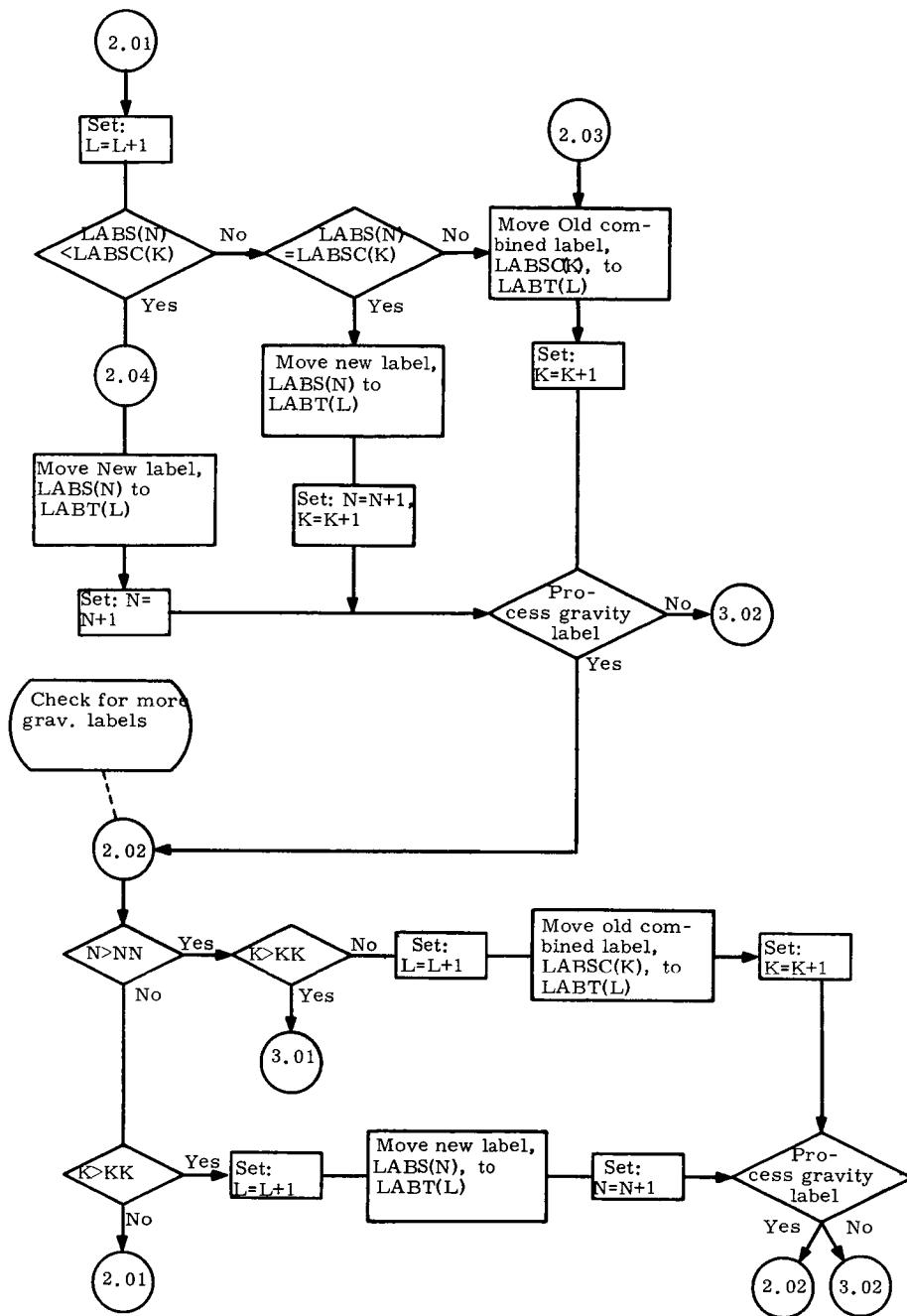


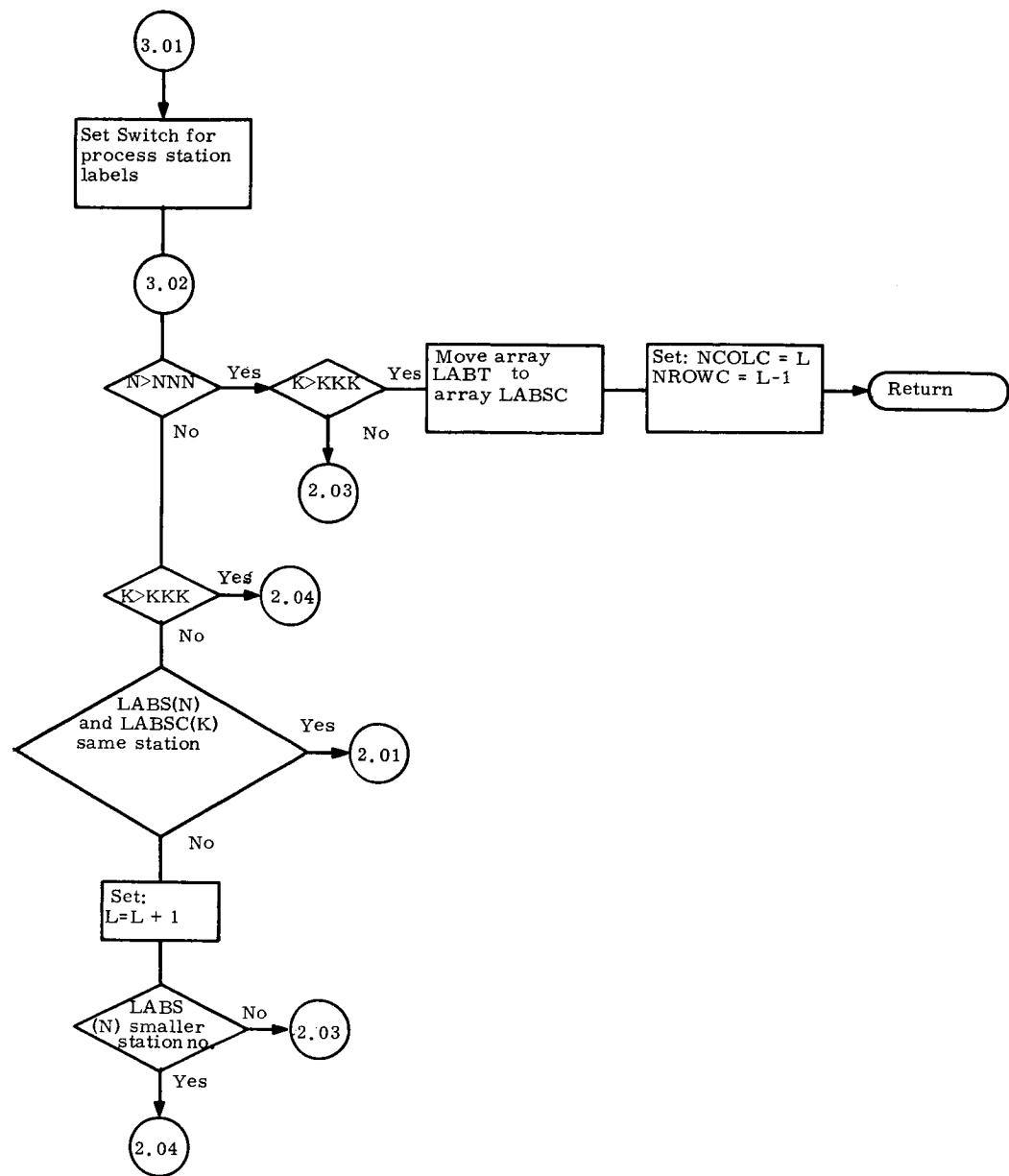












PART 7

MERGE PROGRAM

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SECTION I

INTRODUCTION

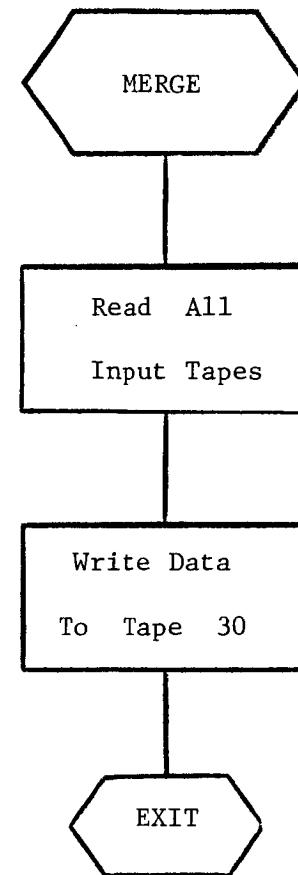
## INTRODUCTION

MERGE is a data handling system, designed to consolidate matrices generated by NORMAL EQUATIONS onto one tape, to be used as input to SOLVE. It will transfer matrices from up to four input tapes to a fifth tape, which may also, if desired, contain matrices to be saved. The output merged tape may be edited in any one of the standard edit formats used in SOLVE. Specified matrices from the four input tapes may be deleted; i. e., they will not be written on the output merged tape. The matrices must be in the standard B-matrix or parameter set matrix formats used by SOLVE. Up to 80 matrices may be written on a single output tape.

Input to MERGE consists of (1) up to four old merged tapes and/or B-matrix tapes generated by NORMAL EQUATIONS, and (2) various input cards indicating program options and other information. A write-up of the input cards appears on page 3.1. Output consists of (1) the new merged tape, and (2) any editing requested. The input tapes are not destroyed.

SECTION II  
SYSTEM FLOW CHART

LUNGFISH MERGE SYSTEM FLOWCHART



SECTION III  
USER INFORMATION

## INPUT CARDS

### 1) Card Type One, Options Card

cc 5        Integer 1, 2, 3 or 4 indicating the number of input tapes.

cc 9-10      Positive integer less than or equal to 80, indicating the maximum number of matrices to appear on output merged tape.

cc 15        Integer edit code for the output merged tape, as follows:

0 - No Editing Required

1 - Unnormalized

2 - Normalized, diagonal elements one

3 - Inverse

4 - Identification Records Only

5 - Normalized Inverse with Standard Deviations

(Note: For more detail on edit formats, see the subroutine write-up for EDIT, in SOLVE. )

cc 20        Integer 0 or 1, as follows:

0 - The output tape does not contain matrices to be saved.

1 - The output tape does contain matrices to be saved.

cc 24-25      Positive integer indicating the number of matrices which, if found on one of the four input tapes, will not be written on the merged tape (i. e., will be deleted).

### 2) Card Type Two, Matrix Deletion List

cc 1-70      Positive integers, in five column fields. These are the matrix identification numbers for those matrices, if any, to be deleted. This list may extend over more than one card. If no matrices are to be deleted, omit this card.

3) Card Type Three, Page Header

cc 1-72      Alpha-numeric data to appear at the top of each page  
of output if editing is required. If editing is not  
specified, omit this card.

## OPERATING INSTRUCTIONS

- 1) The system control cards required in the overall deck setup are:

```
$JOB  
$SETUP    04  
$SETUP    06      (omit if only one input tape)  
$SETUP    14      (omit if less than three input tapes)  
$SETUP    15      (omit if less than four input tapes)  
$SETUP    16  
$EXECUTE  IBJOB  
$IBJOB  
        MERGE decks, binary or source  
$DATA  
        MERGE data deck
```

- 2) The tape setup is:

<u>DCS Unit</u>	<u>Tape Function</u>
04	First Input Tape
06	Second Input Tape
14	Third Input Tape
15	Fourth Input Tape
16	Output Tape

If only one tape is used, it is mounted on DCS unit 04; if two are used, they are mounted on units 04 and 06; and so forth.

- 3) Output consists of the output merged tape on DCS unit 16, and any editing requested.

## ERROR LIST

Number	Routine	Meaning
101	MERGE	The number of matrices to be written on the merged tape exceeds 80.
102	MERGE	The number of tapes to be merged is less than one or greater than four.
6	BEDIT	Edit requested of a scratch tape (system or program bug).
103	MEDIT	Edit requested requires the inversion of a matrix of order 83 or greater.

## PROGRAM DECK ARRANGEMENT

The MERGE decks do not have to be in any special order, they are currently set up as follows:

. UN18.

. UN20.

. UN28.

. UN29.

. UN30.

MERGE

BEDIT

CHECK

ERROR

MEDIT

MINV

## FILE BLOCK PROGRAM OPTIONS

1) Tape 18:

    Filename is "UNIT18"

    Mode is "BIN"

    Unit assignment is "A(1)"

2) Tape 20:

    Filename is "UNIT20"

    Mode is "BIN"

    Unit assignment is "A(3)"

3) Tape 28:

    Filename is "UNIT28"

    Mode is "BIN"

    Unit assignment is "B(1)"

4) Tape 29:

    Filename is "UNIT29"

    Mode is "BIN"

    Unit assignment is "B(2)"

5) Tape 30:

    Filename is "UNIT30"

    Mode is "BIN"

    Unit assignment is "B(3)"

## TAPE FORMATS

MERGE uses five tapes, all binary. The input tapes are designated 18, 20, 28 and 29 in the code. Each input tape contains various matrices in the standard format (given in the following pages) used in SOLVE, with an end of logical tape record. The output tape is designated tape 30 in the code. At the start of a MERGE run it may contain matrices and an end of logical tape record, or it may be a scratch tape. (The card input to MERGE specifies which type of output tape is being used.) At the end of a MERGE run, the output tape is in standard format for SOLVE.

## STANDARD FORMAT, SQUARE MATRICES

### Matrix Identification (ID) Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT1	1	Integer	"10001"
IDMAT	1	Integer	Matrix Identification Number, 1 to 99998
NRROW	1	Integer	Number of matrix data rows
NCOL	1	Integer	Number of matrix data elements per row, including Right Hand Side element
V1	1 x 2	Double	Total Variance
V2	1 x 2	Double	Dummy Variance word
V3	1 x 2	Double	Arc Variance
NOB	1	Integer	Number of Observations
ITYPE	1	Integer	Code for matrix type, as follows: "1" B-matrix "3" Combined matrix "5" Reduced matrix "6" Inverse combined matrix "7" Suppressed matrix
BNAME	2	Alpha	Alpha-numeric name for matrix, for editing purposes only. It can be blanks.

### Matrix Label Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT2	1	Integer	"10002"
IDUM	1	Integer	Dummy parameter label
LABS	NCOL-1	Integer	Parameter labels

### Matrix Data Element Records, NROW Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT3	1	Integer	"10003"
RHS	1 x 2	Double	Right Hand Side element
DATA	(NCOL-1)x 2	Double	Matrix data elements, one matrix row

### End of Logical Tape Record, One Per Tape

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT	1	Integer	" - 19991"
IDUM	13	Integer	Dummy words to fill out record

## STANDARD FORMAT, PARAMETER SET MATRIX

Parameter Set Identification (ID) Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT1	1	Integer	"10011"
IDMAT	1	Integer	Matrix Identification Number (same as in matrix ID record for corresponding matrix)
NRDW	1	Integer	"1"
NCOL	1	Integer	Number of elements in parameter set
IDUM	7	Integer	Dummy words to fill record
ITYPE	1	Integer	"8"
BNAME	2	Alpha	Alpha-numeric name for parameter set, for editing only. It may be blanks.

Parameter Set Label Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT2	1	Integer	"10012"
LABS	NCOL	Integer	Parameter Labels

Parameter Set Data Element Record, One Per Matrix

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
IRT3	1	Integer	"10013"
DATA	NCOL x 2	Double	Parameter Values

## PERM COMMON DEFINITIONS

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
B	82 x 2	Double	Right hand side or solution vector for inversion
BNEW	60 x 2	Double	Solution vector from backsubstitution
SIGT $\varnothing$ N	1 x 2	Double	Signal to noise ratio
V1	1 x 2	Double	Total variance
V2	1 x 2	Double	Dummy variance words
V3	1 x 2	Double	Arc variance
V1C	1 x 2	Double	Combined matrix total variance
V2C	1 x 2	Double	Combined matrix dummy variance
V3C	1 x 2	Double	Combined matrix arc variance
IRT1	1	Integer	Record type one (ID)
IDMAT	1	Integer	Matrix identification number
NR $\varnothing$ W	1	Integer	Number of rows in matrix
NC $\varnothing$ L	1	Integer	Number of columns in matrix
N $\varnothing$ B	1	Integer	Number of observations
ITYPE	1	Integer	Matrix type
BNAME	2	Alpha	Matrix alpha-numeric name
IRT2	1	Integer	Record type two (label)
LABS	101	Integer	Parameter labels record
LA BSI	82	Integer	Labels of inverted matrix
NR $\varnothing$ WI	1	Integer	Number of rows in inverted matrix
LA BSN	60	Integer	Labels of parameters solved for by backsubstitution
NR $\varnothing$ WN	1	Integer	Number of elements in LA BSN
NGRAV	1	Integer	Number of gravity parameters
NSTAT	1	Integer	Number of station parameters
NARC	1	Integer	Number of arc parameters
JPAGE	1	Integer	Printed output page number

<u>MNEMONIC</u>	<u>NO. WDS.</u>	<u>FORMAT</u>	<u>CONTENTS</u>
LINE	1	Integer	Printed output line number
NØREC	1	Integer	Number of backspaces necessary to position tape at 10001 record
NØREC2	1	Integer	Number of backspaces necessary to position tape at 10001 record
ØBVS	1	Real	Total number of observations
ALPHA	12	Alpha	Page header for printed output
IDCØMB	1	Integer	Matrix identification number for combined matrix
NRØWC	1	Integer	Number of rows in combined matrix
NCØLC	1	Integer	Number of columns in combined matrix
NØBC	1	Integer	Number of observations in combined matrix
ITYPEC	1	Integer	"3"
BNAMEC	2	Alpha	Combined matrix alpha name
LABSC	101	Integer	Parameter label record of combined matrix

**SECTION IV**  
**SUBROUTINE WRITE-UPS**

NAME	MERGE	
PURPOSE	Overall control program for the B matrix tape MERGE system.	
CALLS	BEDIT	Binary tape to tape routine
	ERROR	Error exit from MERGE
	MEDIT	Matrix edit routine
OPTIONS	IEDIT	Edit option, indicates either no editing, or one of five edit formats (see subroutine write up for MEDIT)
	IOOLDM	Save old matrices option, indicates whether or not there are matrices to be saved on the output tape.
	NODELT	Deletion option, indicates whether or not certain matrices are not to be written from the input tapes to the output tape.
INPUT	NOTAP	Number of input tapes, one through four.
	IDELT	List of matrices to be deleted, if any.
	ALPHA	Alpha-numeric page header for printed output, if any.
OUTPUT	Merged tape on tape 30	
TAPES	1) USED	18, 20, 28 and 29, input tapes. 30 is the output tape.
	All tapes are rewound at the beginning and end of MERGE.	

ERROR  
CHECKS

Error number 101 indicates too many matrices were to  
be merged onto one output tape.

Error number 102 indicates too many input tapes requested

NAME	BEDIT (NØREC, NØTAP, ITYP)		
PURPOSE	Writes a matrix to be edited onto tape 30		
CALLED BY	MAIN	Overall control program for SØLVE	
CALLS	ERRØR	Handles error exits from SØLVE	
INPUT	NØREC	The number of times a tape must be back-spaced to position it at the X0001 (ID) record	
	NØTAP	The logical tape number of the input matrix	
	ITYP	An integer indicating the desired format for the edited matrix. This is read from input card type three, the edit card.	
OUTPUT	The matrix, with ITYPE modified, written in standard format on tape 30		
TAPES	USED	30	Output, edit tape
		NØTAP	Input, holds the matrix to be edited
	START	30	Before the old -49991 record
		NØTAP	NØREC records past the ID, (X0001) record of the input matrix
	END	30	Before the new -49991 record
		NØTAP	After the last 10003 record
ERROR CHECKS	Error number 6 indicates that NØTAP is not 18, 20, 28 or 29		
NOTES	The code word ITYPE, used by the EDIT program to determine the type of matrix and the edit format, is computed as follows: $\text{ITYPE} = 100 * \text{ITYP} + \text{ITYPE},$ where the old ITYPE is as it appears in the standard matrix.		

NAME	CHECK (NØLIN)	
PURPOSE	Controls the page feeding and writes the page header for printed output	
CALLED BY	MAIN MINV INCK ØPARC ØPGRAV ØPSTAT	Overall control program for SØLVE Matrix inversion routine Checks input format and values Prints and punches arc parameter output Prints and punches gravity parameter output Prints and punches station parameter output
INPUT	NØLIN LINE ALPHA JPAGE	The number of lines to be printed The number of lines which appear on the current page A twelve-word array consisting of the page header The current page number
OUTPUT	LINE is incremented. If the new LINE is greater than forty-five, a new page is started and JPAGE is incremented.	

NAME            ERROR (NERR)

PURPOSE       Handles error exits from S<sub>O</sub>LVE

CALLED BY      MAIN        Main control routine for S<sub>O</sub>LVE  
                  BACKSB     Backsubstitution routine  
                  BEDIT      Writes matrices to the Edit tape  
                  CQMB      Matrix combination routine  
                  ELIM      Matrix elimination routine  
                  ØPARC     Prints and punches arc parameter output  
                  INCK      Checks input format and values

INPUT           NERR      Error number  
                  PERM      The matrix ID and label records are in PERM  
                              common, as usual

OUTPUT          The following messages are printed:  
  
JOB TERMINATED DUE TO ERROR NUMBER XXXX.  
IDENT        NRØWS      NCØLS      BNAME      TYPE  
XXXXXX      XXXXX      XXXXX      Alpha      X

The "XXXXX" are the appropriate numbers.

NAME MEDIT

PURPOSE This routine "prints" (i.e., writes on the systems output tape) all matrices on tape 30, in a specified format.

CALLED BY MERGE Overall control program of MERGE

CALLS MINV Matrix inversion routine.

OPTIONS ITYP

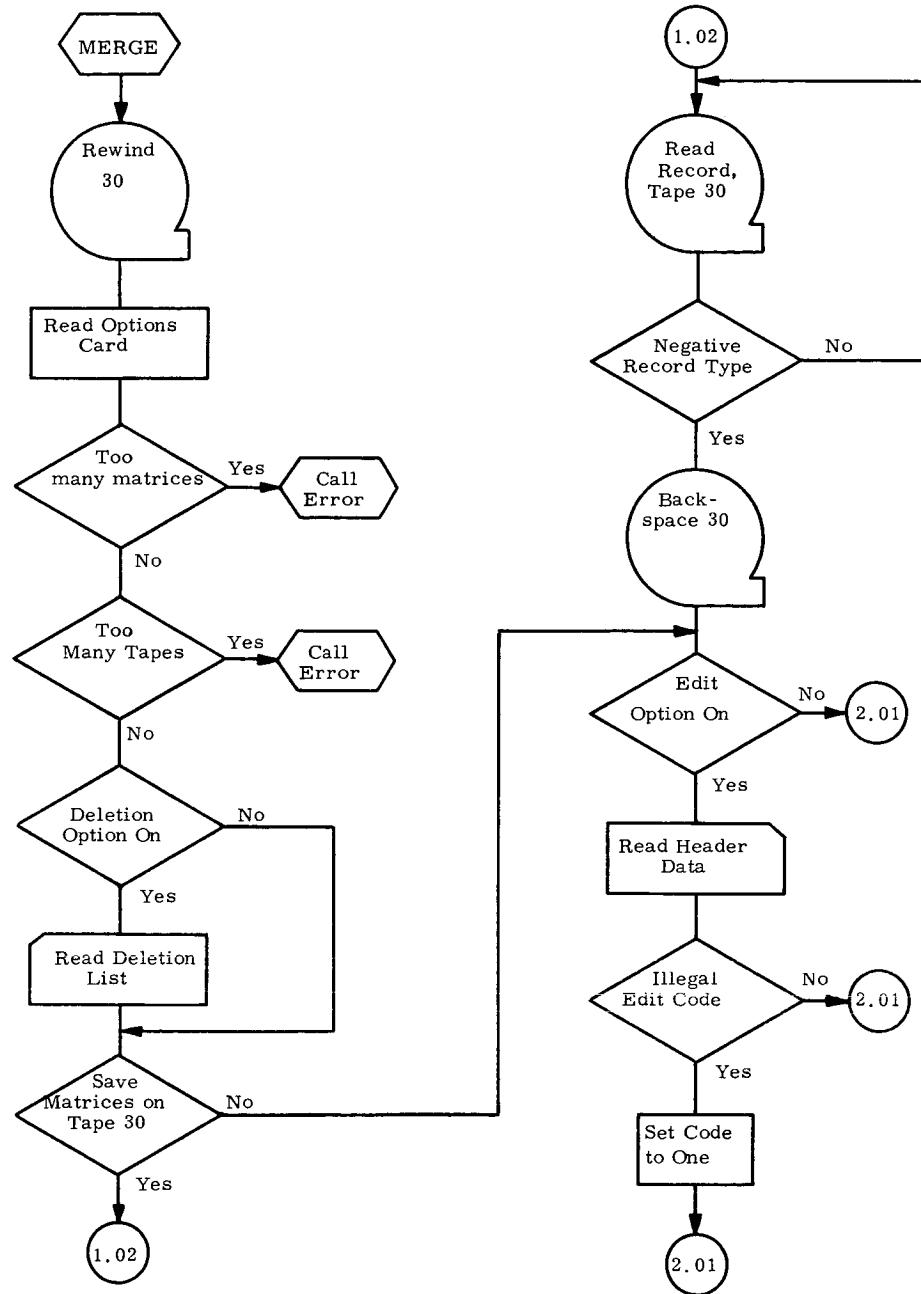
- 1 Print matrix as is; i.e., unnormalized. The rectangular matrices (parameter set matrices and back-substitution matrices) may only be edited in the unnormalized format.
- 2 Print normalized matrix; i.e., the diagonal elements are set to one.
- 3 Print the inverse of the input matrix, with the solution vector as the right hand side.
- 4 Print the Identification and Label records only; i.e., records X0001 and X0002.
- 5 Print the normalized inverse matrix. Also print the standard deviation vector; i.e., the square roots of the diagonal elements of the inverse matrix.

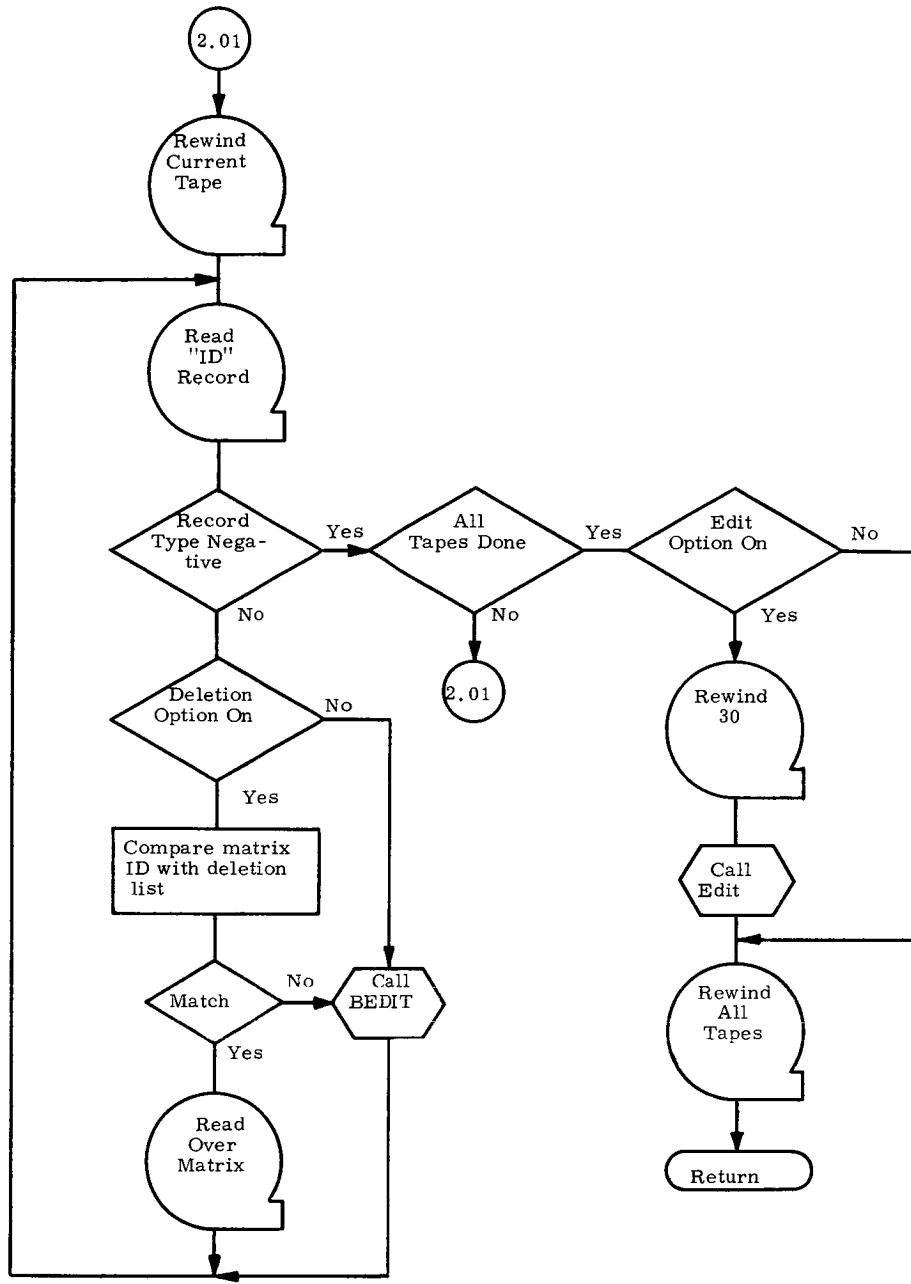
OUTPUT            The matrices in the desired format on the systems  
                  output tape.

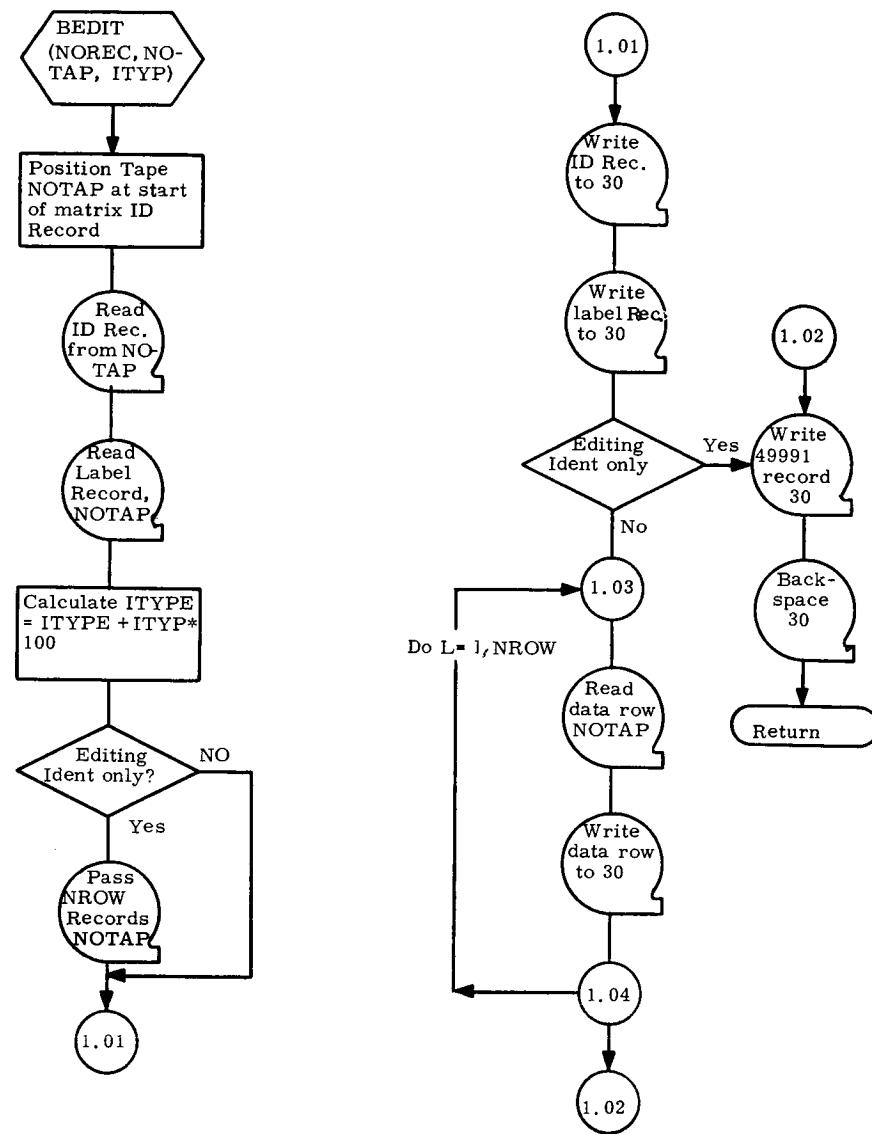
TAPES            USED        30        Input, edit tape  
                  START      30        Rewound  
                  END        30        Rewound

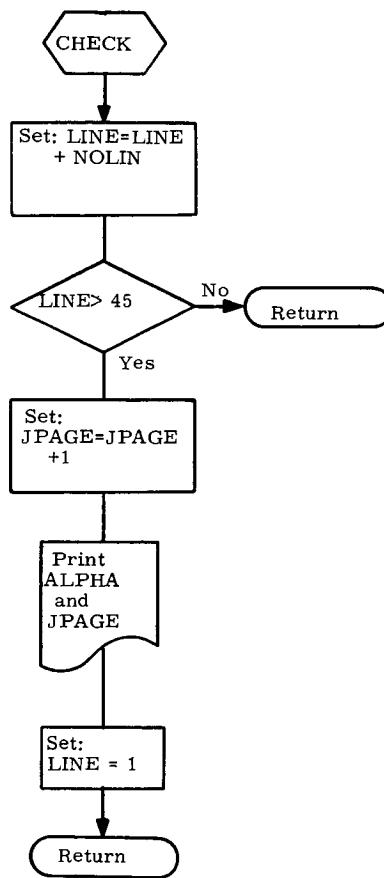
NAME	MINV (N)	
PURPOSE	Inverts and solves a matrix	
METHOD	A Gauss-Jordan elimination, with a pivot search on the diagonal elements	
CALLED BY	INVR	Control program for matrix inversion
	EDIT	Edits matrices for printing
CALLS	CHECK	Controls page spacing of printed output
INPUT	N	Order of matrix, not to exceed 82
	A	Two-dimensional array containing the matrix to be inverted
	B	The Right Hand Side vector
OUTPUT	A	Inverted matrix
	B	The Solution vector
ERROR CHECKS	If a pivot element is found which is negative or zero, a message is printed indicating that the matrix is not positive definite and in which row the bad pivot occurred. However, the run continues.	

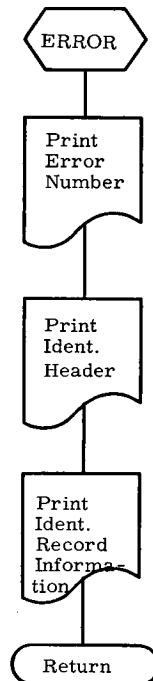
SECTION V  
FLOW CHARTS

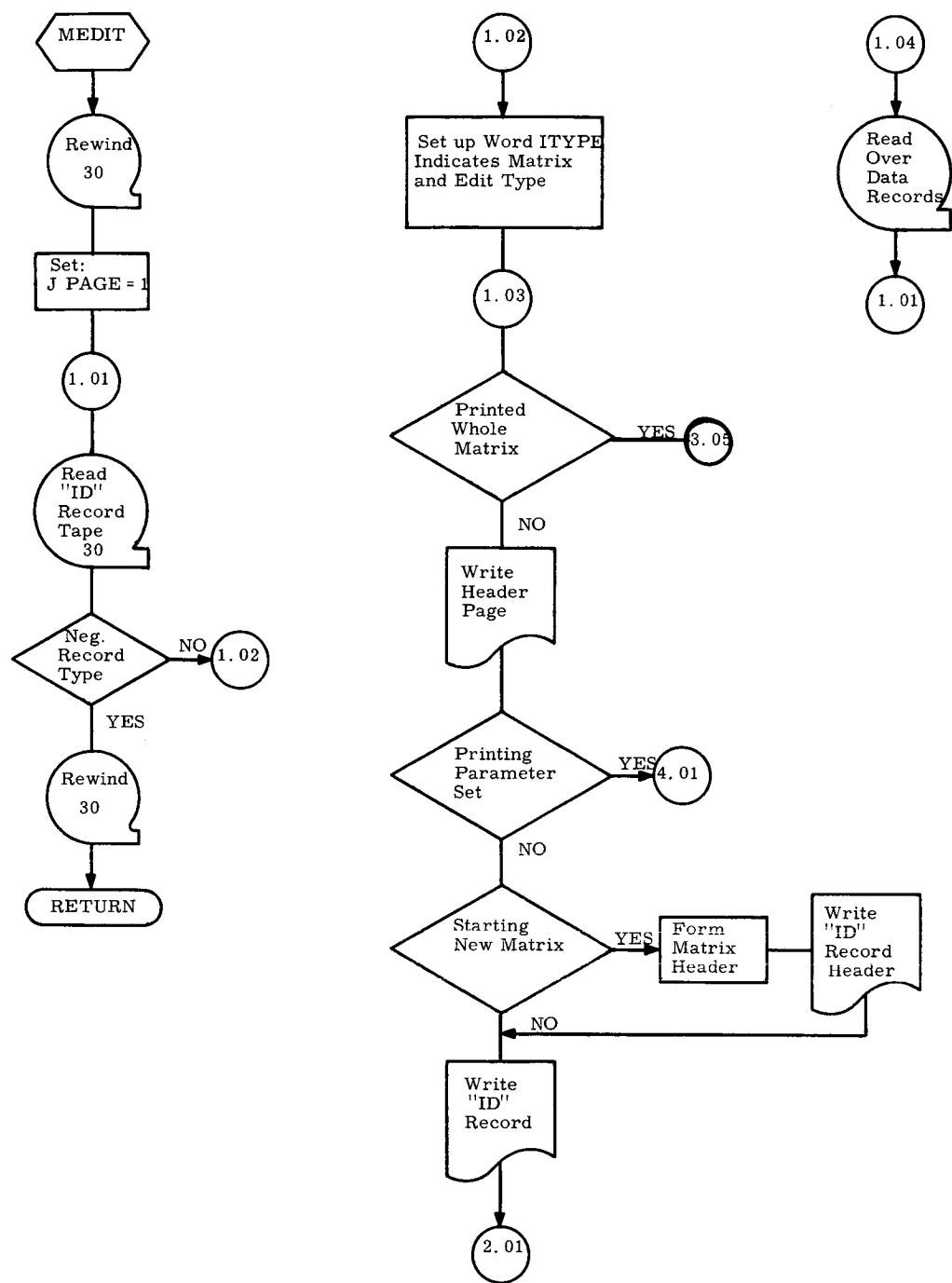


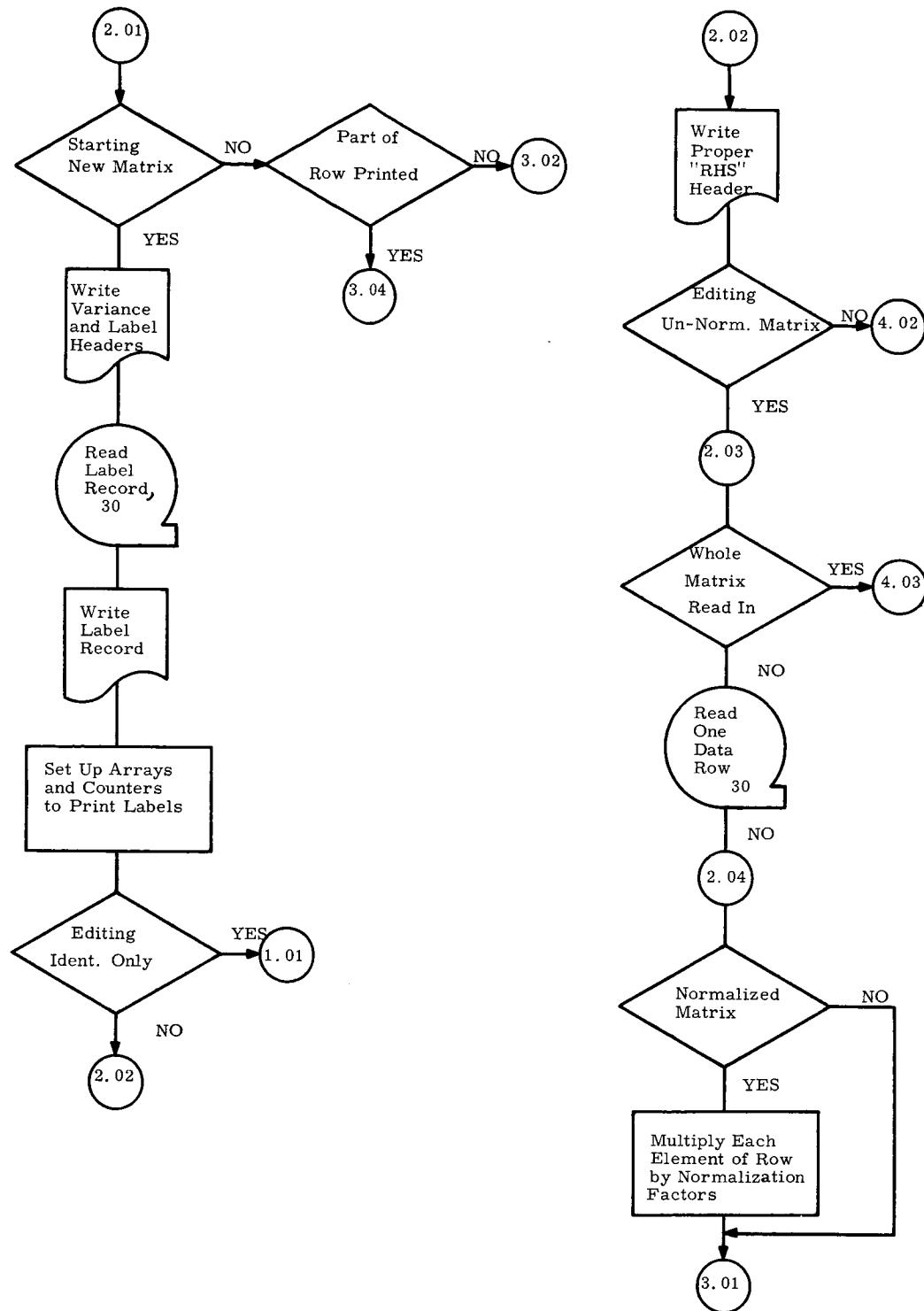


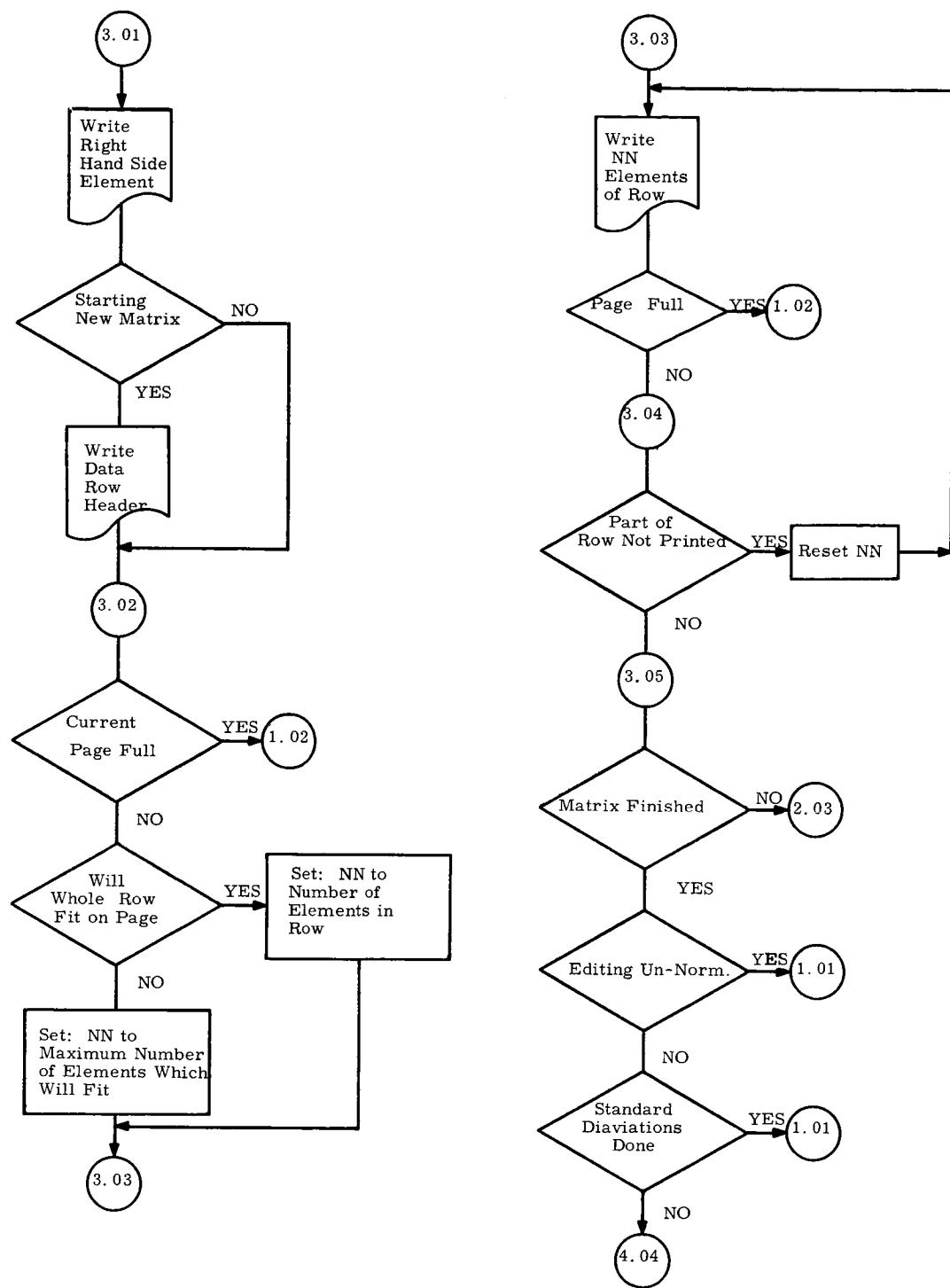


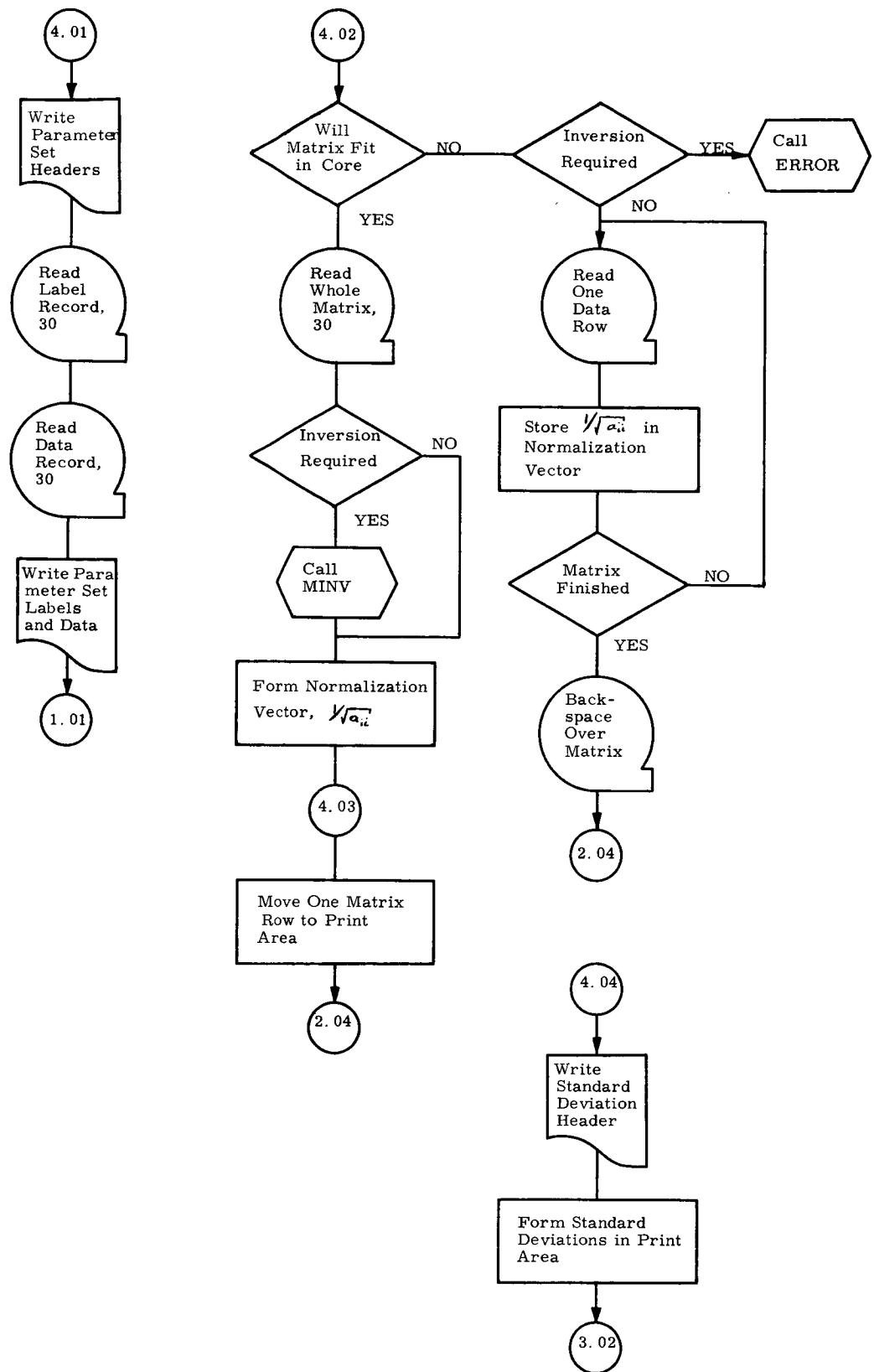


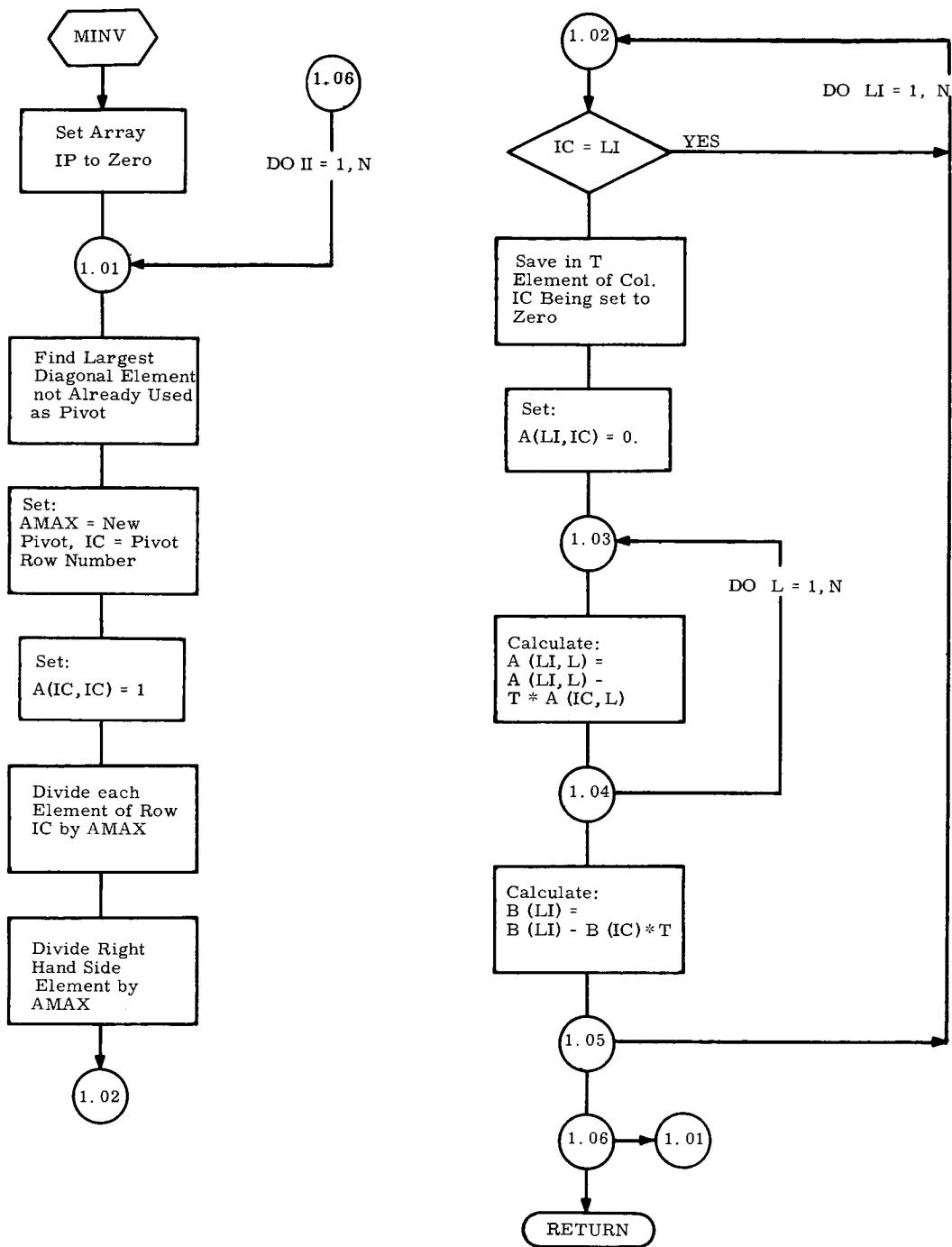












PART 8  
COVARIANCE MATRIX PROGRAM

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## SECTION V FLOWCHARTS

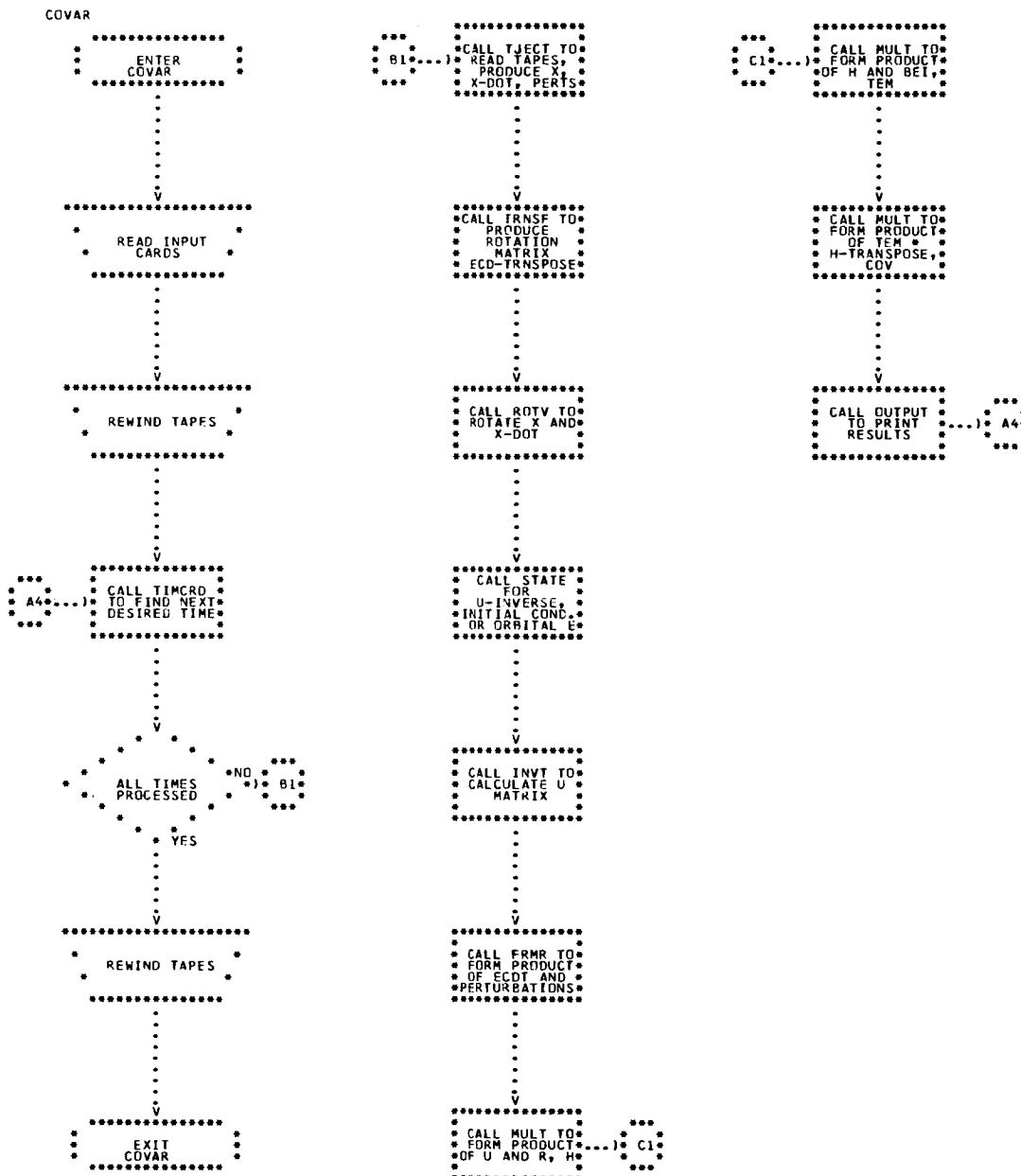
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SECTION I  
INTRODUCTION

## INTRODUCTION

When required, the covariance matrix on the satellite state may be obtained at any time using the covariance matrix at the beginning of the arc and the integrated values of the perturbation equations. The program accomplishing this is not in one sense a part of the LUNGFISH program, since it is needed neither in performing the solution nor in iterating to a new solution. It is used to provide the measure of the uncertainty in the estimated state at any required time.

**SECTION II**  
**SYSTEM FLOW CHART**



SECTION III  
USER INFORMATION

## INPUT CARDS

- 1) Card type One, trajectory identification number  
cc 1-5 Integer trajectory tape identification number
  
- 2) Card type Two, run time limits  
cc 1-24 Double precision start time for run, in seconds from the beginning of the year  
cc 25-48 Double precision final time for run, in seconds from the beginning of the year  
cc 49-72 Double precision gravity of the moon
  
- 3) Card type Three, state inverse matrix BEI(6,6)  
cc 1-24 Double Precision BEI(1,J)  
cc 25-48 Double Precision BEI(2,J)  
cc 49-72 Double Precision BEI(3,J)  
cc 1-24 Double Precision BEI(4,J)  
cc 25-48 Double Precision BEI(5,J)  
cc 49-72 Double Precision BEI(6,J)  
J=1,6 Card type three consists of two cards. It takes a total of twelve cards to hold the BEI matrix.
  
- 4) Card type Four, Debug print options  
The following are logical options, with a "T" (True) indicating debug printout desired, and an "F" (False) or a blank indicating no printout desired.  
cc 5 Print the input BEI matrix  
cc 10 Print the input Time; and an arc parameter label from the trajectory tape  
cc 15 Print the G array from TJECT  
cc 20 Print the unrotated position and velocity arrays  
cc 25 Print the perturbations matrix  
cc 30 Print the ECD<sup>T</sup> matrix  
cc 45 Print the ORBPAR and ORBDOT arrays from state  
cc 50 Print the U<sup>-1</sup> matrix  
cc 55 Print the R matrix  
cc 60 Print the H matrix
  
- 5) Card type Five, Time Cards  
cc 1-5 Integer card type, any integer >0  
cc 6-30 Double precision time, in seconds from the start of the year
  
- 6) Card type Six, End of Times card  
cc 1-5 Integer card type, any integer < 1

## OPERATING INSTRUCTIONS

- 1) The system control cards required in the overall deck setup are:  
      \$JOB

\$SETUP 04

\$EXECUTE IBJOB

\$IBJOB

### COVAR decks, source or binary

\$DATA

## COVAR data deck

- 2) The tape setup is:

DCS Unit  
04

### Tape Function

### Input trajectory tape

16

Scratch tape, or disk file

- 3) Output consists only of printing.

PROGRAM RESTRICTIONS

- 1) The time period over which the covariance matrices are to be computed may not span a year, i.e., year cross-over may not occur.

## ERROR MESSAGES

<u>NUMBER</u>	<u>SUBROUTINE</u>	<u>MEANING</u>
1	TJECT	Illegal record type on the trajectory tape
2	TREAD	Trajectory tape data records are out of sort, i.e., the times are wrong
4	EREAD	Illegal record type on ephermis tape
5	MAIN	Year cross over requested, COVAR cannot process data with year-crossover
6	MAIN	Ten of the requested times were not on the trajectory tape
7	MAIN	Ten of the $U^{-1}$ matrices generated could not be inverted

### PROGRAM DECK ARRANGEMENT

The decks for COVAR should be in approximately the following order

- .UN18.
- .UN30.
- MAIN
- ERROR
- FRMR
- INVT
- MULT
- OUTPUT
- ROTV
- TIMCRD
- TRNSF
- STATE
- XTOORB
- ORBTOX
- INTPAR
- \*TJECT
- TREAD
- INTERP
- ERead

\*The four following decks must be in this order.

FILE BLOCK PROGRAM OPTIONS

- 1) Tape 18:  
    Filename is "UNIT18"  
    Mode is "BIN"  
    Unit assignment is "A(1)"
  
- 2) Tape 30  
    Filename is "UNIT30"  
    Mode is "BIN"  
    Unit assignment is "B(3)"

## TRAJECTORY AND PERTURBATION TAPE

### RECORD TYPES

100	Trajectory tape header
110	Parameter and label record
120	Ephemeris header
130	Ephemeris records
140	Trajectory and perturbation records
150	Trajectory end of file record

### FORMAT

RECORD TYPE	# OF WORDS	MN	FORMAT	CONTENT
100	1	ITYPET	INTEGER	Record type
	1	IDENTT	INTEGER	Identification number for arc
	1	ISATNO	INTEGER	Satellite number
	1	NUMGA	INTEGER	Number of partials calculated by INTEGRATION
	1	NUMGRV	INTEGER	Number of gravity partials calculated by INTEGRATION
	1	ISYR	INTEGER	Start year of ARC
	2	ARCSEC	DOUBLE	Start time of arc (seconds from beginning of year)
	2	ARCEND	DOUBLE	Time of last record (seconds from beginning of current year)
	2	DURA	DOUBLE	Duration of arc
	2	DELTAT	DOUBLE	Interval of storage

RECORD TYPE	# OF WORDS	MN	FORMAT	CONTENT
110	1	ITYPET	INTEGER	Record type
	NUMGAx2	PARAMS	DOUBLE	Initial parameter values for variables in integ- ration
	NUMGA	LABELS	INTEGER	Labels for parameters used in integration
120	1	ITYPET	INTEGER	Record type
	1	IDAY1	INTEGER	First day on tape (days from year start)
	1	IDAYS	INTEGER	Number of days of data equal number of Ephemeris records
	2	YRSECS	DOUBLE	Number of seconds in start year
	2	H1	DOUBLE	H for start year
	2	H2	DOUBLE	H for second year
130	1	ITYPET	INTEGER	Record type
	2	TZERO	DOUBLE	Base time for interpolation
	3x9x2	PXE	DOUBLE	INTERPOLATION Polynominal coefficients for earth- moon vector PXE(I,J)=I,3 J=1,9
	3x5x2	PCDTR	DOUBLE	Interpolation polynominal coefficients for $\Delta h$ PBTR(I) I=1,5
	3x3x5x2	PEC DTR	DOUBLE	PEC DTR (I,II,J) I=1,3 II=1,3 J=1,5

RECORD TYPE	# of WORDS	MN	FORMAT	CONTENT
140	1	ITYPET	INTEGER	Record type
	2	TIMET	DOUBLE	Time of (position, acceleration and perturbations) seconds from beginning of year
	3x2	XSAT	DOUBLE	Position of satellite at TIMET (KM)
	3x2	ASAT	DOUBLE	Acceleration of satellite at TIMET(KM)
	3xNUMGAx2	P	DOUBLE	Array of perturbations
150	1	ITYPET	INTEGER	Record type
	2	TIMET	DOUBLE	Time of last trajectory and perturbation set
	3x2	XSAT	DOUBLE	Last position
	3x2	ASAT	DOUBLE	Last acceleration
	3xNUMGAx2	P	DOUBLE	Last array of perturbations

HEAD COMMON DEFINITIONS

MNEMONIC	# of WORDS	FORMAT	CONTENTS
ARCSEC	1x2	DOUBLE	Start time of arc, in seconds
ARCEND	1x2	DOUBLE	Time of last record on trajectory tape
DELTAT	1x2	DOUBLE	Interval of storage
YRSECS	1x2	DOUBLE	Number of seconds in start year
TIME4	1x2	DOUBLE	Time of the fourth time step, in seconds
TIMET	8x2	DOUBLE	Table of eight time steps corresponding to trajectory data
F	(8x3x77)x2	DOUBLE	Eight consecutive trajectory and perturbation arrays
DURA	1x2	DOUBLE	Duration of arc
S	1x2	DOUBLE	Variable input parameter for interpolation routine
ISPN	1	INTEGER	Switch to indicate year crossover
IDEN	1	INTEGER	Identification number for arc
ISATNO	1	INTEGER	Satellite number
NUMGA	1	INTEGER	Number of gravity partials
ISYR	1	INTEGER	Start year of arc
IDAY	1	INTEGER	First day on trajectory tape
IDAYS	1	INTEGER	Number of days of ephemeris data
ILR	1	INTEGER	Switch indicating whether or not a time was accepted
LABEL	1	INTEGER	Parameter label for last arc parameter

MEPHM COMMON DEFINITION

<u>MNEMONIC</u>	<u># of WORDS</u>	<u>FORMAT</u>	<u>CONTENTS</u>
PECDTR	(3x3x5)x2	DOUBLE	Polynomial coefficients for (ECD) <sup>T</sup> matrix
T	1x2	DOUBLE	Time associated with PECDTR

MNEMONIC DEFINITIONS

<u>MNEMONIC</u>	<u># of WORDS</u>	<u>FORMAT</u>	<u>CONTENTS</u>
SRTIME	1x2	DOUBLE	Start time for run, in seconds
FNTIM	1x2	DOUBLE	Final time of run, in seconds
GMU	1x2	DOUBLE	Moon gravity
BEI	(6x6)x2	DOUBLE	Inverse of state portion of B matrix
TIME	1x2	DOUBLE	Current time
G	(3x16)x2	DOUBLE	Array of position, velocity and perturbations from TJECT
XOLD	3x2	DOUBLE	Unrotated satellite position
XDOTO	3x2	DOUBLE	Unrotated satellite velocity
XNEW	3x2	DOUBLE	Rotated satellite position
XDOTN	3x2	DOUBLE	Rotated satellite velocity
PRTBR	(6x6)x2	DOUBLE	Perturbations matrix
ECDT	(3x3)x2	DOUBLE	Rotation matrix, ECD <sup>T</sup>
ORBEE	6x2	DOUBLE	Orbital elements
ORBPAR	18x2	DOUBLE	Partials of satellite position
ORBDOT	18x2	DOUBLE	Partials of satellite velocity
U	(6x6)x2	DOUBLE	Matrix of partials, U
R	(6x6)x2	DOUBLE	Rotated perturbation matrix
H	(6x6)x2	DOUBLE	Work area
TEM	(6x6)x2	DOUBLE	Work area
COV	(6x6)x2	DOUBLE	Covariance matrix

**SECTION IV**  
**SUBROUTINE WRITE-UPS**

NAME	MAIN	
PURPOSE	Overall control program for the covariance matrix calculation. MAIN reads the input, sets up various arrays and switches, and calls the routines to generate the covariance matrix and other output.	
CALLS	ERROR	Error exit from COVAR
	FRMR	Multiplies a block diagonal matrix of $ECD^T$ times a six by six matrix of perturbation partials.
	INVT	Inverts a matrix
	MULT	Multiplies two matrices
	OUTPUT	Prints the output matrix and vectors
	ROTV	Rotates the vectors $X$ and $\dot{X}$ to selenographic frame of time
	STATE	Calculates orbital elements or initial conditions, and the matrix of partials, $U^{-1}$
	TIMCRD	Determines current time to be processed
	TJECT	Reads trajectory tape, interpolates for position and velocity vectors and perturbations matrix
	TRNSF	Evaluates $ECD^T$ polynomial for $ECD^T$ matrix
INPUT	TIME	Array of times at which the covariance matrix and position vectors are to be calculated
	BEI	Inverse of the state portion of a B matrix, produced by SOLVE

OUTPUT      For each input time, the corresponding covariance matrix in selenographic frame of time, and the orbital elements are printed

TAPES      USED      18    Trajectory tape  
              30    Scratch ephemeris tape

ERROR      Error number five occurs if the start time is larger than the  
CHECKS     finish time, that is, if a run was requested with year crossover.  
              Error number six occurs if more than ten of the requested times  
              are not on the trajectory tape.  
              Error number seven occurs if more than ten of the  $U^{-1}$  matrices  
              formed could not be inverted

NAME	EREAD (TIME, IENT)	
PURPOSE	Read ephemeris data that corresponds to time of observation.	
CALLED BY	MAIN	Overall control program for NORMEQ
INPUT	TIME	Time of observation
	IENT	= True, initial entry to subroutine
	IENT	= False, subsequent entries to subroutine.
OUTPUT	TZERO	Time of ephemeris data
	PXE	Interpolation polynomial coefficients for earth-moon vector, PXE (3, 9)
	PCDTR	Interpolation polynomial coefficients for rotation matrix $(CD)^T$ , PCDTR (3, 3, 5)
	PBTR	Interpolation polynomial coefficients for $\Delta h_{PBTR}(.5)$
NOTES	EREAD reads the ephemeris data from tape 30. All output goes into the INDATA common area.	

NAME                    ERROR(N)

**PURPOSE** Error exit from COVAR

CALLED BY MAIN Overall control program

**ERED**      Reads the ephermis tape

TJECT Control program for trajectory tape read and  
interpolation

**TREAD**      Reads the trajectory tape

INPUT N Error number

**OUTPUT** This subroutine prints the following message and then halts the run.

**ERROR NUMBER N**

NAME            FRMR (ECDT, PRTBR, R)

PURPOSE        Multiply the block diagonal matrix containing  $ECD^T$  times  
                  the matrix of perturbations, PRTBR

CALLED BY      MAIN            Overall control program

INPUT           ECDT          Rotation matrix  $ECD^T$ ,     order 3x3  
                 PRTBR         Matrix of perturbations, order 6x6

OUTPUT          R              Product matrix, order 6x6

NOTES           The matrix R is actually formed by multiplying  $ECD^T$  times  
                  each quarter of the matrix PRTBR, to form the corresponding quarter  
                  of R

NAME                   INTERP (F1, ICOMP, IINTER, DTIME, G1, S)

PURPOSE               Form position, acceleration, velocity and third derivative of trajectories and perturbations.

CALLED BY             MAIN, overall control program for NORMEQ

INPUT                 F1               Input table of trajectories and perturbations  
                        F1(8, 3, 77)  
                       ICOMP           Number of components  
                       IINTER        Number of functions  
                       DTIME           Interval of storage  
                       S               ( $T_{obs}$  - 4<sup>th</sup> time step)/ interval of storage

OUTPUT                G1               Output table of interpolated trajectories and perturbations   G1(3,2,77)

NAME	INTPAR	
PURPOSE	Calculates partials of initial conditions with respect to orbital elements or initial conditions.	
CALLED BY	STATE	control program for conversions
INPUT	XER	initial position of satellite
	XDOTZ	initial velocity of satellite
	PZ	values from ORBTOX
	ERB	orbital elements
	GMU	moon gravity constant
	ORBUSE	logical flag; compute partials of initial conditions with respect to orbital elements if true; partials of initial conditions with respect to initial conditions otherwise.
OUTPUT	ORBP AZ	partials of satellite position with respect to orbital elements.
	ORBDOZ	partials of satellite velocity with respect to orbital elements.
NOTES	If ORBUSE is false a sample "unit" vertex is generated.	

NAME INVT (A, ISW)

PURPOSE Invert matrix A, leaving the inverse matrix in area A

METHOD This is a Gauss-Jordan elimination procedure with a full pivot search

CALLED BY MAIN Overall control program

INPUT A The six by six matrix to be inverted

OUTPUT A The inverse matrix

ISW A logical switch which is TRUE if the matrix inverted successfully, and FALSE if it did not.

NAME            MULT (AMAT, BMAT, CMAT)

PURPOSE        This routine multiplies the matrices AMAT and BMAT to produce CMAT

CALLED BY      MAIN        Overall control program

INPUT            AMAT        A matrix of order six  
                  BMAT        A matrix of order six

OUTPUT          CMAT        A matrix of order six

NAME	ORBTOX	
PURPOSE	Transforms orbital elements to initial conditions and computes values for use in INTPAR.	
CALLED BY	STATE	control program for conversions.
INPUT	ERB	orbital elements
	GMU	moon gravity constant
	ORBIN	true implies orbital element input; false, initial conditions.
OUTPUT	XFR	initial coordinates of satellite
	XDOTZ	initial velocities of satellite
	PZ	array of values for INTPAR
ERROR CHECKS	If iteration for PHI fails to converge, the message NON CONVERGENCE FOR PHI is printed and the run is stopped.	
NOTES	<ol style="list-style-type: none"><li>1. If initial conditions need not be calculated only the first sections of the program are executed, those necessary to provide the input data for INTPAR.</li><li>2. Several sets of equivalances are necessary because of previous definitions in the routine.</li></ol>	

NAME            OUTPUT (XNEW, XDOTN, COV, TIME, ORBEE)

PURPOSE        Prints the output data for each time requested

CALLED BY      MAIN        Overall control program

INPUT            XNEW        Position of satellite in selenographic frame of time  
                  XDOTN      Velocity of satellite in selenographic frame of time  
                  COV         Covariance matrix  
                  TIME        Current time  
                  ORBEE      Orbital elements

OUTPUT          All input items are printed

NAME            ROTV (ECDT, XOLD, XDOTO, XNEW, XDOTN)

PURPOSE        Rotates position and velocity of satellite to selenographic frame of time

CALLED BY      MAIN        Overall control program

INPUT           ECDT        Rotation matrix,  $ECD^T$   
                XOLD        Position of satellite  
                XDOTO       Velocity of satellite

OUTPUT          XNEW        Rotated position of satellite  
                XDOTN       Rotated velocity of satellite

NAME	STATE	
PURPOSE	Control program for conversion of initial conditions to orbital elements and vice versa and for calculation of starting array of arc partials.	
CALLED BY	INPUT	Input program for integration
CALLS	ORBTOX	Computes initial conditions from orbital elements and prepares values for INTPAR
	XTOORB	Computes orbital elements from initial conditions.
	INTPAR	Calculates partials of initial conditions with respect to orbital elements or initial conditions.
INPUT	ORBIN	True implies orbital elements input; false, initial conditions.
	ORBUSE	True implies orbital elements output; false, initial conditions.

NAME            TIMCRD (IEN, SRTIM, FNTIM, TIME)

PURPOSE        This subroutine reads the times from cards and returns them to the main routine one at a time, after checking to be sure they are within the time period for this run.

CALLED BY      MAIN            Overall control routine

OPTIONS        IEN            A logical switch, TRUE for the first call to TIMCRD, and FALSE for the rest of the run

INPUT           SRTIM        Start time for this run  
                FNTIM        Final time for this run

OUTPUT          TIME         Current time

NOTE            Any input time outside of the time period for this run is ignored

NAME TJECT (IEN, IS3, G, TIME, LAB)

PURPOSE Position ephemeris tape; read and interpolate trajectory and arcs at time of observation

CALLED BY MAIN Overall control program

CALLS TREAD Read trajectory tape  
EREAD Position ephemeris tape  
INTERP Interpolate trajectory and arcs at time of observation  
ERROR Input tapes have wrong record types

INPUT IEN =True, initial entry. False, otherwise (set to false by TJECT)  
IS3 =TRUE, observation time accepted.  
=FALSE, observation time not within range of trajectory arc  
TIME TIME of observation

OUTPUT G Table of interpolated trajectory and arcs  
LAB Label of one of the arcs on the trajectory tape.

ERROR CHECK Error number 1 indicated an illegal record type on the trajectory tape.

NAME	TREAD (TIME, TIMEA, DELTAA, ISPAN, IENT, S, F2, ILR, N).	
PURPOSE	Reads in appropriate trajectory and perturbation arrays.	
CALLED BY	MAIN - Overall control program for NORMEQ.	
INPUT	TIME	Time of observation.
	TIMEA	4th time step (on trajectory tape) from previous tape read; or , if initial positioning of tape, TIMEA will be equal to the initial time on the trajectory tape - 5* the time step interval (DELTAA).
	DELTAA	Time step interval.
	ISPAN	= 2, when run spans years. = 1, otherwise.
	IENT	= True, Initial entry to TREAD. = False, all subsequent entries.
	N	Total nr. of trajectory and perturbation functions.
OUTPUT	S	Variable for 8 point Legrangian.
	F2	Storage table F2 (I, J, K) I=1, 8, J=1, 3 K = 1, N.
	ILR	Set to 3-normal return . Set to 2-observation time occurs after final trajectory time. Set to 1-observation time occurs before initial trajectory time.
NOTES	TREAD uses tape 18.	

NAME TRNSF (TIME, ROTATE)

PURPOSE Evaluate the  $ECD^T$  polynomial to produce the matrix ROTATE

CALLED BY MAIN Overall control program

INPUT TIME Current time

PECDTR A (3x3x5) array of polynomial coefficients for the  $ECD^T$  matrix

TMID The time associated with PECDTR

OUTPUT ROTATE The rotation matrix  $ECD^T$ , of order three

NAME	XTOORB	
PURPOSE	Calculates orbital elements from initial conditions.	
CALLED BY	STATE	Control program for conversion.
INPUT	XER	Initial satellite coordinate.
	XDOTZ	Initial satellite velocity.
	GMU	Gravity constant of moon (GRAVMN)
OUTPUT	ERB	Computed orbital elements
ERROR CHECK	If AI is greater than $\pi$ , the message AI GREATER THAN PI is printed, and the run continues.	

SECTION V  
FLOW CHARTS

